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Evaluation of the long-term performance of the deep U-type borehole heat exchanger on different geological parameters using the Taguchi method

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Abstract

In recent years, deep geothermal energy has become a solid option for building heating worldwide. For the densely populated urban area, a novel closed-loop system of the deep U-type borehole heat exchanger (DUBHE) has attracted attention in northern China. In order to achieve the evaluation of geological parameters on the long-term performance of DUBHE, thermal conductivity, geothermal gradient, specific heat capacity, groundwater flow direction, and Darcy velocity are selected in this paper and all the parameters are set in three levels. And orthogonal test $L_{18}(3^5)$ is established by adopting the Taguchi method for the reduction of simulation time cost. Three evaluation indexes are introduced to investigate the impacts of geological parameters on the performance of DUBHE and obtain the optimal set, including average outlet temperature T_{out} , maximum cumulative heat extraction amount Q_{total} and soil temperature decay rate D_{soil} . Results show that the geothermal gradient has the most significant effect on T_{out} and

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Q_{total} , and its contribution degree is 70.14% and 62.10% respectively. As for the D_{soil} index, the most influential parameter is specific heat capacity and the corresponding contribution ratio is 92.41% determined by the analysis of variance (ANOVA) method. For the optimized combination by adopting matrix analysis, the T_{out} reaches 33.92 °C, the Q_{total} is 284.08 TJ and the D_{soil} of the optimized scenario is 12.66% after the long-term operation. In addition, according to the orthogonal test results, this study intuitively discusses the potential of carbon emission reduction for the DUBHE under the typical geological conditions in northern China. The study results presented in this work can guide the system design of DUBHE and serve as the reference for the decision-maker in the application of deep geothermal heating technology.

Keywords: Deep U-type borehole heat exchanger (DUBHE); Long-term performance; Geological parameters; Taguchi method; Evaluation index

1

2 **Nomenclature**

3 **Roman letters**

| | | |
|----|--------------|-------------------------------------------------------------|
| 4 | c | specific heat capacity ($\text{J kg}^{-1} \text{K}^{-1}$) |
| 5 | H | heat sink/source term (W m^{-3}) |
| 6 | \mathbf{I} | identity matrix (-) |
| 7 | D | decay rate of soil temperature (-) |
| 8 | L_1 | length of descending/ascending pipe (m) |
| 9 | L_2 | length of horizontal pipe (m) |
| 10 | m | number of factor levels (-) |
| 11 | n | total number of experiments (-) |
| 12 | r | repeated number of each level experiment(-) |
| 13 | d | pipe diameter(m) |
| 14 | i | number of sample iterations(-) |
| 15 | Q | heat extraction (TJ) |

16 q_n heat flux (W m^{-2})

17 y simulated result

18 T temperature ($^{\circ}\text{C}$)

19 t time (s)

20 \mathbf{v} vector of flow velocity (m s^{-1})

21 **Greek Letters**

22 ϵ rock/soil porosity (-)

23 β_L longitudinal heat dispersivity (m)

24 Γ boundary

25 λ thermal conductivity ($\text{W m}^{-1} \text{K}^{-1}$)

26 Λ thermal hydrodynamic dispersion tensor ($\text{W m}^{-1} \text{K}^{-1}$)

27 Φ thermal resistance ($\text{m}^2 \text{K/W}$)

28 ρ density (kg m^{-3})

29 **Operators**

30 Δ difference operator

31 ∇ nabla vector operator

32 \sum integral operator

33 **Subscripts**

34 f circulation fluid

35 g grout

36 s soil

37 w groundwater

38 **Abbreviations**

39 ANOVA Analysis of Variance

- 40 BHE Borehole Heat Exchanger
- 41 DBHE Deep Borehole Heat Exchanger
- 42 DC-FEM Dual Continuum Finite Element Method
- 43 DCBHE Deep Coaxial Borehole Heat Exchanger
- 44 DOF Degrees of Freedom
- 45 DUBHE Deep U-type Borehole Heat Exchanger
- 46 FDM Finite Difference Method
- 47 GSHP Ground Source Heat Pump
- 48 S/N Signal to Noise
- 49 SS Sum of the Squares of the deviations
- 50 V Variance

51 1. Introduction

52 Energy production and supply are important factors restricting the de-
 53 velopment of society and are directly related to the lifeblood of countries
 54 worldwide [1]. In 2018, the Intergovernmental Panel on Climate Change
 55 of the United Nations (IPCC) has clearly stated that the global tempera-
 56 ture rise will be limited around 1.5 °C [2] by the end of the century in the
 57 climate change assessment report. In order to limit global warming and
 58 enhance the realization for green and sustainable development, countries all
 59 over the world are committed to the utilization of renewable energy for the
 60 low-carbon energy transition [3]. It is worth noting that building energy
 61 consumption accounts for the largest proportion of global energy consump-
 62 tion [4] and contributes to more than 40% [5] [6] of the total primary energy
 63 consumption in the European Union. Focusing on space heating in build-
 64 ing sector, the proportions reach 60%~80% [7] and 40% [8] of the energy
 65 consumption in Europe and China, respectively. Therefore, the renewable
 66 energy transition for building heating in order to reduce energy consumption
 67 has become a key part of achieving the carbon neutral goal [9].

68 The geothermal resource is a kind of clean, low-carbon, and renewable
 69 resource with huge reserve contained in the subsurface. It is widely used for
 70 versatile purposes, such as power generation, building heating, and agricul-
 71 ture [10]. Considering the heat exchange capacity of a single shallow BHE

72 in Ground Source Heat Pump (GSHP) systems, a concept of deep coaxial
73 borehole heat exchanger (DCBHE) was proposed by Rybach [11] to obtain
74 higher heat extraction capacity. For the DCBHE, an earliest field test was
75 reported in Hawaii [12], and later there were pilot applications in Aachen,
76 Germany [13] and Shaanxi Province, China [14]. There have been many
77 studies reported concerning DCBHE, including the field test [15] and nu-
78 merical analysis [16, 17, 18]. Both experimental data and simulated results
79 show that one single DCBHE with the depth of 2500 m can extract about
80 300 kW heat amount for building heating.

81 To get better heat extraction performance, a new type of deep U-type
82 borehole heat exchanger (DUBHE) has been proposed for building heating
83 in northern China recently [19, 20]. As for the DUBHE, it has a single-pipe
84 structure, which involves two vertical pipes with thousand-meter depth and
85 a horizontal section connecting vertical boreholes. The circulation fluid in
86 DUBHE flows through descending well, horizontal well and ascending well
87 successively, forming a closed-loop circulation to extract deep geothermal
88 energy. The schematic diagram of DUBHE can be seen in Fig. 1.

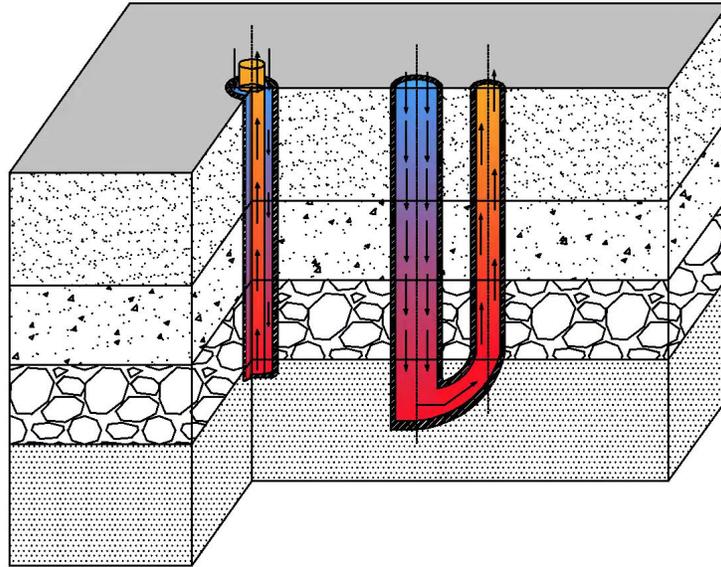


Figure 1: Schematic diagram of deep borehole heat exchanger: left, DCBHE; right, DUBHE

89 In scientific studies, numerical approach is usually chosen by researchers

90 to conduct related research for DUBHE because of the convenient on han-
91 dling the complex boundary conditions. For instance, FLUENT [21], Open-
92 GeoSys [22] software and Finite Difference Method (FDM) [23] have been
93 used for the heat extraction performance analysis and parameter optimiza-
94 tion of DUBHE. Several foreign researchers focus on the transformation of
95 abandoned oil Wells into BHE [24] [25]. In Hinton, a model of DUBHE
96 was established to investigate the feasibility of retrofitting an abandoned oil
97 well with DUBHE to extract geothermal energy in the Western Canadian
98 Sedimentary Basin near Hinton [26]. Gharibi et al. [27] proved that the
99 extracted geothermal energy from an abandoned oil well retrofitted with
100 a DUBHE can be used for direct applications in Iran, and even electric-
101 ity generation under the condition of 0.01m pipe diameter, 303.16K inlet
102 temperature and 0.5m/s inlet velocity (circulation fluid is water). Domes-
103 tic researchers mainly study and optimize the performance of DUBHE. For
104 instance, S. Tang [28] conducted detailed numerical investigations on the
105 performance of horizontal section of the DUBHE, and found that the heat
106 extraction rate can be optimal when the circulation flow rate is 33.85 t/h.
107 Wang [29] found that the inlet temperature for the DUBHE of 2000 m depth
108 increased by 10.46 °C when the geothermal gradient increased from 20 °C/km
109 to 30 °C/km. Li et al. [30] discussed the influence of design parameters, geo-
110 logical parameters and operation parameters on the heat extraction perfor-
111 mance of DUBHE. And the contribution degree of each influencing factor
112 to the system performance are quantified.

