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Table 2. Details on *How to sample*

Table 3. Details on *How to model*

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Abstract

Biodiversity conservation faces a methodological conundrum: Biodiversity measurement often relies on species, most of which are rare at various scales, especially prone to extinction under global change, but also the most challenging to sample and model. Predicting the distribution change of rare species using conventional species distribution models is challenging because rare species are hardly captured by most survey systems. When enough data is available, predictions are usually spatially biased toward locations where the species is most likely to occur, violating the assumptions of many modelling frameworks. Workflows to predict and eventually map rare species distributions imply important trade-offs between data quantity, quality, representativeness, and model complexity that need to be considered prior to survey and analysis. Our opinion is that study designs need to carefully integrate the different steps, from species sampling to modelling, in accordance to the different types of rarity and available data in order to improve our capacity for sound assessment and prediction of rare species distribution. In this article, we summarize and comment on how different categories of species rarity lead to different types of occurrence and distribution data depending on choices made during the survey process, namely the spatial distribution of samples (where to sample) and the sampling protocol in each selected location (how to sample). We then clarify which species distribution models are suitable depending on the different types of distribution data (how to model). Among others, for most rarity forms, we highlight the insights from systematic species-targeted sampling coupled with hierarchical models that allow correcting for overdispersion and for spatial and sampling sources of bias. Our article provides scientists and practitioners with a much-needed guide through the ever-increasing diversity of methodological developments to improve prediction of rare species distribution depending on rarity type and available data.

Keywords
bias, detectability, distribution change, methods, occupancy, rare species, sampling, spatial data, species distribution modelling, survey

Box 1. Glossary (of the terms underlined in the main text)

- **Hierarchical Models (HM):** or *multi-level models*. Statistical models of parameters that vary at more than one level of data organization (e.g., nested data, such as abundances of a given species located in different habitat types themselves located in different ecoregions) and thus allow accounting for the potential interdependence between the data points (for further details, see e.g. (Gelman & Hill, 2007; Raudenbush & Bryk, 2002)).
- **Mark-release-recapture (MRR):** Mark-release-recapture, or *capture-mark-recapture*, is a sampling technique that consists in capturing, marking and releasing individuals of a species in a first capture session. In one or more follow-up capture sessions, the ratio of marked to unmarked specimens is taken to estimate population size (see e.g. (Southwood & Henderson, 2009; B. K. Williams et al., 2002)).
- **Occupancy:** Occupancy can refer to two different notions (MacKenzie et al., 2017); (1) the probability of a site to be occupied by a given species, i.e. the *a priori* expectation that a particular site will be occupied by the species as determined by

some underlying process (or occurrence probability), (2) the proportion of area or sites occupied, which results from the realization of the former process.

- **Patchiness:** The way habitat patches (and populations) are distributed through space. Habitat patches can be clumped (i.e. spatially aggregated in patches concentrated in a few places, potentially most at risk under environmental stochasticity), patchy (i.e. spatially aggregated according to irregular patterns, e.g. one, two, or five patches per group of patches), random, and regular (i.e. uniformly distributed apart from each other).
- **Spatially representative sample-set:** Sample-set collected at a set of locations that are spatially distributed in a statistically unconstrained manner, e.g. by a stratified design, in which areas are stratified according to their environmental conditions and the number of samples in each stratum is proportional to the area of that stratum. Such sampling is spatially representative of the variability of these conditions over the whole study area and does not over-represent unusual but rare environmental conditions.
- **Species Distribution Model (SDM):** Here used as a generic catch-all term to refer to any empirical model that allows spatially-explicit prediction of the current or future environmental suitability for a species (using presence-only, presence/absence and/or abundance data) based on predictors (such as climate, land-use, etc.) and, possibly, scenarios (e.g. IPCC's climate change scenarios) (Guisan & Thuiller, 2005). Depending on the objectives and underlying assumptions – but mostly using the same types of data and algorithms, these models are also called ecological niche models (ENMs), habitat suitability models (HSMs), niche-based models (NBMs), potential habitat distribution models (PHDMs), and when used only with climate variables, climate-envelope models (CEMs) or climate matching models (CMMs) (Guisan et al. 2013). For instance, ENM can give more focus to species niche quantification or requirements while strict SDMs focus more on getting spatial predictions of species distribution(Saupe et al., 2012). In the context of rare species modelling, models aim to predict either the probability / likelihood of occurrence, or

the probability of environmental suitability for the species, with the caution that these predictions may differ from the realized distribution because a location may be suitable but not reachable by the species.

Introduction

Almost all international, national, and local conservation planning activities flag biodiversity as a crucial environmental property (e.g. Aichi Targets, Sustainable Development Goals) (Butchart et al., 2016; Griggs et al., 2013) to be protected from the deleterious effects of habitat loss, exploitation, pollution and climate change (IPBES, 2019; Maxwell et al., 2016; Rands et al., 2010). However, biodiversity measurement often relies on species, most of which are rare at various scales (Enquist et al., 2019; Fontaine et al., 2007; Hartley & Kunin, 2003; Henle et al., 2010; Rabinowitz, 1981; Steege et al., 2013). Several initiatives to halt biodiversity loss have questioned whether current measures of biodiversity do actually sufficiently account for rare species (e.g. Fontaine et al., 2007). For example, one third of plant species worldwide are too poorly known and have too few data for a Red List assessment (Brummitt et al., 2015; Enquist et al., 2019). At the same time, rare species are especially prone to extinction (Courchamp et al., 2006; Henle et al., 2004; Işik, 2011; Kunin & Gaston, 1993; McKinney, 1997). One way to assess extinction risk is to track the change in spatial distribution through time (Araújo et al., 2002; Benito et al., 2009; Gärdenfors et al., 2001; Thomas et al., 2004). Therefore, protecting species diversity directly implies protecting rare species, which requires understanding their distribution patterns.

Unfortunately, rarity causes considerable methodological difficulties in obtaining sufficient data from survey programmes or alternative sources (e.g. D. L. Roberts et al., 2016), which limits the ability of models to predict distribution patterns. For example, many studies using species distribution models (SDMs, *defined in Box 1)* need a minimum number of occurrences below which the models cannot be reliably trained and/or validated (e.g. van Proosdij et al., 2016). Thus, we are locked in the 'rare-species modelling paradox' (Lomba et al., 2010): the majority of species that require the greatest protection also are the species we know least about and are most difficult to model.

However, rarity is an umbrella term used to describe various types of distribution patterns at various scales. Rabinowitz (1981) defined seven categories of rarity based on combinations of the range of a species, the distribution of populations within its range and the local density of the species when present (**Figure 1a**). Whatever measure used (e.g. range size, occupancy, abundance, relative cover, biomass), and ecosystem or scale of the study, a community is likely to include a handful of common species and a long tail of rare species (Fisher et al., 1943; Preston, 1948). The resulting pattern of species-abundance distributions, following a log-like curve in most natural systems (but also see (Magurran & Henderson, 2003)), is observed on local to global scales, with correspondingly fine abundance (McGill et al., 2007) to range size frequency (Gaston, 1998) data.

With the goal of mapping rare species' distribution ranges and changes for protection purposes, each of the seven types of rarity implies different problems in accumulating data for modelling. For example, two species A and B with similar prevalence are both found within an area: Species A has a narrow range with high local density (rarity category 2) and species B has a broad range with low local density (rarity category 4). Randomly distributed sampling in this area is likely to sample only a few sites where species A is present and many sites where species B is present; consequently, species B’s distribution is likely to be better evaluated than species A’s distribution. However, *a priori* knowledge on where species A is present may mean that species A is more often encountered than species B; consequently, the dataset contains more presences of species A than of species B. The type of rarity, the spatial distribution of samples and the protocol used to sample each location thus all affect the data generated, and the types of model used to project the species’ distribution range. Finally, with the perpetual changes in taxonomy (taxonomic revisions), the identification, assessment, and conservation of rare species are constantly challenged (Ota, 2000; Schwartz & Simberloff, 2001; Standley, 1992) (but see also (Domínguez Lozano et al., 2007; Simkins et al., 2020)) and the expected increase of species number for some taxonomic groups (Morrison III et al., 2009) foresees an endless need to coping with rarity issues.

