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1 Long-term thermal imbalance in large borehole heat
2 exchangers array - A numerical study based on the
3 Leicester project

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13 **Abstract**

When a Borehole Heat Exchanger (BHE) array is coupled with heat pump to provide cooling and heating to the buildings, thermal interaction between BHEs may occur in the subsurface. In the long term, imbalanced seasonal thermal load may lead to low or high temperature zones accumulating in the centre of the array. In this study, numerical models are configured according to a real BHE array project in Leicester, UK, and verified against monitoring data. Based on this reference model, a series of numerical experiments are conducted to investigate the response of circulation fluid temperature to different settings of imbalanced thermal load. It is found that over long-term operation, the sub array with a larger number of installed BHEs is shifting its thermal load towards the other branch with less BHEs installed. Within each sub array, the heat injection rate on the central BHEs is gradually shifted towards those located at the edge. A linear correlation is also found between the working fluid temperature increment and the amount of the accumulated heat injected into the subsurface.

14 *Keywords:* Shallow geothermal energy utilisation, Building heating and
15 cooling, Borehole Heat Exchanger (BHE) array, Ground source heat pump,
16 OpenGeoSys (OGS), Thermal Engineering System in Python (TESPy)

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18 **Nomenclature**

19 **Roman letters**

20 b wall thickness of pipe installed in the BHE (m)

21 c specific heat capacity ($\text{J kg}^{-1} \text{K}^{-1}$)

22 D diameter of the BHE (m)

23 d diameter of the pipe installed in the BHE (m)

24 k_s roughness coefficient of the pipe (m)

25 L length of the BHE (m)

26 l length of the pipe (m)

27 \dot{m} flow rate of the circulating fluid (kg s^{-1})

28 p hydraulic pressure of the circulating fluid (bar)

29 \dot{Q} heat extraction rate on the BHE (W)

30 Q amount of heat (MWh)

31 Re Reynolds number (–)

32 S adjacent distance between BHEs (m)

33 T temperature ($^{\circ}\text{C}$)

34 t time (–)

35 T_p penalty temperature ($^{\circ}\text{C}$)

36 V volume of the BHE array (m^3)

37 v flow velocity in pipelines (m s^{-1})

38 **Greek Letters**

39 η dynamic viscosity of circulating fluid (Pa s)

40 λ thermal conductivity ($\text{W m}^{-1} \text{K}^{-1}$)

41 π mathematical constant Pi (–)

42 ρ density (kg m^{-3})
43 ζ Darcy friction factor as used in Eq. (1) (–)

44 **Operators**

45 Δ difference operator
46 \int integral operator
47 Σ summation operator

48 **Subscripts**

49 f fluid
50 g grout
51 i index of BHE as used in Eq. (4)
52 in inlet pipe
53 ini initial time
54 out outlet pipe
55 p pipe
56 s solid or soil

57 **Abbreviations**

58 1U single U-shape pipe
59 BHE borehole heat exchanger
60 COP coefficient of performance
61 GSHP ground source heat pump
62 PSTL proportion of the shifted thermal load (%)

63 1. Introduction

64 Geothermal heat, due to its wide availability, has been considered as a re-
65 newable and sustainable energy source for building cooling and heating [1, 2].
66 Shallow geothermal exploitation is even favourable in urban areas, because
67 the accelerated heat fluxes from the warm basement often lead to elevated
68 temperatures in the subsurface [3, 4]. In modern building projects, a com-
69 mon practice is to install dozens of Borehole Heat Exchangers (BHE) prior
70 to the building construction and then connect them through a pipe network
71 to form a BHE array. This array is later connected with heat pumps to
72 extract or inject thermal energy out of or into the shallow subsurface [5, 6].
73 A recent trend in the industry is to build large BHE arrays with hundreds
74 or sometimes thousands of BHEs to meet the high demand from commercial
75 buildings and residential neighbourhood [7].