113 Based on the current research status, geological parameters and ground-
114 water seepage [31] have an obvious impact on the long-term heat extraction
115 performance of DUBHE. There will be a corresponding series of scientific
116 questions when systematically analyzing the influence of geological parame-
117 ters including groundwater seepage on the performance of DUBHE: 1) What
118 is the difference in heat extraction performance of DUBHE under differ-
119 ent geological conditions? 2) How to quantify the significance of influence
120 and contribution of factors on the heat extraction performance of DUBHE
121 during the long-term operation? 3) And where are the advantages of the
122 DUBHE system compared with the common heating system using fossil fu-
123 els in northern China? In order to solve above three scientific questions,
124 Taguchi method will be introduced in this study. Taguchi method was pro-
125 posed by Genichi Taguchi [32], which has the advantages of high efficiency
126 and economy in calculation. And this method is often used to quantify
127 and evaluate the affect of parameters on the system performance [33], espe-
128 cially in the field of geothermal energy utilization. The existing researches
129 mostly use Taguchi method to optimize the performance of GSHP system,

130 including single U-tube BHE [34], double U-tube BHE [35] and helical heat
131 exchanger [36]. Thus, the Taguchi method is selected to conduct the quan-
132 titative analysis for long-term performance of DUBHE.

133 Overall, this paper establishes DUBHE model by OpenGeoSys software
134 and conducts a series of long-term simulation of DUBHE. Then the Taguchi
135 method is used to answer the scientific questions. The related content is or-
136 ganized as follows: Section 2 introduces the governing equation for DUBHE
137 model in OpenGeoSys and describes the model verification results. Specific
138 details of DUBHE parameters and step size of model are given in section
139 3. Section 4 introduces the Taguchi method, and 18 sets of orthogonal test
140 conditions $L_{18}(3^5)$ are made based on five factors and corresponding three
141 levels. By adopting the signal-to-noise (S/N) ratio, matrix analysis and
142 analysis of variance (ANOVA), the significance and contribution ratio of
143 influencing factors for the long-term performance of DUBHE are evaluated
144 and quantified by analyzing three evaluation indexes T_{out} , Q_{total} , and D_{soil}
145 of the DUBHE system. And the corresponding results are shown in section
146 5. Case study including carbon emission reduction analysis of DUBHE and
147 future prospects are presented in section 6. This paper ends with a brief
148 summary and main conclusions in section 7.

149 2. Methodology

150 2.1. Governing equations

151 In this study, the OpenGeoSys software, which adopts the Dual-continuum
152 Finite Element Method (DC-FEM) [37, 22], is used for the simulation of
153 DUBHE. According to the DC-FEM method, the soil is discretized by 3D
154 elements in a prism form, while the borehole part (including both DUBHE
155 and surrounding grout) is simplified as one-dimensional line elements. The
156 coupling boundary between these two parts depends on the the Robin-type
157 boundary condition of heat flux [38]. By imposing the governing equations
158 on both the borehole part and soil part, the DC-FEM method can mimic the
159 dynamic heat transfer process among circulation fluid, borehole pipe, grout,
160 and surrounding soil. Compared with the conventional numerical simulator,
161 OpenGeoSys does not need to describe all the millimeter-level details within
162 and beside the borehole heat exchanger. Consequently, the calculation cost
163 will be considerably reduced and the long-term simulation for the DUBHE
164 will be of feasibility. Considering that the complete governing equations
165 have been introduced in the published study of DUBHE, we will not spend
166 too much space on the introduction in this part, interested readers can refer
167 to the literature [22].

168 *2.2. Model verification*

169 Based on OpenGeoSys software, there are a large number of model vali-
170 dation and verification cases reported in the previous publication conducted
171 by our research group. In the aspect of shallow BHE, the BHE array model
172 implemented by OpenGeoSys software has been verified against analytical
173 solutions [39, 40] and validated with actual monitoring data from the Leices-
174 ter’s GSHP project [41]. As for the DBHE, the DCBHE and DUBHE model
175 established by OpenGeoSys software have previously been verified against
176 Beier’s analytical solution [18, 42] and Ramey’s analytical solution [22], re-
177 spectively. Moreover, the simulated results of DCBHE have been validated
178 by monitoring data from a pilot project in Xi’an [43]. Based on the sufficient
179 monitoring data and analytical solutions, we believe that the previous work
180 concerning verification of the BHE/DBHE models ensures the capability
181 of OpenGeoSys software to simulate the long-term performance of DBHE
182 within an acceptable calculation cost. Therefore, the OpenGeoSys software
183 is chosen to calculate the heat extraction capacity of DUBHE under different
184 geological parameters during long-term operation.

185 **3. Model description**

186 *3.1. Model setup*

187 In this study, the ascending and descending wells are perpendicular to
188 the horizontal borehole and connected by the horizontal borehole at the
189 bottom. According to a pilot project of DUBHE in northern China [20],
190 the length of the descending and ascending wells are set as 2500 m, and the
191 horizontal distance between them is 600 m. In order to avoid the thermal
192 plume touching the lateral boundary during long-term operation, the size of
193 the entire domain is set as $800 \times 200 \times 2700$ m. The entire model domain
194 can be seen in Fig. 2 and the detailed parameters of the DUBHE are listed in
195 Table 1. The soil properties are kept to be isotropic over the entire domain.

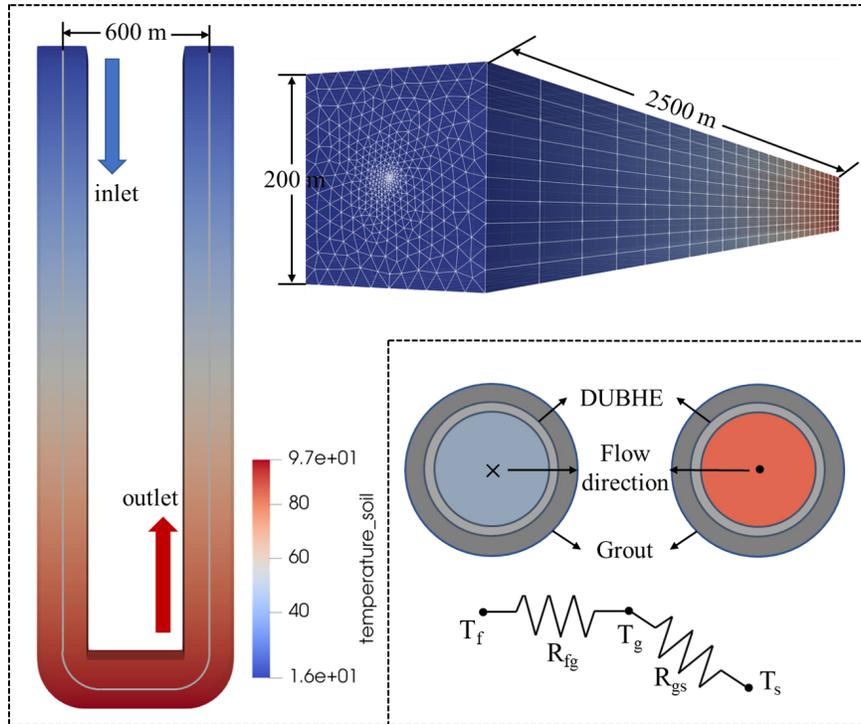


Figure 2: DUBHE 3D model domain in OpenGeoSys

Table 1: Detailed parameters of the DUBHE in numerical models

| Item | Parameter | Value | Unit |
|-------------------|-----------------------------------|----------|----------------------------------|
| Borehole | Borehole depth | 2500 | m |
| | Borehole diameter | 0.2445 | m |
| | Borehole spacing | 600 | m |
| | Outer diameter of tube | 0.1594 | m |
| | Wall thickness of tube | 0.00919 | m |
| | Thermal conductivity of tube wall | 40 | $\text{W m}^{-1} \text{K}^{-1}$ |
| Grout | Density | 2190 | kg m^{-3} |
| | Specific heat capacity | 1735.16 | $\text{J kg}^{-1} \text{K}^{-1}$ |
| | Thermal conductivity | 1.2 | $\text{W m}^{-1} \text{K}^{-1}$ |
| Circulation fluid | Thermal conductivity | 0.6 | $\text{W m}^{-1} \text{K}^{-1}$ |
| | Specific heat capacity | 4190 | $\text{J kg}^{-1} \text{K}^{-1}$ |
| | Density | 998 | kg m^{-3} |
| | Dynamic viscosity | 0.000931 | $\text{kg m}^{-1} \text{s}^{-1}$ |
| | flow rate | 0.01389 | $\text{m}^3 \text{s}^{-1}$ |

196 The previous study have shown that the fluctuation in surface temper-
197 ature have little effect on the overall heat extraction of DBHE [18], so the
198 top boundary of the soil domain is set to a Dirichlet-type boundary with
199 constant surface temperature of 15.6°C [44]. The lateral side of domain is
200 adiabatic boundary, which is set as no-heat-flux condition in OpenGeoSys
201 software. And the Neumann-type boundary with 60 mW/m^2 is set for the
202 bottom of the domain to simulate the actual geothermal heat flux [43].