We therefore face a conundrum in which, although rarity is ubiquitous, it is particularly challenging to account for, sample and model, at all scales. While some publications already provide comprehensive overview on specific aspects of the different steps from sampling to modelling rare species (Cunningham & Lindenmayer, 2005; Green & Young, 1993; Hermoso et al., 2015; Kenkel et al., 1990; Milner-Gulland & Rowcliffe, 2007; Robinson et al., 2018; W. Thompson, 2013), how to improve our prediction of rare species distribution changes remains a complete challenge to date (Aubry et al., 2017; Didham et al., 2020; Galante et al., 2018; Helmstetter et al., 2021). Our perspective is that all steps need to be integrated in study design. In particular, their sequence needs to be adapted to the different types of rarity to improve our capacity for sound assessments and predictions of the distribution of the majority of biodiversity. However, the trade-offs faced when modelling the distribution of rare species and the decision path linking the form of rarity with the sampling and modelling strategies have largely been neglected. Therefore, to help untangle the rarity conundrum and adapt modelling strategies to the rarity issues, we aim, for each of Rabinowitz's categories of rarity:

(i) To identify the main trade-offs involved in selecting adequate, cost-effective sampling strategies and how these affect the properties of the data,
(ii) To identify modelling frameworks that are potentially suitable for the type of data generated and to highlight gaps that require model development.

To address the first aim, we focus on the spatial distribution of samples ('where to sample') and on the protocols used to do the sampling ('how to sample'). For the second aim, we list and discuss the main modelling frameworks suitable for producing distribution maps for different types of rarity ('how to model'). We synthesize our findings, provide guidelines to optimize and integrate monitoring and modelling of rare species depending on their rarity characteristics and briefly discuss remaining challenges with respect to sampling and modelling rare species.

Where to sample

When setting up a survey program there are multiple ways by which the spatial allocation of samples can be decided (**Table 1**; **Figure 1b**). Any choice made at this stage will affect the properties of the collected data. The main trade-off to consider is between sampling efficiency and spatial coverage.

Locally-focused sampling targeting a particular species allows its population to be studied efficiently, but at the expense of a spatially non-representative sample of the species distribution. This conflicts with the aim of covering the realised niche of a species, an assumption of most modelling frameworks. For species whose distribution range is relatively wide and distribution pattern is dispersed (common species and rarity category 4), a spatially representative sample-set of the entire extent is more likely to provide the required occurrence data. Spatially representative sampling has several positive properties. First, data are comparable among species, allowing cost-effective monitoring of multiple species. Second, even if the location of samples is not constant, data remain comparable between years, allowing the detection of temporal changes in distribution (if sampling intensity is kept constant). Third, data on the focal species fit easily into most modelling frameworks, if enough are collected. This is usually done with a systematic sampling scheme on a grid, stratifying the sampling according to habitat or land cover (while ensuring proportional sampling in each stratum), or by randomly selecting the sampling locations (**Table 1**; **Figure 1b**).

However, for species with narrow and/or clumped and patchy distribution patterns (rarity categories 1, 2, 3, 5, 6, 7), a random sample-set of the entire extent is unlikely to capture sufficient information. For example, in the 2007 UK plants countryside survey, 591 one-km^2

locations were included in a stratified random design (Bunce et al., 2014; Carey et al., 2008): the survey recorded 880 species. As there are approximately 4000 plant species in the UK, the survey failed to detect 2400 rare species. In fact, the narrower and clumpier the distribution of a species, the larger the number of random sites needed to encounter the species in enough locations to make credible estimates of abundance or distributional status and changes. Thus, one may need to constrain the sampling towards the target species.

Various methods allow the distribution of samples to target locations more likely to contain a certain rare species (**Table 1**; **Figure 1b**). One such example is adaptive sampling (W. Thompson, 2013; Yoccoz et al., 2001). Many programs periodically monitoring rare species sample locations where the species is known to occur, but rarely look in new sites. Such adaptive sampling may be excellent in keeping track of known populations, but eventually leads to erroneous conclusions regarding distribution trends. Consider a species subject to metapopulation dynamics, experiencing local extinctions and colonization of patches: if sampling is in known locations only, one may identify all local extinctions (and a preceding gradual decrease in population size) but not identify the colonization of new patches. Thus, we might wrongly conclude that the species distribution is deteriorating while it may in fact be in an equilibrium state (Magurran et al., 2010) (but see (McRae et al., 2017)).

Another fruitful approach is to combine adaptive with SDM-guided sampling (Aizpurua et al., 2015; Chiffard et al., 2020; e.g. Lin et al., 2014) where one sampling session provides information to model and the following sessions allow adjusting the distribution of samples (S. K. Thompson, 2013; W. Thompson, 2013; Yoccoz et al., 2001). For example, a SDM with data sampled at a certain time can tag potentially unknown local populations for sampling the next year (e.g. Lin et al., 2014). Once the area is sampled and SDM parameters updated, the SDM is re-run and new locations targeted. Such a strategy may be very efficient at accumulating observations of rare species. However, it comes with the risk of estimating an over-optimistic occupancy trend, as the number of detected presences can increase over time while the distribution actually decreases (**Table 1**). Appropriately parametrized stacked SDMs, including rarity weighting, can further allow improving the sampling of multiple rare species and help prioritize sampling areas (Rosner-Katz et al., 2020). Any form of adaptive sampling therefore needs considerable manipulation and/or reliable complementary information for further species distribution modelling (Dorazio, 2014; Hefley et al., 2014; Phillips et al., 2009; Raes & ter Steege, 2007).

The transition from spatially representative sampling to species-targeted sampling also reflects a gradient of *a priori* knowledge (**Table 1**). Random sampling does not require specific knowledge. Adaptive sampling and SDM-guided approaches instead need considerable knowledge of the species and its requirements before designing the sampling scheme. Stratified schemes require knowledge about sampling sites and their habitats or environmental conditions across the full range of the target species. Additionally, stratified schemes depend on the quality of the original information used to guide the stratification that has its own uncertainty, due to potential spatial errors and classification issues (Rocchini et al., 2011).

To summarize, different strategies for defining the spatial distribution of samples reflect the compromise between sampling efficiency and spatial representativeness (**Figure 1b**). Overall, three main types of data may be generated, each with implications for modelling: data can be spatially representative (of the species range, potentially for multiple species), spatially constrained independent of the species, or spatially constrained towards particular species.

How to sample

For assessing the distribution of species and changes therein, sampling should aim to collect the appropriate quantity of presence data, reduce the number of false absences, and account for detectability of the sampled species (**Table 2**; **Figure 1c**). Locally rare as well as elusive (e.g. cryptic or trap-shy) species (W. Thompson, 2013) both pose specific challenges. The probability of detecting a species depends on a range of factors, such as

habitat type, time of the day and year, population density and methods employed to survey the species. Repeated sampling with methods targeting rare and elusive species reduce the probability of false absences and the latter may generate presence/absence data accounting for detection probability (MacKenzie et al., 2017).
Multiple methods increase the detectability of species; some are just a function of sampling effort (e.g. longer transects), others are more directly related to the known ecology of the target species (**Table 2**; **Figure 1c**). These latter methods include, for example, baited traps (e.g. Steyer et al., 2013), camera traps (e.g. Schüttler et al., 2017), species-specific markers in environmental DNA (eDNA) sampling (e.g. Carraro et al., 2018), expert knowledge of the species' habitat preference and/or behaviour, or the use of detection dogs (Grimm-Seyfarth et al., 2019; Grimm-Seyfarth & Klenke, 2019; Hollerbach et al., 2018).