76 Despite of minor differences, most countries follow the same design proce-
77 dure for large BHE array as the guideline recommended by the American So-
78 ciety of Heating, Refrigerating and Air-Conditioning Engineers (ASHRAE) [8].
79 It is based on the well known line source method originally developed by
80 Carslaw and Jaeger [9] and later promoted by Ingersoll and Zobel [10]. First,
81 the thermal load of the building is quantified. This load is divided into
82 three successive pulses, i.e. the peak load, the monthly average load, and
83 the annual average load (in kW). When the heating and cooling load is in
84 equilibrium, the total length of all BHEs are then calculated based on the
85 short-term peak load and the effective thermal resistance of the ground. In
86 the second step, the total length is equally divided based on the depth of
87 each BHE, so that the number of BHEs to be installed on site can be de-
88 termined accordingly. If the heating and cooling load is not balanced, then
89 the penalty temperature T_p and the total BHE length will be calculated in
90 an iterative manner. Based on the ASHRAE procedure, several alternative
91 methods have been developed in recent years, to improve the calculation
92 of T_p in particular [11, 12]. Ahmadfard and Bernier [13] have presented a
93 comprehensive review on the available BHE array designing procedures. In
94 both the original ASHRAE guideline and all the extended procedures, the
95 minimum borehole separation distance S is always defined as an empirical
96 parameter to reduce thermal interference between individual boreholes, and
97 it is also used in the calculation of penalty temperature T_p (cf. Chapter 35.1
98 in [8]).

99 When looking into different countries, the regulation on this minimum
100 distance S is not exactly the same. The ASHRAE guideline in United States
101 fix the S value at 6 m [8]. Switzerland requires a minimum distance of 5 m

102 (cf. Miglani et al. [14]). In Germany, this value has been increased from
103 5 m to 6 m in the 2019 updated VID guideline [15, 16]. In China, a distance
104 between 3 m to 6 m is recommended [17]. In Sweden, a much larger distance
105 of 20 m is enforced (cf. Haehnlein et al. [18]). Due to the fact that differ-
106 ent countries have varying climate conditions and initial soil temperatures,
107 this minimum distance S value remains a parameter that is empirically de-
108 termined. Another issue in the ASHRAE and other guidelines is that the
109 specific heat extraction rate is assumed to distribute equally on each BHE
110 and spread evenly along the entire borehole length. This assumption holds
111 true under the ideal condition where no thermal interference exists among
112 BHEs. However, during the long-term operation, thermal interaction is dif-
113 ficult to avoid and it often varies in space and also over time. Details about
114 this shifted thermal load behaviour could be found in our previous work
115 (Chen et al. [19]) through numerical simulation, or from the work of You
116 et al. [20] through an analytical analysis. Furthermore, if the BHEs are
117 connected in a sequential manner, it is not possible to have identical heat
118 extraction rate on each borehole [21].

119 In most BHE array projects, the annual cooling and heating load is often
120 not fully balanced. This means thermal plumes can form and accumulate in
121 the subsurface, causing the working fluid temperature to gradually increase
122 or decrease over time. In extreme cases, this may lead to freezing in the
123 vicinity of the BHE or causing the failure of the heat pump [22, 23, 24].
124 Instead of the adjacent distance S and penalty temperature T_p , the size of
125 a BHE array is more constrained by the outflow temperature of the circula-
126 tion fluid. In cooling applications, this temperature normally should not
127 exceed 35 °C, otherwise the heat pump will not be working efficiently. When
128 operated in heating mode, the circulation temperature has to be kept above
129 0 °C [13], in order to mechanically protect the heat pump and avoid ground
130 freezing. As mentioned above, engineers who are designing the BHE array
131 would like to have a calculation procedure, in which the change of circula-
132 tion fluid temperature can be accurately estimated. In order to do that, a
133 scientific question has to be answered first, i.e. how will the circulation fluid
134 temperature change in response to the imbalanced thermal load, when the
135 thermal interaction in a BHE array can not be avoided?