203 3.2. Grid independence test

204 For numerical simulation, grid independence test is needed to save cal-
205 culation time, while the accuracy of simulated results can be guaranteed.
206 According to the red points in Fig. 3, it can be seen that the step selected
207 in the axial direction are 100 m of a layer, and the change of axial step size
208 has little effect on the simulated outlet temperature of DUBHE. Considering
209 the actual borehole diameter, the mesh size in the area near the DUBHE
210 is 0.75m. The mesh size in the peripheral area is gradually sparse, and the
211 radial step at the edge of DUBHE model is 20 m. After the axial and radial
212 step size is determined, the number of nodes of the 3D numerical model in
213 this paper is 37370. In order to ensure generate stable numerical results, the
214 time step of the heating season gradually increased from 1 h (initial) to 12 h
215 (one month later) according to the previous study [43]. And the time cost

216 of running a heating season under constant inflow temperature boundary
 217 condition is 14 min by using HP Z6 G4 Workstation.

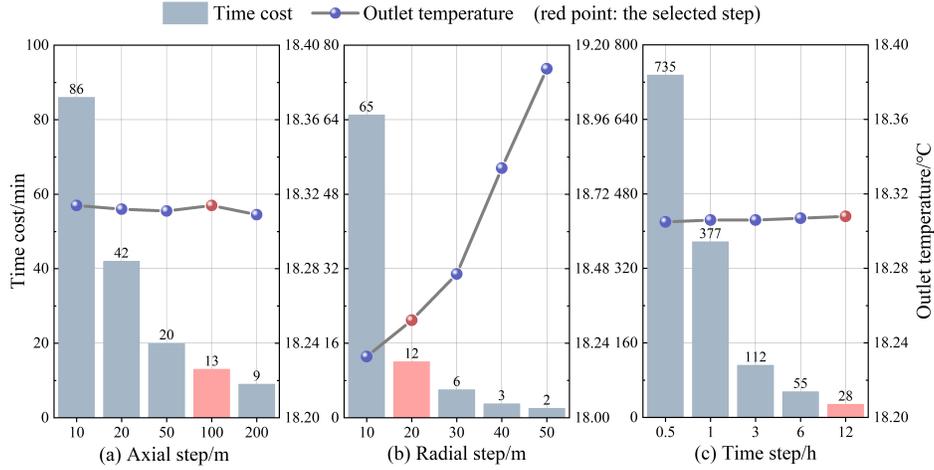


Figure 3: Outlet temperature of DUBHE and simulated time cost under different radial, axial density and time steps (after one heating season)

218 4. Orthogonal test design

219 4.1. Taguchi method

220 The analysis of influencing factors under multiple levels often faces the
 221 problem of redundant experiment conditions. At this time, it is necessary
 222 to select representative combinations for tests under various experimental
 223 conditions to reduce the calculation time. Taguchi method is widely used in
 224 engineering research because of its advantages of the balanced and dispersed
 225 test, simple data calculation and so on [45]. Based on the Taguchi method,
 226 this paper analyzes and evaluates the influence of geological parameters on
 227 the long-term performance of DUBHE, and the process is listed as follows:

228 ★Preparatory work

229 1) Determine the geological influencing factors and the corresponding
 230 level;

231 2) Make the corresponding orthogonal experiment table;

232 3) Execute the simulation of various scenarios;

233 ★Post processing and analysis

234 4) Select evaluation indexes;

- 235 5) Use S/N ratio to determine the significance of influencing factors;
 236 6) Make average S/N ratio tables and draw related figures;
 237 7) Use ANOVA method to determine the contribution of factors;
 238 8) Make contribution rate tables and draw related figures.

239 Table 2 shows detailed information about the five geological parameters,
 240 including level parameters and thermal reservoir information. The related
 241 references are also cited in the specific position in Table 2.

Table 2: Influencing factors and their levels

| | Factors | Unit | Levels | | | |
|---|---------------------------------|---------------------------------|--------------------|--------------------|--------------------|--------------------|
| | | | 1 | 2 | 3 | |
| A | Thermal conductivity [46] | $\text{W m}^{-1} \text{K}^{-1}$ | 0-500m | 1.2 | 1.6 | 1.8 |
| | | | 500-1300m | 1.5 | 1.8 | 2.2 |
| | | | 1300-2000m | 1.8 | 2.0 | 3.0 |
| | | | >2000m | 2.0 | 2.5 | 4.0 |
| B | Geothermal gradient [47] | $^{\circ}\text{C km}^{-1}$ | 20 | 30 | 40 | |
| C | Specific heat capacity [48] | $\text{J m}^{-3} \text{K}^{-1}$ | 0-500m | 2.28×10^6 | 2.52×10^6 | 4.20×10^6 |
| | | | 500-1300m | 2.00×10^6 | 2.32×10^6 | 4.00×10^6 |
| | | | 1300-2000m | 1.72×10^6 | 1.97×10^6 | 3.60×10^6 |
| | | | >2000m | 1.70×10^6 | 1.96×10^6 | 3.56×10^6 |
| D | Groundwater flow direction [49] | | Counter | Parallel | Vertical | |
| E | Darcy velocity [50] | m s^{-1} | 2×10^{-9} | 2×10^{-8} | 2×10^{-7} | |

242 4.2. Objective functions

243 In this paper, three indexes, including T_{out} , Q_{total} , and D_{soil} are intro-
 244 duced to evaluate and quantify the heat extraction of DUBHE under dif-
 245 ferent geological parameters both on short-term performance and long-term
 246 sustainability. The T_{out} index is defined as the average outlet temperature
 247 of DUBHE during the first heating season when the inlet temperature is
 248 4°C considering that the temperature threshold of the heat pump unit [51].
 249 The Q_{total} index is determined by the maximum cumulative heat extraction
 250 amount of DUBHE during long-term operation, and its calculation reads,

$$Q_{\text{total}} = NQ_{\text{average}} \quad (1)$$

251 Where, Q_{average} is the maximum heat extraction amount when the inlet
 252 temperature of DUBHE approaches 0°C in the last heating season after
 253 long-term operation. N is operation years, and the value of N is 20 in this
 254 study.

255 The D_{soil} refers to the soil temperature decay rate compared with the
 256 initial temperature at the position 5 m away from the descending boreholes
 257 of DUBHE and 1250 m away from the surface. The concept of D_{soil} is defined
 258 as follows.

$$D_{soil} = \frac{T_{initial} - T_{soil}}{T_{initial}} \times 100\% \quad (2)$$

259 *4.3. Post-processing method: signal-to-noise (S/N) ratio*

260 In the post-processing of Taguchi method, ‘the larger the better’ [52] and
 261 ‘the smaller the better’ [53] are the most common functions. The former
 262 mode means that with a larger result of the objective function, the impact
 263 of factor is more significant, and so does the latter mode. Obviously, for
 264 the first two indicators, the larger the result, the better the influence of
 265 parameters [30]. For the D_{soil} , that is ‘the smaller the better’ objective
 266 function [54].

267 The relevant calculation formula is listed as follows:

268 The larger the better:

$$\frac{S}{N} = -10 \lg \left(\frac{1}{i} \sum \frac{1}{y^2} \right) \quad (3)$$

269 The smaller the better:

$$\frac{S}{N} = -10 \lg \left(\frac{1}{i} \sum y^2 \right) \quad (4)$$

270 Where, i is the number of sample iterations, y is the simulated result for
 271 each scenario.

272 *4.4. Post-processing method: analysis of variance (ANOVA)*

273 ANOVA is a statistical model used to further evaluate the relative signif-
 274 icance, the contribution of each factor, and error to the objective function.
 275 The essence of the ANOVA method is to analyze the significance of influ-
 276 ence by constructing a statistical function F and using F_{test} under certain
 277 reliability levels [55]. The larger the F value is, the greater the contribution
 278 is. The calculation within ANOVA is presented as follows.

$$DOF = m - 1 \quad (5)$$

279 Where, DOF is the degree of freedom and m is the number of factor
 280 levels.

$$SS = \frac{1}{r} \sum_{i=1}^m K_{ij}^2 - \frac{(\sum_{i=1}^n y)^2}{n} \quad (6)$$

281 Where, SS is the sum of the squares of the deviations, K_{ij} is the sum of
 282 all the calculated results when the factor is i, y is the simulated result for
 283 each scenario.

$$r = \frac{n}{m} \quad (7)$$

284 Where, r is the repeated number of each level and n is the total number
 285 of experiments.

$$V = \frac{SS}{DOF} \quad (8)$$

286 Where, V is the variance.

287 Finally, the expression of a statistical function is constructed as follows:

$$F_{factor} = \frac{V_{factor}}{V_{error}} \quad (9)$$

288 5. Results

289 In this section, the long-term heat extraction performance of DUBHE
 290 under different geological parameters are investigated based on the orthog-
 291 onal test. Table 3 shows the values and S/N ratios of T_{out} , Q_{total} , and D_{soil}
 292 of 18 orthogonal scenarios.