There are several points to consider. First, most of these methods increase the effort or costs required compared with simpler methods, especially when the sampling aims to detect several rare species simultaneously. Second, methods increase detection probability differently for different species, producing output less comparable between species unless methods are highly standardized. For example, a trap baited with pheromones of a specific species will attract more individuals of the focal species than baiting a trap with food utilized by many species (e.g. dung for dung beetles) (Marsh et al., 2013). However, recent advances in genetic monitoring, such as improved markers in eDNA detection of stream species (Carraro et al., 2021; e.g. Jerde et al., 2011; Leese et al., 2021), significantly increase the number of species detected, including many rare species, especially from rivers over several kilometres in length (Altermatt et al., 2020; e.g. Mächler et al., 2019) - but these methods still need further calibration works (Alsos et al., 2018; e.g. Beng & Corlett, 2020; Cristescu & Hebert, 2018). Third, highly standardized protocols are essential for comparisons among sites, although some variability in detectability between sites will remain; for example, bird songs are less audible in leaved deciduous forests than in mixed pine forests (Pacifici et al., 2008).

Some sampling methods generate presence/absence and even abundance data in sufficient quality and quantity to account for detection probability (with repeated sampling of selected sites during a specific period (Mackenzie & Royle, 2005). Among others, such methods include distance sampling (Buckland et al., 2015) and capture-mark-recapture (B. K. Williams et al., 2002). For the latter, capture by camera traps coupled with image analysis is particularly promising for rare species (Schüttler et al., 2017) (**Table 2**; **Figure 1c**). Although these data greatly increase the spectrum of models that can be applied, they require high effort and cost; hardly suitable for rare species except perhaps for those with high local density. However, combining such methods with occupancy surveys or opportunistic observations (e.g. atlas or citizen-science data) and the incorporation of environmental data as potential predictors of occupancy and/or abundance may allow the extrapolation of rare species distributions across large spatial scales (e.g. Bowler et al., 2019; Giraud et al., 2016).

How to model

As discussed above, choices on the spatial distribution of samples eventually lead to three types of datasets: spatially representative, spatially constrained independent of the species (e.g. due to unrepresentative sampling of environments (see e.g. Bystriakova et al., 2012; Varela et al., 2014)), or spatially constrained towards target species. From a modelling perspective, this results in a trade-off between the number of presences and the need to account for spatial auto-correlation in the data. Similarly, sampling protocols affect the type of data obtained for modelling, be it presence-only, presence/absence, or presence/absence with detectability or estimates of abundances, and thus condition the type and quality of inference. Depending on the type of rarity, the 'where to sample' and 'how to sample' decisions, successful modelling of rare species require modelling tools that fall into all combinations of the cases above (**Figure 1d**).

When only presences are available, some methods produce pseudo-absences based on external information (e.g. habitat suitability (Barbet-Massin et al., 2012)). For some models, such as Maxent and Poisson point-process models (PPPMs), pseudo-absences are better interpreted as background points, not implying absences but rather samples of the available environment, where presences are compared against unsampled background locations (Merow et al., 2013; Phillips et al., 2009). They do not produce probability of occurrence but relative occurrence rates (Guillera-Arroita et al., 2015) and can be appropriate for rare species modelling if proper bias correction is applied (**Table 3**; **Figure 1d**).

Where presence/absence data are available, developments in SDMs allow handling of data over-dispersion (e.g. negative-binomial and mixed effect models (Harrison, 2014; Molenberghs et al., 2007; O'Hara & Kotze, 2014)), spatial-autocorrelation (e.g. F. C. Dormann et al., 2007; Marcer et al., 2013), uncertainty in predictions (e.g. ensemble forecasting (Araújo & New, 2007; Guisan et al., 2017; Thuiller et al., 2019)), and biases due to sampling scales (Keil et al., 2013; Keil & Chase, 2019). Hierarchical models (HM) are especially useful due to their flexibility: they describe, on the one hand, the true state of nature that is not or only partly observable (e.g. variation in occurrence probability potentially due to variation in available resources), and on the other hand, the measurement error (e.g. variation in detection probability potentially due to variable observer skills) (Kéry & Royle, 2015). Multi-scale hierarchical SDMs account for the fact that increasing the sampling extent increases the probability of detecting rare species (Rocchini et al., 2017). HMs thus allow imperfect detectability to be considered in the modelling procedure (**Table 3**). By integrating prior knowledge, Bayesian Belief Networks explicitly decompose causal pathways involved in the capture rate of species, including respective influences of detection and occupancy in small or incomplete datasets (Uusitalo, 2007): capture can be considered dependent on detectability, influenced by date and trapping effort, and by occupancy, influenced by suitability of local habitat conditions (Marcot et al., 2006). Such methods have already proved useful for modelling species distributions (Van Echelpoel et al., 2015) and responses of rare and endangered species (Hamilton et al., 2015; Smith et al., 2007) (**Table 3**).

When abundance data from standardized survey or monitoring protocols are available, these can be used to fit rare species distribution models and track distribution changes (Howard et al., 2014). However, because such protocols usually do not detect most of the rare species, especially clumped and low local-density species (see 'how to sample' section), abundance-based SDMs are rarely possible for rare species.
If recapture data are available, distribution modelling can be done using classical site-occupancy models and different methods developed as mark-release-recapture analyses (MacKenzie et al., 2017; K. H. Pollock et al., 1990) (**Table 3**).

For occurrence data from spatio-temporally replicated measurements of presences/absences, under the assumption of population closure (i.e. if the populations did not exchange propagules between the time steps under study), the Royle-Nichols model (Kéry & Royle, 2015; Royle & Nichols, 2003) allows occurrence probability to be estimated and detection heterogeneity accommodated (**Table 3**; **Figure 1d**). When 'unmarked' abundance data are available, N-mixture models can estimate both detectability and abundances used in large-scale species distribution modelling (Guélat & Kéry, 2018; Jakob et al., 2014; Kéry, 2018) (**Table 3**; **Figure 1d**). When potential sources of measurement bias are known (e.g. type of observer, weather, vegetation density), these can be integrated as covariates in the latent state submodel (e.g. Cunningham & Lindenmayer, 2005).

When data are zero-inflated, as typical for rare species data, variants of Royle-Nichols or N-mixture models can be applied that allow extra parameters and account for data overdispersion. Variants of N-mixture models have further been developed that address spatial bias and scale-dependence, such as variation of sampling grain size (Keil et al., 2018) or scales of environmental influence (R. Chandler & Hepinstall-Cymerman, 2016). However, the underlying assumptions are quite restrictive for species distribution modelling and further simulation studies are needed to assess their performance with rare species when assumptions are not met. This approach is also not necessarily the most cost-effective strategy when it comes to tracking species distribution changes over time compared with presence/absence data (Joseph et al., 2006).

When multiple types of data are available (presences, presence/absence, abundance), their combination within single modelling frameworks provides valuable insights into predicting species distributions, occupancy, even abundance (**Table 3**). Even if available over a restricted spatial extent, multiple sources of abundance data can be used together with more extensive data, such as occupancy surveys or opportunistic observations. HMs can include different submodels for the different sources of data, and potential detection biases, and incorporate environmental data as potential predictors of occupancy and/or abundance. Such methods allow extrapolation and even comparison of rare species' distributions across large spatial scales (e.g. Bowler et al., 2019; Giraud et al., 2016) and potentially for all categories of rarity if data sources are available and models well built (**Figure 1d**).