136 One obstacle preventing the exploration of the above scientific question is
137 the lack of monitoring data. In order to fully capture the system behaviour,
138 both the annual amount of imbalanced heat imposed on the BHE array and
139 the responding ground loop temperature have to be quantified. This means,
140 sensors and flow meters have to be installed on the inlets and outlets of
141 the building loop, the heat pumps, and also different branches of the ground

142 loops. Continuous monitoring has to be conducted for several years, in order
143 to catch the trend in circulation fluid temperature. Fortunately, Naicker et
144 al. [25] has recently carried out such an intensive monitoring campaign and
145 made the data available to the general public. Their BHE array project
146 is located in Leicester, UK (hereafter as Leicester Project). The building
147 thermal load, heat pump operation, and also ground loop temperatures have
148 been monitored for over 3 years with minute-wise data readings. Detailed
149 introduction of the project is available in Naicker’s PhD thesis [26], as well
150 as in his following publications [27, 25]. Interested readers may also access
151 the monitoring data set from the Research Data Archive at the University
152 of Leeds [28].

153 In this study, we investigate the BHE array behaviour under imbalanced
154 annual thermal load by conducting a series of numerical experiments based
155 on the Leicester project monitoring data. In Sec 2, the mathematical back-
156 ground of the numerical model is introduced. In Sec 3, the numerical model
157 is set up based on the Leicester project and validated against the moni-
158 tored data set. Analysis on the modelling results reveals the thermal imbal-
159 ance and thermal interaction among BHEs. In Sec 4, a series of extended
160 numerical experiments are designed and simulated, aiming to investigate
161 the relationship between the circulation fluid temperature change and the
162 amount of imbalanced thermal load. Since the form and accumulation of
163 thermal plume is a critical issue for the long-term operation of a BHE array,
164 the amount of stored thermal energy in the subsurface has been carefully
165 analysed and quantified. Discussions (Sec 5) are also given on the potential
166 implications of our findings.

167 2. Method

168 As discussed in our previous work [19], most analytical approaches have
169 difficulties in quantifying the thermal interaction in large BHE arrays. In
170 comparison, numerical models offer more flexibility, by considering different
171 boundary conditions, thermal recharge from the ground surface, groundwa-
172 ter flow and also the geothermal gradient effects [29, 30, 31, 32, 33]. For
173 the large BHE array considered in this work, a pipeline network is always
174 present, coupling the BHEs and the heat pump. The thermal behaviour
175 on each BHE will be affected by this network over the long-term opera-
176 tion. Recently, we have presented the OpenGeoSys (OGS) model that takes
177 the above-mentioned factors into account ([19]). In the HeatTransportBHE
178 module of the OGS software, the variation of BHE outlet temperature and
179 surrounding soil temperature field can be simulated by the dual-continuum

180 approach. In the finite element mesh, the BHE is considered as line ele-
181 ments, while the surrounding soil is represented by prisms. The heat fluxes
182 between BHE wall and the surrounding subsurface are quantified by the
183 coupling term. Readers who are interested in this numerical scheme may
184 refer to Al-Khoury et al. [34] and Diersch et al. [35, 36] for more detailed
185 explanation.

186 For the coupling of a pipeline network, the open-source simulator Ther-
187 mal Engineering Systems in Python (TESPy) is introduced. Developed by
188 Witte [37], TESPy is capable of simulating a pipe network with both the
189 thermal and hydraulic balance equations. The nonlinear feature of the cou-
190 pled equations require the Newton-Raphson iteration, in order to solve for
191 pressure, mass flow and fluid enthalpy at each conjunction point. In OGS,
192 the Python interface library pybind11 is embedded and used for the commu-
193 nication between OGS and TESPy. In this study, the OpenGeoSys version
194 6.2.2 and the TESPy version 0.2.0 is used accordingly. For more informa-
195 tion on the coupling between OGS and TESPy, please refer to Chen et al.
196 [19], and also the online documentation [38], in which detailed tutorials are
197 available to the general public.