Table 3: T_{out} , Q_{total} and D_{soil} for DUBHE and the corresponding S/N ratios

| Scenarios | Parameters | | | | | Results | | | S/N | | |
|-----------|------------|---|---|---|---|------------------------------------|-------------------------------|-----------------------|------------------|--------------------|-------------------|
| | A | B | C | D | E | $T_{\text{out}}(^{\circ}\text{C})$ | $Q_{\text{total}}(\text{TJ})$ | $D_{\text{soil}}(\%)$ | T_{out} | Q_{total} | D_{soil} |
| 1 | 1 | 1 | 1 | 1 | 1 | 27.10 | 111.97 | 14.34 | 28.66 | 40.98 | 16.87 |
| 2 | 1 | 1 | 2 | 2 | 3 | 27.01 | 114.05 | 13.68 | 28.63 | 41.14 | 17.28 |
| 3 | 1 | 2 | 1 | 3 | 3 | 28.99 | 152.41 | 14.20 | 29.24 | 43.66 | 16.95 |
| 4 | 1 | 2 | 3 | 1 | 2 | 28.56 | 159.67 | 11.78 | 29.12 | 44.06 | 18.58 |
| 5 | 1 | 3 | 2 | 3 | 2 | 30.71 | 188.70 | 13.75 | 29.75 | 45.52 | 17.23 |
| 6 | 1 | 3 | 3 | 2 | 1 | 30.50 | 196.99 | 11.63 | 29.69 | 45.89 | 18.69 |
| 7 | 2 | 1 | 1 | 3 | 2 | 27.69 | 127.53 | 14.82 | 28.85 | 42.11 | 16.58 |
| 8 | 2 | 1 | 3 | 1 | 3 | 27.22 | 134.78 | 11.87 | 28.70 | 42.59 | 18.51 |
| 9 | 2 | 2 | 2 | 2 | 2 | 29.63 | 172.11 | 14.24 | 29.43 | 44.72 | 16.93 |
| 10 | 2 | 2 | 3 | 3 | 1 | 29.35 | 180.40 | 12.05 | 29.35 | 45.12 | 18.38 |
| 11 | 2 | 3 | 1 | 2 | 3 | 31.74 | 213.58 | 14.87 | 30.03 | 46.59 | 16.55 |
| 12 | 2 | 3 | 2 | 1 | 1 | 31.67 | 214.62 | 14.25 | 30.01 | 46.63 | 16.92 |
| 13 | 3 | 1 | 2 | 3 | 1 | 28.96 | 165.89 | 14.83 | 29.24 | 44.40 | 16.58 |
| 14 | 3 | 1 | 3 | 2 | 2 | 28.61 | 169.00 | 12.15 | 29.13 | 44.56 | 18.31 |
| 15 | 3 | 2 | 1 | 2 | 1 | 31.58 | 214.62 | 15.15 | 29.99 | 46.63 | 16.39 |
| 16 | 3 | 2 | 2 | 1 | 3 | 31.52 | 217.73 | 14.46 | 29.97 | 46.76 | 16.80 |
| 17 | 3 | 3 | 1 | 1 | 2 | 34.11 | 269.57 | 15.23 | 30.66 | 48.61 | 16.35 |
| 18 | 3 | 3 | 3 | 3 | 3 | 33.94 | 290.30 | 12.34 | 30.61 | 49.26 | 18.17 |

293 *5.1. Analysis of S/N ratio*

294 Table 4, Table 5, and Table 6 show corresponding average S/N ratios of
 295 five geological parameters at three levels respectively. And the relevant data
 296 are shown in Fig. 4, Fig. 5 and Fig. 6.

297 According to Fig. 4, the significance of influence for T_{out} is in the or-
 298 der of B, A, C, E, and D (geothermal gradient, thermal conductivity, spe-
 299 cific heat capacity, Darcy velocity, and groundwater flow direction). And
 300 the levels and S/N ratios for the factor giving the best T_{out} are specified
 301 as B_3 (S/N=30.13), A_3 (S/N=29.95), C_1 (S/N=29.60), E_3 (S/N=29.56) and
 302 D_1 (S/N=29.55) respectively. For T_{out} index, the optimized combination is
 303 $A_3B_3C_1D_1E_3$.

304 Taking Q_{total} as the objective function, the significance of influence is in
 305 the order of B, A, C, E, and D (geothermal gradient, thermal conductivity,
 306 specific heat capacity, Darcy velocity, and groundwater flow direction). Ac-
 307 cording to Fig. 5, the optimal parameters of five factors at three levels can

308 be obtained, which are B_3 (S/N=47.20), A_3 (S/N=46.90), C_3 (S/N=45.51),
309 E_3 (S/N=45.44), and D_1 (S/N=45.33) respectively. And the corresponding
310 optimized combination is $A_3B_3C_3D_1E_3$.

311 As for the D_{soil} index, the significance of influence is in the order of
312 C, A, E, B, and D (specific heat capacity, thermal conductivity, Darcy ve-
313 locity, geothermal gradient, and groundwater flow direction). According to
314 the Fig. 6, the optimal parameters of five factors at three levels can also
315 be obtained, which are C_3 (S/N=18.44), A_1 (S/N=17.57), E_3 (S/N=17.35),
316 B_1 (S/N=17.32), and D_2 (S/N=17.32) respectively. And the corresponding
317 optimized combination is $A_1B_1C_3D_2E_3$.

318 According to Fig. 4 and Fig. 5, average S/N ratios of T_{out} and Q_{total}
319 will have an increment with the increase of thermal conductivity. Thermal
320 conductivity is used to measure the heat conduct ability. The higher the
321 thermal conductivity is, the faster the heat transfer rate will be. The specific
322 data show that, when the thermal conductivity is the level-1, the average
323 T_{out} of DUBHE is 28.81 °C (S/N=29.19), and the average Q_{total} of DUBHE
324 is 153.96 TJ (S/N=43.75). When the thermal conductivity is at the level-
325 3, the above two indicators increase to 31.45 °C(S/N=29.95) and 221.18 TJ
326 (S/N=46.90). The soil temperature decay rate decreases with the increase of
327 thermal conductivity, which can be interpreted as the stronger heat recovery
328 of the surrounding subsurface.

329 The larger the geothermal gradient, the higher the bottom temperature
330 of the soil. Therefore, the average T_{out} and the average Q_{total} of DUBHE
331 will increase with the increase of geothermal gradient. For example, when
332 the geothermal gradient increases from 20°C km⁻¹ to 40°C km⁻¹, T_{out}
333 of DUBHE increases from 27.77 to 32.11 °C, which the increasing rate is
334 15.66% compared with level-1. And the average Q_{total} of DUBHE varies
335 from 137.20 TJ(S/N=42.75) to 228.96 TJ(S/N=47.20) when the geothermal
336 gradient increases from 20°C km⁻¹ to 40°C km⁻¹. The soil temperature
337 decay rate is less affected by geothermal gradient, and the average value of
338 D_{soil} for the three levels is about 13.6%.

339 Thermal diffusivity is defined as the ratio of thermal conductivity to
340 specific heat capacity, which is used to measure the ability of an object to
341 achieve uniform temperature in the heat transfer process. With the same
342 thermal conductivity, the thermal diffusivity of soil gradually decreases with
343 the increase of specific heat capacity, which is not conducive to heat trans-
344 fer. Thus, the outlet water temperature of DUBHE will decrease with the
345 increase of specific heat capacity and the corresponding soil temperature de-
346 cay rate will increase. In addition, specific heat capacity has little influence
347 for Q_{total} index, and the increasing rate of the average S/N ratio in level-3

348 only has a 0.73% difference compared with level-1.