To summarize, model choice will mainly depend on the nature of the data and biases involved. From presence only, to presence/absence, to abundance, in **Figure 1d**, there is a change in the temporal comparability of SDMs, and thus their ability to track distributional changes. In the top row, the output is relative likelihood, which is not comparable even for a given species over multiple time steps. Naïve presence/absence SDMs provide an estimate that does not separate probability of occurrence from detectability, but if we assume detectability to be constant across time and space (including no drastic change in abundances), the resulting probability map is comparable for a given species over time. Finally, population size information allows the separate estimation of detectability and probability of occurrence, which is comparable over time, species and space. Comparability is important as it enables conservationists to assess changes in the environmental suitability, and ideally (see Dallas & Hastings, 2018; Jiménez-Valverde et al., 2021; Weber et al., 2017), in the distribution of rare species that could require revision of a species' status and protection needs.

More generally, whatever the type of rarity, several methodological aspects are to be considered to ensure SDM quality, including predictor selection (e.g. Le Rest et al., 2014; Saupe et al., 2012; K. J. Williams et al., 2012), model averaging (e.g. Burnham & Anderson, 2004; C. F. Dormann et al., 2018), spatial-explicit cross-validation (e.g. D. R. Roberts et al., 2017), optimisation of model performance (e.g. Anderson & Gonzalez, 2011; Norberg et al., 2019; Radosavljevic & Anderson, 2014), and testing or improvement of the extrapolation abilities of the fitted models (e.g. Mesgaran et al., 2014; Owens et al., 2013; Qiao et al., 2019; Stohlgren et al., 2011; Zurell et al., 2012).

Conclusion and future perspectives

Protecting species diversity implies protecting rare species. However, surveying and modelling rare species involves considerable methodological challenges. In this paper, we have identified how the main decisions on sampling strategy condition properties of the data, and how these in turn condition the range of appropriate modelling methods. With this perspective, we provide guidelines to optimize monitoring and modelling of rare species depending on their rarity characteristics and to ensure consistency between sampling methods, and modelling approaches (**Figure 1**).

Significant data on the occurrence of species is collected by citizen scientists (Amano et al., 2016; M. Chandler et al., 2017). It is highly valuable for monitoring biodiversity at different scales, but often biased and limited to specific areas. While there are ways to correct biases in such data (Bird et al., 2014; Robinson et al., 2018), for monitoring “rarest” species (i.e. narrow distributional range, clumped population, low local density), a systematic species-targeted sampling design may be preferred. Significant advances are expected from advanced remote sensing techniques, genetic tools and using detection dogs, all with the potential to significantly increase the detection rate of rare species at comparatively low cost and with more or less bias towards the species. Above all, future research is still needed to integrate the type of rarity more explicitly into decisions on how and where to sample with the selection of appropriate models. Another challenge with respect to species conservation is that, although the rarity status is defined with respect to endemicity over a given period, it may be dynamic in the longer term, requiring constant adaptation of assessment strategies.

Considering most forms of rarity, our synthesis highlights the particular potential of HMs as a flexible tool to improve rarity modelling while accounting for spatial, observer, and species-specific biases. Advances in zero-inflation modelling in particular have to be better integrated into rare species distribution modelling as both the conceptual and technical foundations of these approaches impact on the rarity sampling and modelling issues. Considering the rarest forms of rarity, our synthesis suggests that recent HM developments to combine multiple sources of data are extremely promising (**Figure 1**).

Other promising perspectives have recently emerged, such as functional rarity modelling (Carmona et al., 2017; Violle et al., 2017) and the use of co-occurring species information (or the “neighbourly advice” (McInerny & Purves, 2011)) and of positive associations among rare species (Calatayud et al., 2019; Hines & Keil, 2020) as potentially valuable information to model rarity distribution. Other model developments include harnessing information from other sources that either directly inform a species’ distribution at larger scales, such as incorporating expert-drawn range maps (Merow et al., 2017) or elevation ranges (Ellis-Soto et al., 2021) as model offsets. Joint species distribution models (JSDMs), which model multiple species simultaneously to infer the species’ environmental response based on species co-occurrences (Ovaskainen & Soininen, 2011; L. J. Pollock et al., 2014), often incorporate ancillary information such as trait (L. J. Pollock et al., 2012) or phylogenetic similarity (Ovaskainen et al., 2017) and are promising further developments for rare species modelling (Tobler et al., 2019). Finally, machine-learning based methods, including non-parametric methods, and methods tolerant of unstructured data, have shown promise for modelling and mapping rarity with strong predictive ability (Pouteau et al., 2012; Robinson et al., 2018). Further research and sensitivity analyses are needed to assess the appropriateness of these methods in the workflow of rarity sampling and modelling, depending on the rarity type of the species.

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Author contribution

YG and AJ have equally contributed to ideas, first drafting of the paper, production of tables and figures, and coordination of the writing process. WK and KH, at the origin of the project, have jointly supervised the work as project leaders (EU BON) and have equally contributed with the central ideas, orientation and deep revisions of the manuscript. All authors have contributed with ideas and revisions on all versions of the manuscript.

List of items and captions

1 Box + 1 Figure + 3 Tables

Figure 1

Synthesis infographic of (a) the Rabinowitz's seven categories of rarity, (b) examples of approaches to assess where to sample depending on the rarity category, (c) examples of approaches to assess how to sample depending on the rarity category and species local density, and (d) examples of modelling approaches to predict and map species distribution depending on the type of data generated in previous steps (a) and (b). Note that most of the methods can be used in more than one situation, but for the simplicity of the figure, we did not systematically repeat them and rather highlighted the methods we considered as the most useful or relevant. The references (numbers in brackets) are listed below the figure.

References: [1] Breiner et al. 2015, [2] Lomba 2010, [3] Chen & Pollino 2012, [4] Fithian 2014, [5] Marcer et al. 2013, [6] Keil et al. 2013, [7] Rocchini et al. 2017, [8] El-Gabbas & Dormann 2018, [9] Radosavljevic & Anderson 2014, [10] Boria et al. 2014, [11] McKenzie et al. 2017, [12] Royle & Nichols 2003, [13] Kéry & Royle 2015, [14] Willson et al. 2011, [15] Nichols et al. 2008, [16] Giraud et al. 2016, [17] Bowler et al. 2019, [18] Joseph et al. 2009, [19] Cunningham & Lindenmayer 2005, [20] Chandler et al. 2011.

Tables 1, 2, 3

Non-exhaustive list of methods to assess (1) where to sample, (2) how to sample, and (3) how to model rare species data with their brief description, advantages and limits, the type of rarity for which they appear as most appropriate, and examples of references related. Inputs/outputs of modelling methods can be P (presences only), lik (presence likelihood), PA (Presences/Absences), ab (abundance), det (detectability information), pocc (probability of occurrence). Underlined words refer to the Glossary (**Box 1**). The references are listed below the Table 3.

Figure 1

Synthesis infographic of (a) the Rabinowitz's seven categories of rarity, (b) examples of approaches to assess where to sample depending on the rarity category, (c) examples of approaches to assess how to sample depending on the rarity category and species local density, and (d) examples of modelling approaches to predict and map species distribution depending on the type of data generated in previous steps (a) and (b). Note that most of the methods can be used in more than one situation, but for the simplicity of the figure, we did not systematically repeat them and rather highlighted the methods we considered as the most useful or relevant. The references (numbers in brackets) are listed below the figure.

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Tables 1, 2 & 3

Non-exhaustive list of methods to assess (Table 1) where to sample, (Table 2) how to sample, and (Table 3) how to model rare species data with their brief description, advantages and limits, the type of rarity for which they appear as most appropriate, and examples of references related. In Table 3: inputs/outputs can be P (presences only), lik (presence likelihood), PA (Presences/Absences), ab (abundance), det (detectability information), pocc (probability of occurrence). Underlined words refer to the Glossary (**Box 1**). The references are listed below the Table 3.

Table 1. Where to sample?