349 Groundwater seepage strengthens the convection heat transfer outside
350 the borehole and reduces the thermal resistance of soil, which is conducive
351 to heat extraction of DUBHE. The average S/N ratio of T_{out} and Q_{total}
352 under the parallel direction (from the descending well to the ascending well)
353 are 29.85 °C(S/N=29.50) and 180.06 TJ(S/N=45.11), which are lower than
354 the other seepage directions. Moreover, the average S/N ratio of D_{soil} un-
355 der the parallel direction is 13.6% (S/N= 17.32), which is the worst among
356 all the three seepage directions. It means that the enhancement effect of
357 heat extraction performance with the parallel direction of seepage is the
358 weakest. Owing to the existence of groundwater seepage, the heat stored in
359 the remote soil will be transported to the surrounding area of the horizon-
360 tal borehole of DUBHE. Therefore, the vertical seepage direction will have a
361 higher heat supply from the remote subsurface and has the best heat extrac-
362 tion enhancement, which is better than the parallel and counter directions.
363 As for the Darcy velocity, the S/N ratios of T_{out} , Q_{total} , and D_{soil} have an
364 increment with the increase of Darcy velocity. When the Darcy velocity is
365 2×10^{-9} m/s, the average S/N ratios of the three indicators are 29.50, 45.14,
366 and 17.26 respectively. Then the Darcy velocity improves to 2×10^{-7} m/s,
367 the increasing rates of average S/N ratio are just 0.20%, 0.66%, and 0.51%
368 respectively. It is worth noting that Darcy velocity can indeed enhance
369 the heat extraction performance of DUBHE, but the benefit is not obvious
370 within the typical range of groundwater seepage velocity in northern China.
371 The results show that both the groundwater flow direction and Darcy ve-
372 locity will not bring considerable enhancement to the heat extraction per-
373 formance of DUBHE, which indicates that the heat convection phenomenon
374 is not the dominant process surrounding the horizontal borehole.

Table 4: Average S/N ratios response of T_{out} under five factors and different levels

| Scenarios | Parameters | | | | | S/N ratio for T_{out} (dB) | | | | |
|-----------|--------------|--------------|--------------|--------------|--------------|------------------------------|--------------|--------------|--------------|--------------|
| | A | B | C | D | E | A | B | C | D | E |
| 1 | 28.81 | 27.77 | 30.20 | 30.03 | 29.86 | 29.19 | 28.87 | 29.60 | 29.55 | 29.50 |
| 2 | 29.55 | 29.94 | 29.92 | 29.85 | 29.89 | 29.41 | 29.52 | 29.52 | 29.50 | 29.51 |
| 3 | 31.45 | 32.11 | 29.70 | 29.94 | 30.07 | 29.95 | 30.13 | 29.45 | 29.53 | 29.56 |
| Delta | 2.64 | 4.35 | 0.51 | 0.19 | 0.21 | 0.76 | 1.26 | 0.15 | 0.05 | 0.06 |
| Rank | 2 | 1 | 3 | 5 | 4 | 2 | 1 | 3 | 5 | 4 |

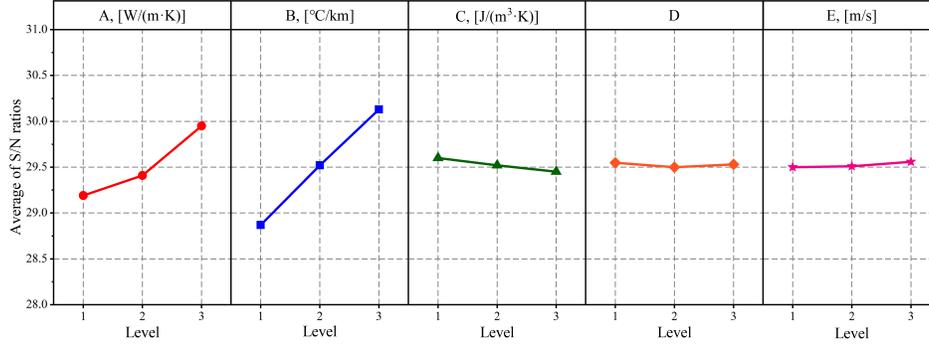


Figure 4: Effect of process parameters on average S/N ratio for T_{out}

Table 5: Average S/N ratios response of Q_{total} under five factors and different levels

| Scenarios | Parameters | | | | | S/N ratio for Q_{total} (dB) | | | | |
|-----------|---------------|---------------|---------------|---------------|---------------|--------------------------------|--------------|--------------|--------------|--------------|
| | A | B | C | D | E | A | B | C | D | E |
| 1 | 153.96 | 137.20 | 181.61 | 184.72 | 180.75 | 43.75 | 42.75 | 45.18 | 45.33 | 45.14 |
| 2 | 173.84 | 182.82 | 178.85 | 180.06 | 181.09 | 44.80 | 45.24 | 45.05 | 45.11 | 45.16 |
| 3 | 221.18 | 228.96 | 188.52 | 184.21 | 187.14 | 46.90 | 47.20 | 45.51 | 45.31 | 45.44 |
| Delta | 67.22 | 91.76 | 9.68 | 4.67 | 6.39 | 3.15 | 4.45 | 0.46 | 0.22 | 0.30 |
| Rank | 2 | 1 | 3 | 5 | 4 | 2 | 1 | 3 | 5 | 4 |

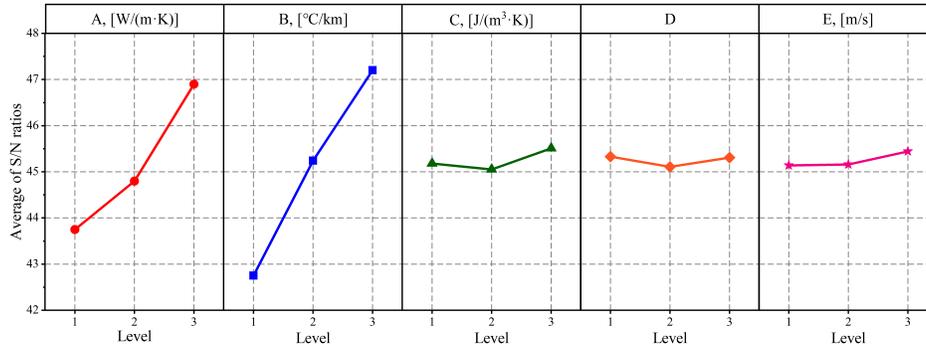


Figure 5: Effect of process parameters on average S/N ratio for Q_{total}

Table 6: Average S/N ratios response of D_{soil} under five factors and different levels

| Scenarios | Parameters | | | | | S/N ratio for D_{soil} (dB) | | | | |
|-----------|--------------|--------------|--------------|--------------|--------------|--------------------------------------|--------------|--------------|--------------|--------------|
| | A | B | C | D | E | A | B | C | D | E |
| 1 | 0.132 | 0.136 | 0.148 | 0.137 | 0.137 | 17.57 | 17.32 | 16.61 | 17.29 | 17.26 |
| 2 | 0.137 | 0.136 | 0.142 | 0.136 | 0.137 | 17.28 | 17.30 | 16.95 | 17.32 | 17.29 |
| 3 | 0.140 | 0.137 | 0.120 | 0.137 | 0.136 | 17.06 | 17.28 | 18.44 | 17.29 | 17.35 |
| Delta | 0.008 | 0.001 | 0.028 | 0.001 | 0.001 | 0.51 | 0.04 | 1.83 | 0.03 | 0.09 |
| Rank | 2 | 4 | 1 | 5 | 3 | 2 | 4 | 1 | 5 | 3 |

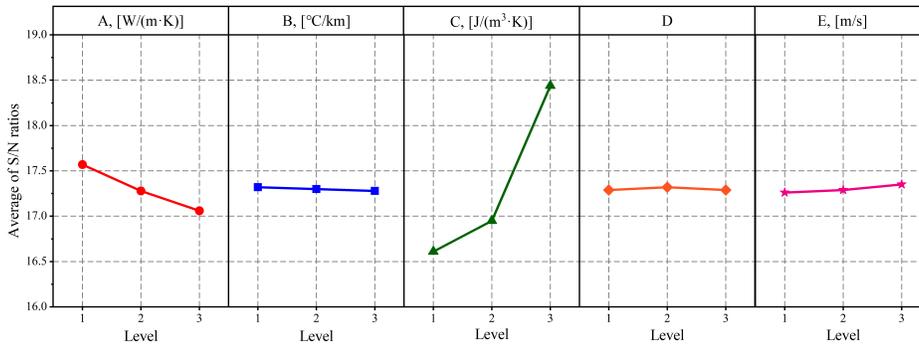


Figure 6: Effect of process parameters on average S/N ratio for D_{soil}

375 5.2. Analysis of ANOVA method

376 In the previous section, the S/N ratio is used to evaluate the influence
377 significance of each factor, and the corresponding optimization combinations
378 for three indexes are obtained. ANOVA method will be used to quantify the
379 contribution of each factor on the objective function. If F_{factor} is greater
380 than $F_{0.05}$ (95% confidence level), the change of the level of factors has a
381 significant influence on the experimental results, then will be marked as *
382 in our paper.

383 The contribution degree of five factors and corresponding experimental
384 errors to the three indexes are drawn as a bar chart Fig. 7. It can be clearly
385 seen that B and A (geothermal gradient and thermal conductivity) have
386 significant influence on the objective function of T_{out} , and their contributions
387 are as high as 70.14% and 27.59%. Moreover, it can be shown that C (specific
388 heat capacity) has a certain influence for T_{out} of DUBHE. Compared with
389 the first two parameters, the influence degree of C has little influence, and
390 its contribution degree only accounts for 0.95%. In addition, groundwater
391 flow direction and Darcy velocity have less influence on T_{out} than the first
392 three.

393 For Q_{total} , the contribution rate of B (geothermal gradient) is the largest,
394 which is 62.10%. Secondly, the influence of A (thermal conductivity) is also
395 obvious for Q_{total} , which has a contribution of 35.18%. This provides a
396 direction for the promotion of deep borehole geothermal heating technology.
397 It is suitable for the promotion of geothermal technology in the abundant
398 geothermal resources, which owns high geothermal gradient and thermal
399 conductivity.

400 The geological parameters that affect the D_{soil} are C and A (specific heat
401 capacity and thermal conductivity), which contribute 92.41% and 6.74% re-
402 spectively. It shows that the thermal diffusivity will directly affect the tem-
403 perature decay rate and temperature recovery of subsurface. The influence
404 of the other three parameters B, D, and E (geothermal gradient, ground-
405 water flow direction, and Darcy velocity) on D_{soil} are less than that of the
406 first two. In scientific research and engineering application, thermal inter-
407 action within the borehole array caused by thermal diffusion should be fully
408 considered for system design in order to give reasonable borehole spacing.

Table 7: Results of ANOVA for DUBHE

| Variance source | Degree of freedom (DOF) | Sum of squares (SS) | Mean square (MS) | F ratio | $F_{0.05}$ | Contribution rate (%) |
|--------------------------|-------------------------|---------------------|------------------|---------|------------|-----------------------|
| T_{out} | | | | | | |
| A | 2 | 22.29 | 11.15 | 97.14 | 4.74 | 27.59* |
| B | 2 | 56.68 | 28.34 | 246.99 | 4.74 | 70.14* |
| C | 2 | 0.77 | 0.38 | 3.35 | 4.74 | 0.95 |
| D | 2 | 0.10 | 0.05 | 0.45 | 4.74 | 0.13 |
| E | 2 | 0.16 | 0.08 | 0.69 | 4.74 | 0.20 |
| Error | 7 | 0.80 | 0.11 | | | 0.99 |
| Total | 17 | 80.81 | | | | 100 |
| Q_{total} | | | | | | |
| A | 2 | 14310.15 | 7155.07 | 87.50 | 4.74 | 35.18* |
| B | 2 | 25258.20 | 12629.10 | 154.44 | 4.74 | 62.10* |
| C | 2 | 298.12 | 149.06 | 1.82 | 4.74 | 0.74 |
| D | 2 | 78.47 | 39.24 | 0.48 | 4.74 | 0.19 |
| E | 2 | 155.15 | 77.58 | 0.95 | 4.74 | 0.38 |
| Error | 7 | 572.41 | 81.77 | | | 1.41 |
| Total | 17 | 40672.51 | | | | 100 |
| D_{soil} | | | | | | |
| A | 2 | 0.192‰ | 0.096‰ | 41.18 | 4.74 | 6.74* |
| B | 2 | 0.001‰ | 0.001‰ | 0.26 | 4.74 | 0.04 |
| C | 2 | 2.626‰ | 1.313‰ | 564.41 | 4.74 | 92.41* |
| D | 2 | 0.001‰ | 0.0003‰ | 0.14 | 4.74 | 0.02 |
| E | 2 | 0.006‰ | 0.003‰ | 1.28 | 4.74 | 0.21 |
| Error | 7 | 0.016‰ | 0.002‰ | | | 0.58 |
| Total | 17 | 2.842‰ | | | | 100 |

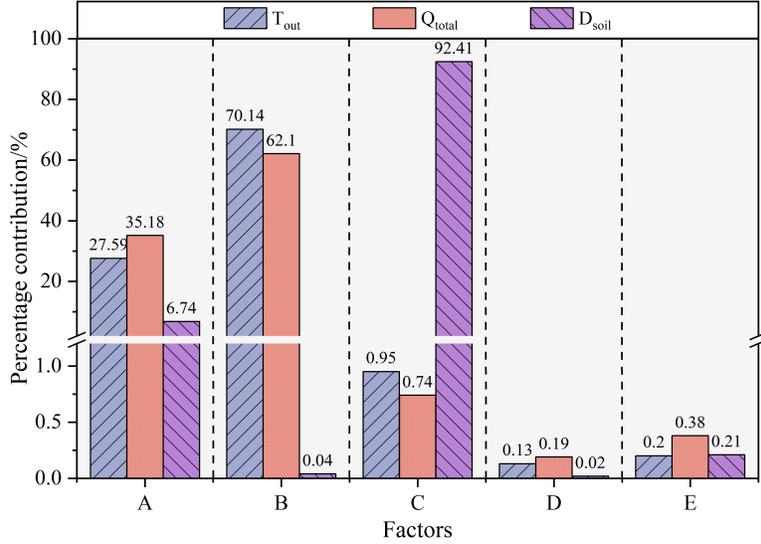


Figure 7: Contribution rates of various factors to evaluation parameters for heat exchange performance

409 5.3. Analysis of matrix method

410 Section 5.1 analyzes the proposed three objective function, the optimal
 411 combination for T_{out} indicator is $A_3B_3C_1D_1E_3$, and the optimal combina-
 412 tion is $A_3B_3C_3D_1E_3$ in view of Q_{total} , the optimal combination for D_{soil} is
 413 $A_1B_1C_3D_2E_3$. The previous analysis does not answer the question about
 414 what is the comprehensive optimal combination in view of the three indica-
 415 tors. Thus, this section uses the matrix-analytic method [56] to determine
 416 the comprehensive optimization combination.

417 The matrix-analytic method decomposes the weight matrix into three-
 418 layer structure models and matrix [57]. The weight matrix of indexes is
 419 obtained by multiplying each layer matrix, and the level weight of factors is
 420 calculated, so as to determine the optimal combination under comprehensive
 421 indexes. The specific expression is as follows:

$$W = MTS \quad (10)$$

422 Where, W is the weight matrix, M is the tested index layer matrix, T is
 423 the factor layer matrix and S is the level matrix.

The calculated result of the weight matrix is presented in this section.
 Also, the detailed calculation process and results of the weight matrix are

shown in section 8 for interested readers.

$$W = \frac{(W_1 + W_2 + W_3)}{3} = \frac{1}{3} \left(\begin{array}{c} 0.1062 \\ 0.1089 \\ 0.1159 \\ 0.1683 \\ 0.1815 \\ 0.1946 \\ 0.0213 \\ 0.0211 \\ 0.0209 \\ 0.0076 \\ 0.0076 \\ 0.0076 \\ 0.0089 \\ 0.0089 \\ 0.0089 \end{array} + \begin{array}{c} 0.1036 \\ 0.1170 \\ 0.1489 \\ 0.1262 \\ 0.1682 \\ 0.2106 \\ 0.0177 \\ 0.0174 \\ 0.0183 \\ 0.0086 \\ 0.0084 \\ 0.0086 \\ 0.0117 \\ 0.0117 \\ 0.0121 \end{array} + \begin{array}{c} 0.0704 \\ 0.0681 \\ 0.0664 \\ 0.0053 \\ 0.0053 \\ 0.0053 \\ 0.2218 \\ 0.2306 \\ 0.2735 \\ 0.0040 \\ 0.0040 \\ 0.0040 \\ 0.0118 \\ 0.0119 \\ 0.0119 \end{array} \right) = \begin{array}{c} 0.0934 \\ 0.0980 \\ \mathbf{0.1104} \\ 0.0999 \\ 0.1183 \\ \mathbf{0.1368} \\ 0.0869 \\ 0.0897 \\ \mathbf{0.1043} \\ 0.0067 \\ 0.0066 \\ \mathbf{0.0067} \\ 0.0108 \\ 0.0108 \\ \mathbf{0.0110} \end{array} = \begin{array}{c} A_1 \\ A_2 \\ A_3 \\ B_1 \\ B_2 \\ B_3 \\ C_1 \\ C_2 \\ C_3 \\ D_1 \\ D_2 \\ D_3 \\ E_1 \\ E_2 \\ E_3 \end{array}$$

424 Assuming that the weight of T_{out} , Q_{total} and D_{soil} are 1/3 respectively,
 425 the final optimized combination is $A_3B_3C_3D_3E_3$ by integrating the three
 426 evaluation indexes.

427 6. Discussion

428 6.1. Case study of carbon emission reduction

429 According to the previous results, we can find that thermal conductivity,
 430 geothermal gradient, and specific heat capacity are three dominant geolog-
 431 ical factors that affect the long-term performance of DUBHE. In order to
 432 intuitively discuss the potential of carbon emission reduction of DUBHE
 433 compared with traditional heating forms, this section sets three scenarios
 434 based on the actual geological characteristics. The geothermal gradient of
 435 the three scenarios increases gradually, and the detailed features are shown
 436 in Table 8.