Method	Brief description	Pros	Cons	Suitable for which rarity categories?	References
Accumulated opportunistic observations	Sampling locations are not chosen but emerge from external contribution of various sources, e.g. data from citizen science programs free from any observation	- depending on the species attractivity and ease of detection/identification, a large number of observations can be accumulated over time, with minimal investment of time and funds - can detect new populations	- sample not representative of the entire extent - species-targeted - absences usually not reported, presence-only data - sampling effort varies through time - mainly done for charismatic	All	[1]Chandler et al. 2017 (iNaturalist); [2]Sullivan et al. 2017 (eBird); [3]Deguines et al. 2012 (spipoll)

Method	Brief description	Pros	Cons	Suitable for which rarity categories?	References
	protocol	and species - may be used to create atlas data - rare species receive particular attention	taxa - risk of misidentification in the case of non-expert observations (particularly critical as even a small fraction of misidentified common species may swamp the true records of a rare species)		
Simple random sampling	Random selection of the locations, i.e. all the locations of the study area have the same probability to be sampled	- spatially unbiased sample - objective and well-defined - sample representative of the study extent - temporally comparable samples - no target species, multi-species sample	- ignores environmental/habitat variability - rare species are unlikely to be detected in sufficient numbers, even in huge samples	Cat4	[4]Greig-Smith 1964; [5]Diekmann et al. 2007; [6]Hedgren & Weslien 2008

Method	Brief description	Pros	Cons	Suitable for which rarity categories?	References
Systematic sampling	Sampling according to a fixed spatial interval(s) that depends on the predefined total number of locations to be sampled in the study area, e.g. plots arranged along a regular grid or (equidistant) transects that cover the space evenly (hyper dispersed distribution of samples)	- simple to implement, no need of external information nor a priori species-specific knowledge - more cost-efficient than simple random sampling as it guarantees even distribution of sites and good coverage of the study area - temporally comparable samples - no target species, multi-species sample	- needs prior information on total number of sites to be sampled - detection strongly depends on the choice of the spatial interval of the sampling and on the starting point of the sampling, e.g. in species with clumped populations; if sampling interval is the same order of magnitude as the clumping interval, the sample will not be representative of the species distribution (will either under- or over-detect the species depending on the starting point)	Cat4 (and Cat5 if habitats are organised randomly)	[7]Madow 1953; [8]Fortin et al. 1989

Method	Brief description	Pros	Cons	Suitable for which rarity categories?	References
Stratified sampling	Sampling organised with respect to a categorisation deemed to be important for the community or species of interest, e.g. habitat type	- sample representative of the study extent with respect to the stratification factor	- depends on subjective a priori, or a priori ecological knowledge	Cat1, Cat3, Cat5, Cat7 (if we consider that for non-specialist species, habitat-stratified sampling would work worse)	[9]Thompson W.L. 2013

Method	Brief description	Pros	Cons	Suitable for which rarity categories?	References
Adaptive (cluster) sampling / prior-informed sampling	Sampling design where site selection depends on previous sampling raw outcomes, either a) from the overall survey, e.g. adaptive *cluster* sampling which consists in searching for a species in a given location and if the species is found, searches continue nearby (neighbourhood shape can vary according to the	- accurate estimations of species abundances - appropriate for rare, clustered and unevenly distributed species	- not widely used in ecological studies - efficiency depends on the spatial distribution of the species - difficult to know the final sample size needed prior to the survey - data collection process is complicated - not fully adapted yet to mobile species, sensitive species and habitats (side-effects of intensive sampling) - resulting data biased towards the species of interest - sampling effort varies through time	Cat2, Cat3	[10]Krebs et al. 1989; [11]Yoccoz et al. 2001; [12,13]Thompson S.K. 1990; 2013; [14]Thompson W.L. 2002

Method	Brief description	Pros	Cons	Suitable for which rarity categories?	References
	study needs), or b) from other surveys, i.e. site selection depends on external source of information and/or belief on the species potential presence, e.g. atlas data				
"SDM"-guided sampling	Sampling locations are drawn from a probability surface generated by modelling the know P/A of a species against	- sampling coverage optimisation - allows a systematic and exhaustive pre-selection of suitable locations	- time-consuming process - requires predictor layers (with good spatial and thematic resolution for narrow range species) - subject to model error and uncertainty	Cat1, Cat3 (potentially Cat5, Cat 7 if clumping is not due to dispersal limitations)	[84]Austin et al. 1984; [15]Le Lay et al. 2010; [16]Lin et al. 2014; [17]Aizpurua et al. 2015; [18]Chiffard et al. 2020

Method	Brief description	Pros	Cons	Suitable for which rarity categories?	References
	environmental predictors and extrapolating the model in space and time, e.g. adaptive niche-based sampling, Direct Gradient Analyses		- may work better for specialist species that are not too much dispersal limited (niche-based modelling)		

Table 2. How to sample?

Method	**Brief description**	**Pros**	**Cons**	**Suitable for which rarity categories?**	**References**
Standardized sampling	Sampling with commonly use methods following a standardized protocol (e.g. quadrats, transects, traps, etc.) without any adaptation to increase the probability of detecting rare species, e.g. biodiversity observatories	- detection of a large number of species - data comparable across locations - unbiased with respect to sampling effort	- rare species less likely to be detected when populations have low local density	Cat1, Cat2, Cat3	[19]Enquist et al. 2016; [20]Bruelheide et al. 2019; [21]Risely et al. 2010; [22]Jiguet et al. 2012

Method	Brief description	Pros	Cons	Suitable for which rarity categories?	References
Occupancy sampling	Sampling that consists of repeated sampling following a standardized protocol within a period during which the targeted species remain available for detection	- multi-species; allows estimating detection probability that can be used to obtain unbiased presence/absence data	- effort required is high unless detection probability is high - may require survey methods targeted to particular rare species, such as lures	All	[23]MacKenzie & Royle 2005; [24]MacKenzie et al. 2017
Distance sampling	Sampling that consists in recording the distance from the observer to the organism when detected. This information can then be used to adjust the sampling strategy	- multi-species	- requires expert knowledge (able to identify species at different distances within a given radius) - locally rare species will not provide sufficient observations for reliable estimates of abundance	Common species, Cat2	[25]Rosenstock et al. 2002; [26]Buckland et al. 2015

Method	Brief description	Pros	Cons	Suitable for which rarity categories?	References
	and to correct for detection probability in prediction models				
Species-targeted sampling (or species-specific sampling)	Sampling specifically designed for given locally rare species, based on fine information on the species' habits, to increase the encounter rate, e.g. traps with specific food items or pheromone baits	- highly efficient in detecting rare species of interest - fine resolution data	- intensive field work - cannot cover large spatial extent (but see promising methods such as detection dogs) - species-targeted	All	[27]Grimm & Klenke 2019; [28]Grimm et al. 2019

Method	**Brief description**	**Pros**	**Cons**	**Suitable for which rarity categories?**	**References**
Mark-Release-Recapture sampling	Sampling that consists in capturing, marking and releasing individuals of given species in order to keep track of their identity and be able to estimate capture rate and population parameters	- under particular assumptions, allows estimating population parameters, such as population size, fecundity, etc. - fine resolution data	- highly time-consuming and field-work intensive - cannot cover large spatial extents - species-targeted	Cat1, Cat2, Cat3	[29]Williams et al. 2002
Passive sampling	Sampling based on the setting up of devices that automatically record species passing within a certain radius, e.g. camera	- allows large-scale surveys - multi-species	- non-specific, detects any species as well as noise - costly in terms of resources (to buy devices, process data, etc.)	Cat3, Cat7 (+ Cat2, Cat6 if devices can be set anywhere)	[30]Schüttler et al. 2016 (camera trapping) [31]Jeliazkov et al. 2016 (acoustic sampling)

Method	Brief description	Pros	Cons	Suitable for which rarity categories?	References
	trapping, acoustic sampling				
eDNA	Sampling based on DNA extraction from the environment (e.g. water, soil, sediments, snow) coming from cells of organisms that are and/or were present at some point in the environment. Specific or unspecific primers can be used to amplify eDNA samples, depending on whether the	- rapid survey at large scales, cost-effective - species-targeted as well as multi-species assessments - high detection power - non-invasive method - no licence constraints for protected species - in some cases, can provide semi-quantitative estimation of abundances	- detectability depends on several parameters whose effects can be confounded with actual ecological responses, e.g. environmental conditions, such as UV light, temperature, and water flow, but also the activity and density of animals, their residence time, etc. - the importance of primer specificity	Cat1, Cat2, Cat3 (+Cat5, Cat7 if we consider that at low population density, habitat specificity may ensure higher eDNA concentrations than habitat unspecificity)	[32]Bohmann et al. 2014; [33]Rees et al. 2014; [34]Jerde et al. 2011; [35]Wilcox et al. 2013; [36]Beng & Corlett 2020

Method	Brief description	Pros	Cons	Suitable for which rarity categories?	References
	survey targets specific species or the whole community, respectively				

Table 3. How to model?