Table 8: List of three simulated scenarios and features

| Scenario | Geological formation | Depth | Thermal conductivity | Geothermal gradient | Specific heat capacity |
|----------|----------------------|-----------|---------------------------------|----------------------------|---------------------------------|
| | | m | $\text{W m}^{-1} \text{K}^{-1}$ | $^{\circ}\text{C km}^{-1}$ | $\text{J m}^{-3} \text{K}^{-1}$ |
| A [58] | Formation 1 | 0-636 | 1.8 | 28.5 | 2.45×10^6 |
| | Formation 2 | 636-1198 | 2.6 | | 2.94×10^6 |
| | Formation 3 | 1198-1910 | 3.5 | | 1.96×10^6 |
| | Formation 4 | 1910-2500 | 5.3 | | 2.28×10^6 |
| B [59] | Formation 1 | 0-418 | 1.042 | 30 | 3.73×10^6 |
| | Formation 2 | 418-1030 | 2.7 | | 2.31×10^6 |
| | Formation 3 | 1030-1530 | 2.58 | | 2.35×10^6 |
| | Formation 4 | 1530-2295 | 2.53 | | 2.31×10^6 |
| | Formation 5 | 2295-2500 | 2.31 | | 2.23×10^6 |
| C [60] | Formation 1 | 0-420 | 0.921 | 33.5 | 1.29×10^6 |
| | Formation 2 | 420-1000 | 1.8 | | 2.45×10^6 |
| | Formation 3 | 1000-1580 | 2.6 | | 2.94×10^6 |
| | Formation 4 | 1580-2000 | 3.5 | | 1.96×10^6 |
| | Formation 5 | 2000-2500 | 5.3 | | 2.28×10^6 |

437 According to Fig. 8, the outlet water temperature and heat extraction
 438 of DUBHE in the three scenarios gradually decrease when the boundary
 439 condition is set as the constant inflow temperature type. They go through
 440 a stage of descending, a period of transition, and a stable stage. The outlet
 441 water temperature at the end of one heating season is arranged in order of
 442 size as 26.51, 24.26, and 19.92 $^{\circ}\text{C}$, corresponding to Scenario_C, Scenario_A,
 443 and Scenario_B. It is worth noting that although the geothermal gradient
 444 of Scenario_B is slightly larger than that of Scenario_A, the outlet water
 445 temperature of Scenario_B is lower than that of Scenario_A. The main rea-
 446 son for this phenomenon is that thermal conductivity occupies an obvious
 447 advantage. According to the Q_{total} index mentioned above, the simulation
 448 results of three scenarios are 274.34 (Scenario_C), 247.80 (Scenario_A) and
 449 191.39 TJ (Scenario_B) respectively.

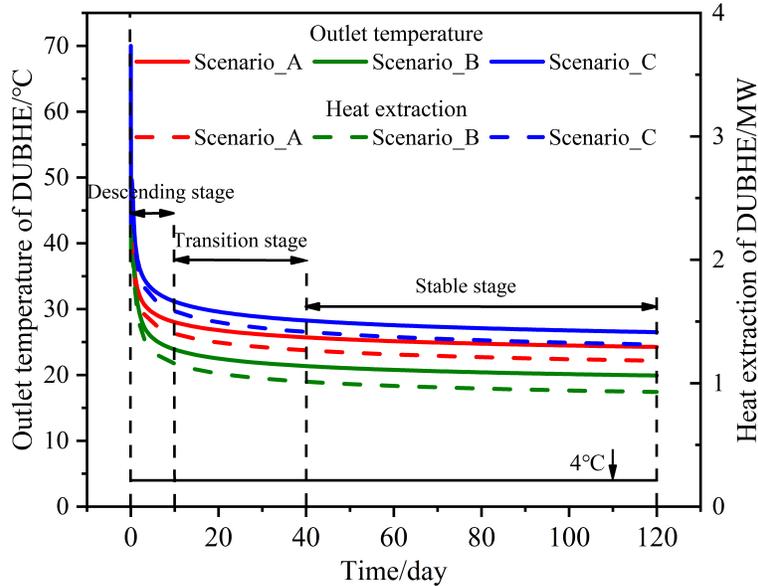


Figure 8: Outlet temperature and heat extraction capacity of DUBHE under three scenarios

450 To explore the environmental benefits of deep borehole geothermal heating
 451 technology, the carbon reduction potential of DUBHE is assessed based
 452 on long-term dynamic heat extraction performance. Assuming that the thermal
 453 efficiency of the coal-fired boiler is 85%, the carbon emission reduction
 454 potential of three scenarios can be calculated. With the highest geothermal
 455 gradient and soil thermal conductivity, Scenario_C has the best performance
 456 in carbon emission reduction, while Scenario_B with the lowest thermal conductivity
 457 has the lowest emission reduction. During the 20 heating seasons,
 458 the average value of emission reduction for the three scenarios can be calculated,
 459 which are 9559.75 tons of standard coal, 25390.71 tons of carbon dioxide emission,
 460 81.26 tons of sulfur dioxide emission, 149.04 tons of nitrogen oxide emission,
 461 and 91.68 tons of dust emission. It can be seen that the carbon emission reduction
 462 potential of the DUBHE system is considerable.
 463 It is worth vigorously promoting this kind of heating technology in the area
 464 with abundant geothermal resources to contribute significantly to a green
 465 and sustainable future.

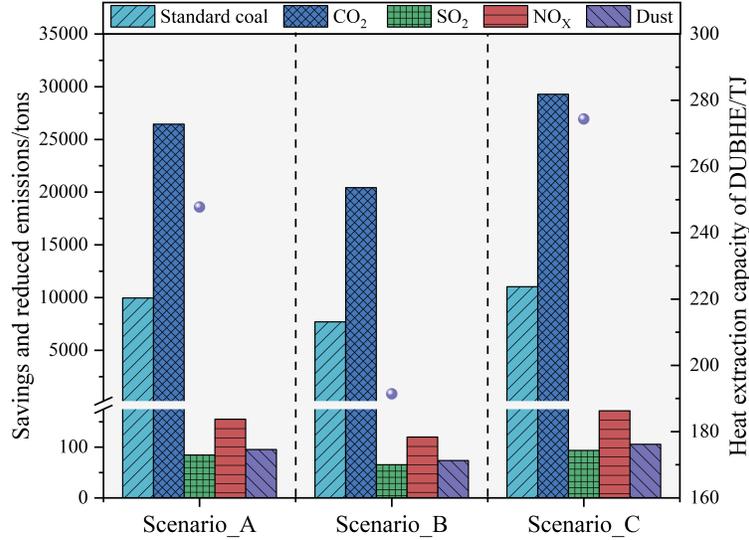


Figure 9: Corresponding carbon reduction amount of DUBHE under the same design parameters

466 6.2. Future work

467 Geothermal energy, as renewable energy with great development poten-
 468 tial in the 21st century [61], has been widely used in the world. Right now,
 469 geothermal energy is basically used for power generation, building heating,
 470 and agriculture. In 2019, the global wind power with a total installed capac-
 471 ity of 6.5 million kilowatts [62], given that clean energy power has become
 472 the future trend. Combining the energy storage concept and the deep bore-
 473 hole geothermal heating technology organically can be an important goal of
 474 the development of renewable energy. In the future research, we will focus
 475 on the combination of DUBHE and energy storage technology, and inves-
 476 tigate the feasibility of coupled energy storage and the DUBHE system, so
 477 as to provide new ideas for the development of energy storage technology in
 478 the future.

479 7. Conclusions

480 The main purpose of this study is to evaluate the heat extraction per-
 481 formance of DUBHE with different geological parameters during long-term
 482 operation. 3D numerical heat transfer models of DUBHE are built using
 483 OpenGeoSys software and the Taguchi method is introduced for this pur-
 484 pose. Thermal conductivity, geothermal gradient, specific heat capacity,

485 groundwater flow direction, and Darcy velocity five geological parameters
486 and corresponding three levels are considered and 18 sets of orthogonal
487 simulation conditions $L_{18}(3^5)$ is made. Using the S/N ratio and ANOVA
488 method, the optimal combination and contribution rate of each influencing
489 factor have been identified and analyzed in detail. To be more specific:

490 (i) Determined by the Taguchi method, the influence for T_{out} indexes
491 follows the sequence of geothermal gradient (70.14%), thermal conductivity
492 (27.59%), specific heat capacity (0.95%), Darcy velocity (0.20%), and
493 groundwater flow direction (0.13%). The calculation of ANOVA method in-
494 dicates that geothermal gradient and thermal conductivity play a vital role
495 in assessing the value of Q_{total} with 62.10% and 35.18% of the contribution
496 rate respectively. The impact of specific heat capacity (0.74%), groundwater
497 flow direction (0.38%), and Darcy velocity (0.19%) can be nearly neglected
498 for Q_{total} of DUBHE. And for the D_{soil} index, the influence degree is in the
499 order of specific heat capacity, thermal conductivity, Darcy velocity, geother-
500 mal gradient, and groundwater flow direction, along with contribution rates
501 of 92.41%, 6.74%, 0.21%, 0.04%, and 0.02% respectively.

502 (ii) By integrating T_{out} , Q_{total} , and D_{soil} indexes with the assumption of
503 average weight proportion, the final optimized combination is $A_3B_3C_3D_3E_3$.
504 The optimized values of thermal conductivity, geothermal gradient, specific
505 heat capacity, groundwater flow direction, and Darcy velocity are level-3
506 (detailed parameters are shown in Table 2). According to the optimized
507 combination of three indexes, the T_{out} reaches 33.92 °C and the Q_{total} is
508 284.08 TJ under long-term operation conditions, while the D_{soil} is 12.66%
509 by using the optimal parameters set.

510 (iii) The popularization of DUBHE has certain environmental friendli-
511 ness and benefits to the environment considering decarbonization. In the
512 case study, the quantification of the reduction potential of carbon emission
513 shows that 1 TJ of heat provided by DUBHE is equivalent to a reduction
514 of 40.19 tons of standard coal. Moreover, 106.75 tons of CO_2 emission,
515 341.65 kg of SO_2 emission, 626.62 kg of NO_x emission, and 385.46 kg of
516 dust emission can be reduced for 1 TJ of heat provided by DUBHE.

517 Our work shows that the three geological parameters of geothermal gra-
518 dient, thermal conductivity, and specific heat capacity of soil have significant
519 influences on the long-term performance of DUBHE. Moreover, the ground-
520 water seepage also has certain effects on the long-term performance of the
521 DUBHE system so it should be carefully considered and evaluated in the sys-
522 tem design. Therefore, sufficient geological investigation should be adopted
523 in the early stage of the geothermal projects to ensure the long-term sus-
524 tainability of DUBHE. Comprehensive simulation tools such as OpenGeoSys

525 can be introduced to conduct the optimization in the application of deep
 526 geothermal energy.

527 **8. Appendix**

$$M_1 = \begin{bmatrix} 28.81 & 0 & 0 & 0 & 0 \\ 29.55 & 0 & 0 & 0 & 0 \\ 31.45 & 0 & 0 & 0 & 0 \\ 0 & 27.77 & 0 & 0 & 0 \\ 0 & 29.94 & 0 & 0 & 0 \\ 0 & 32.11 & 0 & 0 & 0 \\ 0 & 0 & 30.20 & 0 & 0 \\ 0 & 0 & 29.92 & 0 & 0 \\ 0 & 0 & 29.70 & 0 & 0 \\ 0 & 0 & 0 & 30.03 & 0 \\ 0 & 0 & 0 & 29.85 & 0 \\ 0 & 0 & 0 & 29.94 & 0 \\ 0 & 0 & 0 & 0 & 29.86 \\ 0 & 0 & 0 & 0 & 29.89 \\ 0 & 0 & 0 & 0 & 30.07 \end{bmatrix}$$

$$T_1 = \begin{bmatrix} 0.011 & 0 & 0 & 0 & 0 \\ 0 & 0.011 & 0 & 0 & 0 \\ 0 & 0 & 0.011 & 0 & 0 \\ 0 & 0 & 0 & 0.011 & 0 \\ 0 & 0 & 0 & 0 & 0.011 \end{bmatrix}$$

$$S_1^T = [0.335 \quad 0.551 \quad 0.064 \quad 0.023 \quad 0.027]$$

$$M_2 = \begin{bmatrix} 153.96 & 0 & 0 & 0 & 0 \\ 173.84 & 0 & 0 & 0 & 0 \\ 221.18 & 0 & 0 & 0 & 0 \\ 0 & 137.20 & 0 & 0 & 0 \\ 0 & 182.82 & 0 & 0 & 0 \\ 0 & 228.96 & 0 & 0 & 0 \\ 0 & 0 & 181.61 & 0 & 0 \\ 0 & 0 & 178.85 & 0 & 0 \\ 0 & 0 & 188.52 & 0 & 0 \\ 0 & 0 & 0 & 184.72 & 0 \\ 0 & 0 & 0 & 180.06 & 0 \\ 0 & 0 & 0 & 184.21 & 0 \\ 0 & 0 & 0 & 0 & 180.75 \\ 0 & 0 & 0 & 0 & 181.09 \\ 0 & 0 & 0 & 0 & 187.14 \end{bmatrix}$$

$$T_2 = \begin{bmatrix} 0.0018 & 0 & 0 & 0 & 0 \\ 0 & 0.0018 & 0 & 0 & 0 \\ 0 & 0 & 0.0018 & 0 & 0 \\ 0 & 0 & 0 & 0.0018 & 0 \\ 0 & 0 & 0 & 0 & 0.0018 \end{bmatrix}$$

$$S_2^T = [0.374 \quad 0.511 \quad 0.054 \quad 0.026 \quad 0.036]$$

$$M_3 = \begin{bmatrix} 7.56 & 0 & 0 & 0 & 0 \\ 7.31 & 0 & 0 & 0 & 0 \\ 7.13 & 0 & 0 & 0 & 0 \\ 0 & 7.34 & 0 & 0 & 0 \\ 0 & 7.33 & 0 & 0 & 0 \\ 0 & 7.31 & 0 & 0 & 0 \\ 0 & 0 & 6.77 & 0 & 0 \\ 0 & 0 & 7.04 & 0 & 0 \\ 0 & 0 & 8.35 & 0 & 0 \\ 0 & 0 & 0 & 7.32 & 0 \\ 0 & 0 & 0 & 7.34 & 0 \\ 0 & 0 & 0 & 7.32 & 0 \\ 0 & 0 & 0 & 0 & 7.29 \\ 0 & 0 & 0 & 0 & 7.32 \\ 0 & 0 & 0 & 0 & 7.37 \end{bmatrix}$$

$$T_3 = \begin{bmatrix} 0.045 & 0 & 0 & 0 & 0 \\ 0 & 0.045 & 0 & 0 & 0 \\ 0 & 0 & 0.045 & 0 & 0 \\ 0 & 0 & 0 & 0.045 & 0 \\ 0 & 0 & 0 & 0 & 0.045 \end{bmatrix}$$

$$S_3^T = [0.207 \quad 0.016 \quad 0.728 \quad 0.012 \quad 0.036]$$

$$W = \frac{(W_1 + W_2 + W_3)}{3} = \frac{1}{3} \left(\begin{bmatrix} 0.1062 \\ 0.1089 \\ 0.1159 \\ 0.1683 \\ 0.1815 \\ 0.1946 \\ 0.0213 \\ 0.0211 \\ 0.0209 \\ 0.0076 \\ 0.0076 \\ 0.0076 \\ 0.0089 \\ 0.0089 \\ 0.0089 \end{bmatrix} + \begin{bmatrix} 0.1036 \\ 0.1170 \\ 0.1489 \\ 0.1262 \\ 0.1682 \\ 0.2106 \\ 0.0177 \\ 0.0174 \\ 0.0183 \\ 0.0086 \\ 0.0084 \\ 0.0086 \\ 0.0117 \\ 0.0117 \\ 0.0121 \end{bmatrix} + \begin{bmatrix} 0.0704 \\ 0.0681 \\ 0.0664 \\ 0.0053 \\ 0.0053 \\ 0.0053 \\ 0.2218 \\ 0.2306 \\ 0.2735 \\ 0.0040 \\ 0.0040 \\ 0.0040 \\ 0.0118 \\ 0.0119 \\ 0.0119 \end{bmatrix} \right) = \begin{bmatrix} 0.0934 \\ 0.0980 \\ \mathbf{0.1104} \\ 0.0999 \\ 0.1183 \\ \mathbf{0.1368} \\ 0.0869 \\ 0.0897 \\ \mathbf{0.1043} \\ 0.0067 \\ 0.0066 \\ \mathbf{0.0067} \\ 0.0108 \\ 0.0108 \\ \mathbf{0.0110} \end{bmatrix} = \begin{bmatrix} A_1 \\ A_2 \\ A_3 \\ B_1 \\ B_2 \\ B_3 \\ C_1 \\ C_2 \\ C_3 \\ D_1 \\ D_2 \\ D_3 \\ E_1 \\ E_2 \\ E_3 \end{bmatrix}$$

528 **CRedit authorship contribution statement**

529 **Jinghua Jiang:** Conceptualization, Methodology, Software, Validation,
530 Writing - Original Draft, Visualization. **Fenghao Wang:** Conceptual-
531 ization, Formal analysis, Project administration, Funding acquisition, Su-
532 pervision. **Xiong Yang:** Methodology, Software, Visualization. **Yuping**
533 **Zhang:** Investigation, Data curation. **Jiewen Deng:** Methodology, In-
534 vestigation. **Qingpeng Wei:** Methodology, Formal analysis. **Wanlong**
535 **Cai:** Conceptualization, Software, Validation, Investigation, Writing - Re-
536 view & Editing. **Chaofan Chen:** Methodology, Software, Writing - Review
537 & Editing, Resources.

538 **Declaration of competing interest**

539 The authors declare that they have no known competing financial in-
540 terests or personal relationships that could have appeared to influence the
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