Method	Brief description	Pros	Cons	Suitable for which rarity categories?	Examples / references	Input data -> Output calculated/ estimate*

Method		**Brief description**	**Pros**	**Cons**	**Suitable for which rarity categories?**	**Examples / references**	**Input data -> Output calculated/ estimate***
Data processing	Data processing	Different processing strategies can be applied on data prior to actual modelling which allows making data more appropriate, more powerful, or more in line with the assumptions of subsequent modelling; e.g. combine opportunistic observations with atlas data, correct biases in presence-only data, data transformations (e.g. abundances into rank abundance curves)	- data-saving, allows using the maximum of information available	- often requires to take arbitrary decisions to select thresholds, correcting factors, etc.	All	[37]Fithian et al. 2015; [38]Phillips 2009 (correct biases in presence-only data); [39]Nekola et al. 2008 (data transformations)	PA -> PA ab -> ab

Method		**Brief description**	**Pros**	**Cons**	**Suitable for which rarity categories?**	**Examples / references**	**Input data -> Output calculated/ estimate***
Modelling methods commonly grouped under "SDMs"	Regular SDMs with absence data	SDMs with no particular correction effect nor sophistication when enough data are available and meet all modelling assumptions (rarely the case), e.g. GLM	- simple	- requires absence data - often too simplistic, resulting in strongly biased results - can suffer overfitting if the number of predictors is too high compared to too few species occurrences - assumes that habitat suitability is the most limiting driver of species distribution - doesn't control for sampling	Common species	[40]Guisan & Zimmermann 2000	PA -> relative pocc

Method		Brief description	Pros	Cons	Suitable for which rarity categories?	Examples / references	Input data -> Output calculated/ estimate*
	SDMs + pseudo-absences	SDMs where no absence data is unavailable. Models either attempt to generate absences where they believe the species to be absent (pseudo-absences) or sample environmental conditions available to the species (background points)	- simple - only requires readily-available presence data	- requires data and prior knowledge on habitat suitability - assumes that habitat suitability is the most limiting driver of species distribution	Common species	[41]Barbet-Massin et al. 2012	P (+background data) -> relative lik

Method		Brief description	Pros	Cons	Suitable for which rarity categories?	Examples / references	Input data -> Output calculated/ estimate*
	Bias-corrected SDMs	(Hierarchical) SDMs accounting for different, potential sources of biases due to spatial location, autocorrelation, observation effects, etc. Examples of models are mixed effect models with an observer random effect, models accounting for spatial auto-correlation, SDMs with model-based bias correction, zero-inflated models that allow modelling true and false absences separately	- accurate - particularly appropriate and flexible for rare species modelling - hypothesis-driven	- interpretation sometimes difficult - hypothesis-driven - requires information on observational conditions	All	[42]Dormann et al. 2007, [43]Marcer 2013 (models accounting for spatial auto-correlation); [37]Fithian et al. 2015 (mixed effect models with an observer random effect); [44]El-Gabbas & Dormann 2018 (SDMs with model-based bias correction); [45]Zuur et al. 2009 (zero-	P -> relative lik PA -> relative pocc ab+det -> relative ab

Method		**Brief description**	**Pros**	**Cons**	**Suitable for which rarity categories?**	**Examples / references**	**Input data -> Output calculated/ estimate***
	Multi-scale SDMs	Models incorporating distribution information at multiple grain sizes - information from distribution data at multiple grain sizes constrain fine-grain predictions - information on environmental conditions at multiple grain sizes used as inputs	- processes that operate at multiple spatial scales, and ones unrelated to environmental relationships, can be incorporated in to model predictions	- complicated fitting frameworks	Common species	[46]Keil et al. 2013 (hierarchical models incorporating distribution information at multiple grain sizes); [47]Rocchini et al. 2017	PA -> relative pocc P -> relative lik

Method		**Brief description**	**Pros**	**Cons**	**Suitable for which rarity categories?**	**Examples / references**	**Input data -> Output calculated/ estimate***
	Geographically-structured SDMs	SDM procedure that: 1) splits evaluation data based on spatial clustering of the data; 2) using modelling data (e.g. creation of pseudo-absence/ background data), incorporates spatial bias of presence data or taxonomic group	- can use most traditional SDM algorithms (only affects input data) - reduces the risk of overfitting data to spatial biases in sampling data	- assumes that habitat suitability is the most limiting driver of species distribution - can cause nearly all data to be assigned to 1-2 folds, and other folds being constructed with v. few occurrence points	Common species	[48]Radosavljevic & Anderson 2014; [38]Phillips et al. 2009	PA -> relative pocc P -> relative lik

Method		Brief description	Pros	Cons	Suitable for which rarity categories?	Examples / references	Input data -> Output calculated/ estimate*
	Spatial-thinning SDMs	SDM procedure that consists in removing spatially clustered occurrence points to reduce the spatial autocorrelation in input data	- can use most traditional SDM algorithms (only affects input data) - reduces the spatial autocorrelation in input data - reduces the risk of overfitting data to spatial biases in sampling data	- assumes that habitat suitability is the most limiting driver of species distribution - reduces quantity of modelling data	Common species	[49]Boria et al. 2014	PA -> relative pocc P -> relative lik

Method		**Brief description**	**Pros**	**Cons**	**Suitable for which rarity categories?**	**Examples / references**	**Input data -> Output calculated/ estimate***
Ensemble of multiple SDMs	Ensemble SDMs	Procedure that takes outputs from several algorithms of SDMs, weights these outputs based on respective model performances (using e.g. AIC) and generates single 'consensus' predictions by model averaging methods	- does not rely on single best model - ensemble predictions perform better compared to single modelling techniques - can use variance between models as estimate of uncertainty	- all the cons of SDM approaches above - model averaging also has limitations (e.g. sensitivity to performance score and thresholds used) - predictive performance still questioned	Common species	[50]Araújo & New 2007; [85]Hao et al. 2019; [86]2020	PA -> relative pocc P -> relative lik

Method		Brief description	Pros	Cons	Suitable for which rarity categories?	Examples / references	Input data -> Output calculated/ estimate*
	Ensemble of Small Models (ESM)	Strategy that consists in modelling the distribution of rare species based on fitting a larger number of small (bivariate, trivariate, etc.) models, that is models with only two predictors at a time (although only one or three could also be used), and averaging them in an ensemble prediction using weights based on model performances (e.g. based on AUC score).	- circumvents the risk of overfitting when applying an SDM on too few occurrences data - excellent performance on species data with low number of occurrences - allows structuring the modelling framework according to different scales of drivers of species distribution (e.g. local vs. climatic predictors)	- requires to choose thresholds of performance scores to decide which models are included in the ensemble - remains unclear how this method performs for the different forms of rarity, especially the spatially-biased ones, as it is mainly based on the number of occurrences and related IUCN status - ESM performance (compared to	Cat4, Cat6 (low density but spatially dispersed)	[51]Lomba 2010; [52]Breiner et al. 2015	P -> relative lik

Method		Brief description	Pros	Cons	Suitable for which rarity categories?	Examples / references	Input data -> Output calculated/ estimate*
Bayesian Belief Network SDMs	Bayesian Belief Network SDMs	(a.k.a. Bayesian networks, causal probability networks, acyclic directed graphs) Statistical tool derived from graph theory and Bayesian inference that predicts the probability of ecological responses to varying input assumptions such as habitat and population demography conditions and to hypothesized causal relationships.	- all the pros related to Bayesian statistical frameworks: flexibility, accounting and quantification of uncertainties, integration of prior knowledge information on the rare species of interest, easily updatable with new data / information, etc. - integration, assessment and visualization of causal pathways to explain	- requires to discretize input predictors with choices of thresholds which can lead to class edge effects (but see Aguilera et al. 2010) - more appropriate for risk or conservation category assessment than for predicting or mapping species distribution - assumptions and reasoning behind the hypothesized influence diagram	Potentially all (provided that enough prior knowledge and validation data are available)	[53,54]Marcot et al. 2006a,b; [55]Smith et al. 2007; [56]Aguilera et al. 2010; [57]Chen & Pollino 2012; [58]MacCracken et al. 2012; [59]Hamilton et al. 2015; [60]Van Echelpoel et al. 2015	P -> relative lik PA -> relative pocc ab -> relative ab

Method		Brief description	Pros	Cons	Suitable for which rarity categories?	Examples / references	Input data -> Output calculated/ estimate*
Occupancy downscaling modelling	Occupancy downscaling modelling	Models that describe the OAR* are fitted at large grain sizes to atlas data and then extrapolated to predict occupancy at fine grain sizes. *Occupancy-Area Relationship (OAR) (or scale-area curve or range-area relationship) (Harte & Kinzig, 1997; Kunin, 1998) is the relationship between the area occupied by a species and the sampling grain size. This relationship is positive and its shape is characteristic of the species distribution pattern (extent, patchiness, prevalence).	- by aggregating data at large scales, overcomes sampling gaps (false absences in atlas data) and effects of sampling biases - no need for covariates	- needs some atlas data - only determines occupancy in terms of proportion of sites or area occupied, i.e. not spatial-explicit - may be subject to some errors/uncertainty from the models - requires to think carefully about how to fit the upscaling functions - may not be possible to fit models for some species - e.g. very	Cat1, Cat2, Cat4, Cat5, Cat6	[61]Azaele et al. 2012; [62]Barwell et al. 2014; [63]Marsh et al. 2019	PA (atlas data) -> occupancy (as the proportion of sites or area occupied)

Method		Brief description	Pros	Cons	Suitable for which rarity categories?	Examples / references	Input data -> Output calculated/ estimate*
Modelling methods commonly grouped under "site-occupancy* models"	Mark-release-recapture* modelling (robust design)	HM* using mark-recapture histories to estimate population parameters (colonization, extinction, etc.), occurrence probability, and detectability. Requires to fulfil the population closure assumption between the temporal replicates and to have relatively good temporal replication (robust design). Can use covariates to estimate detectability and other potential biases.	- provides accurate estimations of population parameters (e.g. population size, survivorship, fecundity) - provides accurate estimations of detectability (e.g. trap happiness/shyness effects, time-varying capture, sex-dependent detectability) - thanks to the robust design principle, if one has multiple	- hypothesis-driven - computationally intensive	All, especially for Cat4, Cat5, Cat6, Cat7 (low local density) but for low local density, it may be challenging to get enough data for reliable estimates	[64]Pollock et al. 1990; [65]MacKenzie et al. 2002; [66]MacKenzie 2006; [67]Willson et al. 2011	PA+det -> pocc

Method		Brief description	Pros	Cons	Suitable for which rarity categories?	Examples / references	Input data -> Output calculated/ estimate*
	Multi-scale occupancy models	HM* site-occupancy model that allows estimation of occupancy at different spatial scales to account for different scales of habitat, environmental, ecological or sampling influences; e.g. local habitat vs. landscape-scale effects. The approach accounts for the lack of independence of detections within a sampling occasion and use this dependence to infer scale-specific occupancy, namely the study area scale and the site scale. This method is a variation of the classical site-occupancy model robust design, except that it does not model seasonal colonization and extinction, but simply	- accounts for the scale-dependence of occupancy estimation	- hypothesis-driven - requires good data with sufficient spatial-temporal replicates and detections	All, providing that sufficient spatial-temporal replicates are available	[68]Nichols et al. 2008; [69]Mordecai et al. 2011. [70]Pavlacky et al. 2012; [71]Hagen et al. 2016;	PA+det -> pocc

Method		**Brief description**	**Pros**	**Cons**	**Suitable for which rarity categories?**	**Examples / references**	**Input data -> Output calculated/ estimate***
N-mixture models	Royle-Nichols models (RN) or Bernoulli-Poisson N-mixture models (for occurrences)	HM* that estimate species occurrence probability using different submodels (and potentially different sets of predictors) for the "detection" and the "occurrence" processes. RN model provides the conceptual links between the N-mixture models for abundances and the classical site-occupancy* models. RN can estimate abundances from spatio-temporally replicated measurements of presences/absences, can accommodate detection heterogeneity when focusing on occupancy and can link occupancy and abundance data in an integrated model. Some people consider RN as	- provides two useful estimates : one for the detection probability and one for the occurrence probability	- requires a sufficient amount of spatio-temporal replications in the data - requires good sets of predictors for both the detection and the occurrence parts of the model	All, especially for Cat4, Cat5, Cat6, Cat7 (low local density)	[72]Royle & Nichols 2003; [73]Kéry & Royle 2015	PA+det -> pocc

Method		**Brief description**	**Pros**	**Cons**	**Suitable for which rarity categories?**	**Examples / references**	**Input data -> Output calculated/ estimate***
	N-mixture models for abundances	HM that estimate species abundances using different submodels (and potentially different sets of predictors) for the "detection" and the "abundance" processes. For instance, in "The N-mix" model, the detection probability can be estimated based on a binomial function of some predictors assumed as relevant to the detection process (e.g. vegetation density). This estimation is then incorporated in a (mixed) Poisson model that estimates species abundances (based on predictors relevant to the species ecology) while weighting by the imperfect detection (weighted likelihood). Examples of N-	- provides two useful estimates : one for the detectability and one for the relative abundances - provides fine estimation of species relative abundances - with a sufficient amount of data and in some circumstances, some of these models can be used relaxing the population closure assumption	- most of these models require good quality and large amount of abundance data with both spatial and temporal replications (except zero-inflated and hurdle models) - computationally intensive - requires good sets of predictors for both the detection and the abundance parts of the model	All, especially for Cat4, Cat5, Cat6, Cat7 (low local density)	[74]Welsh et al. 2000, [75]Martin et al. 2005, [76]Joseph et al. 2009 (zero-inflated N-mixture models); [77]Royle 2004, [78]Dénes et al. 2015 ("The N-mix" model); [73]Kéry & Royle 2015 (Poisson-binomial/Poisson-Poisson/multinomial/density models); [79]Cunningham	ab+det -> relative ab

Method		Brief description	Pros	Cons	Suitable for which rarity categories?	Examples / references	Input data -> Output calculated/ estimate*
Occupancy or abundance modelling with multiple detection methods	Occupancy or abundance modelling with multiple detection methods	HM that permits simultaneous use of data from multiple detection methods for inference about method-specific detection probabilities. The approach accounts for the lack of independence of detections within a sampling campaign and use this dependence to infer method-specific occupancy and detectability.	- can be used with data that are produced by different sampling methods and devices (provides device-specific detection probability estimates for use in survey design)	- if the species of interest is locally rare or solitary, and one of the detection devices is a method that retains (a trap) or repels (a camera's flash) an individual upon detection, then the model needs to be extended to include different device-specific detection probabilities that differ based on whether or not the species was detected by one of the other	All, especially for Cat4, Cat5, Cat6, Cat7 (low local density)	[68]Nichols et al. 2008; [82]Giraud et al. 2016; [83]Bowler et al. 2019	PA+det -> pocc ab+det -> relative ab

Method	Brief description	Pros	Cons	Suitable for which rarity categories?	Examples / references	Input data -> Output calculated/ estimate*

*P=presence only, PA=presence/absence, ab=abundance, pocc=probability of occurrence, det=detection probability, lik=likelihood

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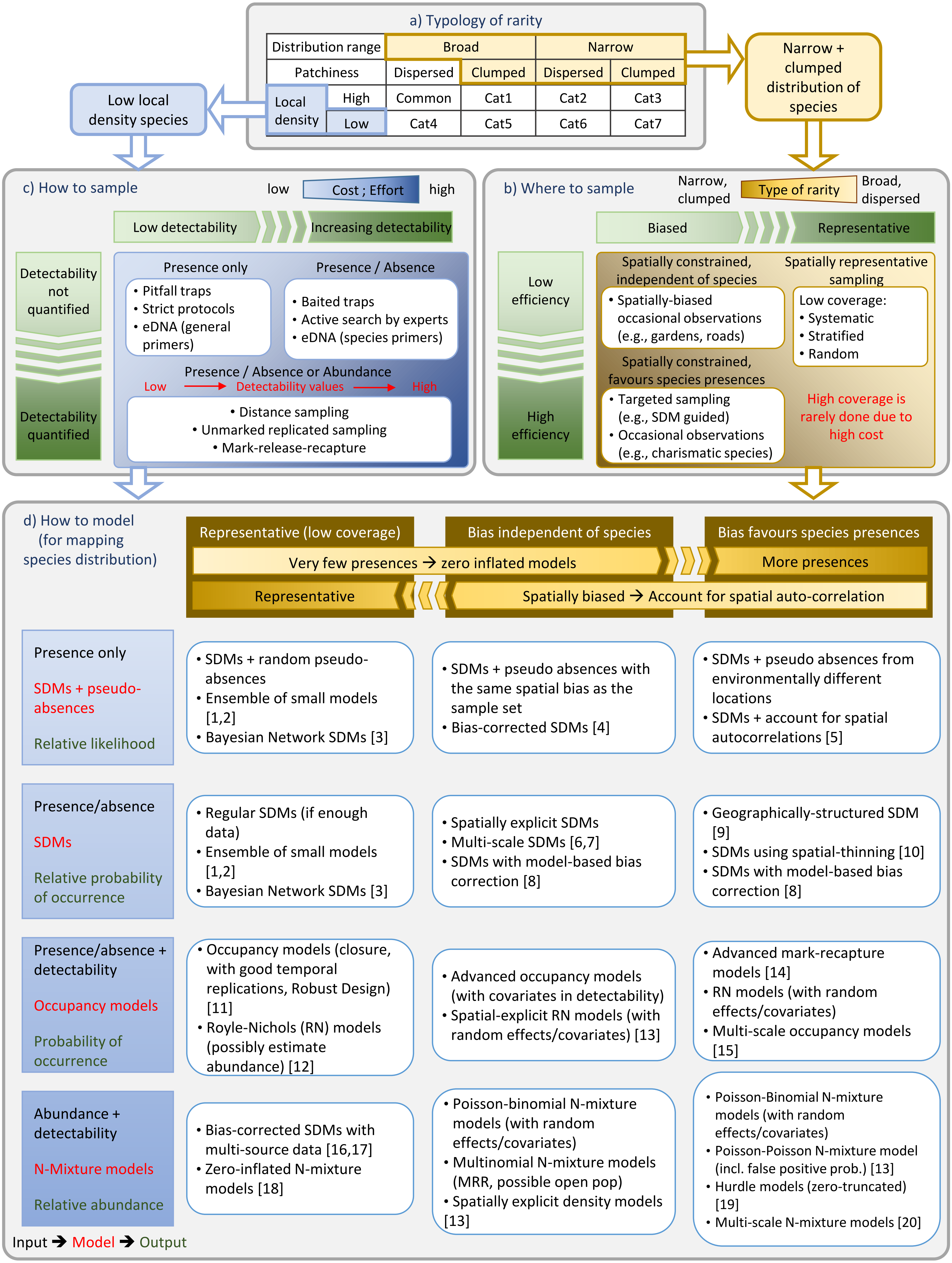

a) Typology of rarity

Distribution range		Broad		Narrow	
Patchiness		Dispersed	Clumped	Dispersed	Clumped
Local density	High	Common	Cat1	Cat2	Cat3
	Low	Cat4	Cat5	Cat6	Cat7

Low local density species

Narrow + clumped distribution of species

c) How to sample

low Cost ; Effort high

Low detectability → Increasing detectability

Detectability not quantified

Detectability quantified

Presence only

- Pitfall traps
- Strict protocols
- eDNA (general primers)

Presence / Absence

- Baited traps
- Active search by experts
- eDNA (species primers)

Presence / Absence or Abundance

Low → Detectability values → High

- Distance sampling
- Unmarked replicated sampling
- Mark-release-recapture

b) Where to sample

Narrow, clumped — Type of rarity — Broad, dispersed

Biased → Representative

Low efficiency

High efficiency

Spatially constrained, independent of species

- Spatially-biased occasional observations (e.g., gardens, roads)

Spatially constrained, favours species presences

- Targeted sampling (e.g., SDM guided)
- Occasional observations (e.g., charismatic species)

Spatially representative sampling

Low coverage:
- Systematic
- Stratified
- Random

High coverage is rarely done due to high cost

d) How to model (for mapping species distribution)

Very few presences → zero inflated models → More presences

Representative ← Spatially biased → Account for spatial auto-correlation

	Representative (low coverage)	Bias independent of species	Bias favours species presences
Presence only SDMs + pseudo-absences Relative likelihood	• SDMs + random pseudo-absences • Ensemble of small models [1,2] • Bayesian Network SDMs [3]	• SDMs + pseudo absences with the same spatial bias as the sample set • Bias-corrected SDMs [4]	• SDMs + pseudo absences from environmentally different locations • SDMs + account for spatial autocorrelations [5]
Presence/absence SDMs Relative probability of occurrence	• Regular SDMs (if enough data) • Ensemble of small models [1,2] • Bayesian Network SDMs [3]	• Spatially explicit SDMs • Multi-scale SDMs [6,7] • SDMs with model-based bias correction [8]	• Geographically-structured SDM [9] • SDMs using spatial-thinning [10] • SDMs with model-based bias correction [8]
Presence/absence + detectability Occupancy models Probability of occurrence	• Occupancy models (closure, with good temporal replications, Robust Design) [11] • Royle-Nichols (RN) models (possibly estimate abundance) [12]	• Advanced occupancy models (with covariates in detectability) • Spatial-explicit RN models (with random effects/covariates) [13]	• Advanced mark-recapture models [14] • RN models (with random effects/covariates) • Multi-scale occupancy models [15]
Abundance + detectability N-Mixture models Relative abundance	• Bias-corrected SDMs with multi-source data [16,17] • Zero-inflated N-mixture models [18]	• Poisson-binomial N-mixture models (with random effects/covariates) • Multinomial N-mixture models (MRR, possible open pop) • Spatially explicit density models [13]	• Poisson-Binomial N-mixture models (with random effects/covariates) • Poisson-Poisson N-mixture model (incl. false positive prob.) [13] • Hurdle models (zero-truncated) [19] • Multi-scale N-mixture models [20]

Input ➔ Model ➔ Output