198 **3. Modelling Leicester Project**

199 *3.1. Project description*

200 In the Leicester Project [25], a large BHE array was installed. It is se-
201 lected in this work as the reference to validate our numerical model. This
202 system is configured to provide both heating and cooling to the Hugh Aston
203 building with a total floor area of 16,467 m². The designed peak cooling
204 capacity of this project is 360 kW through the Fan Coil Unit (FCU) and Air
205 Handling Unit (AHU). The corresponding peak heating capacity is 330 kW
206 through a underfloor heating system. The source side is equipped with 56
207 borehole heat exchangers, each of which has a depth of 100 m and a diameter
208 of 125 mm. In the basement of the building, there are four water-to-water
209 heat pumps which are all reversible for both cooling and heating application.
210 A single variable speed circulation pump is installed for the ground loop, so
211 that it is able to adjust the flow rate according to the operation condition
212 of the heat pumps. Before construction, a thermal response test (TRT)
213 was carried out on site and the result was evaluated based on the conven-
214 tional line-source model. The geotechnical characteristics, including initial
215 ground temperature, thermal conductivity and volumetric heat capacity of
216 the subsurface were determined by the TRT. All detailed parameters and
217 array layout could be found in Table 1 and Fig. 1, respectively.

218 *3.2. Model setup*

219 A comprehensive 3D numerical model (Fig. 1(a)), which comprises a
220 BHE array, the surrounding subsurface, and a coupled pipeline network, is
221 established according to the design of Leicester project described above [25].
222 The model domain is shown in the left part of Fig. 1(a). The subsurface
223 domain around the BHE array has a size of $280 \times 220 \times 151$ m. In it, the soil
224 part is discretized with prism elements, while the BHEs are represented by
225 lines. In total, the mesh contains 69,275 nodes and 130,128 elements. The
226 56 BHEs are placed in the centre of the domain according to their real-world
227 location. Each BHE has a single U-shape pipe (1U type) installed in it. The
228 BHE top is set at a depth of 1 m from the surface. The arrangement of the
229 array is illustrated in Fig. 1(b), which is in consistence with the original
230 planning. Most of the BHEs have a distance of 5 m to its adjacent ones.
231 However, BHE #11 is only 2 m away from its closest neighbour, exactly
232 following its coordinates reported in Naicker et al. [25].

233 According to the ground loop configuration, a simplified closed-loop
234 pipeline network is configured in the TESPpy software (see the right part
235 of Fig. 1(a)). Pre-defined components in the network are borehole heat ex-
236 changers (BHEs), water pump and heat pumps. Since in this study only
237 the working condition on the ground side is investigated, the measured and
238 reported ground loop thermal load in Leicester project is directly imposed as
239 the thermal boundary condition in the BHE array model. The black lines in
240 the network denote to the connection pipes between the components. And
241 the arrows indicates the flow direction of the circulating fluid. After lifted
242 by the water pump, the circulating fluid flows into the array with 56 paral-
243 lelly connected BHEs. As shown in Fig. 1(b) the entire array is divided into
244 two parts, which is achieved by adding two sub-splitter and merge compo-
245 nents in the network (see Fig. 1(a) right). After circulating through each
246 sub-array, the outflows are mixed at the merging point and then flow back
247 to the heat pump, where the heat is either extracted to or injected based on
248 the load profile from the building side. The physical configuration of each
249 BHE pipe in the TESPpy network are assigned with the same parameters as
250 those used in the OGS model. They are listed in Table 1 for reference.

251 Since there is no detailed information for the connection pipes on the
252 ground side from the report of Leicester project, we have configured the
253 model in a way that only the hydraulic and heat loss within the U-pipe in
254 the BHEs are considered, while those loss along the connecting pipes are
255 assumed to be negligible.

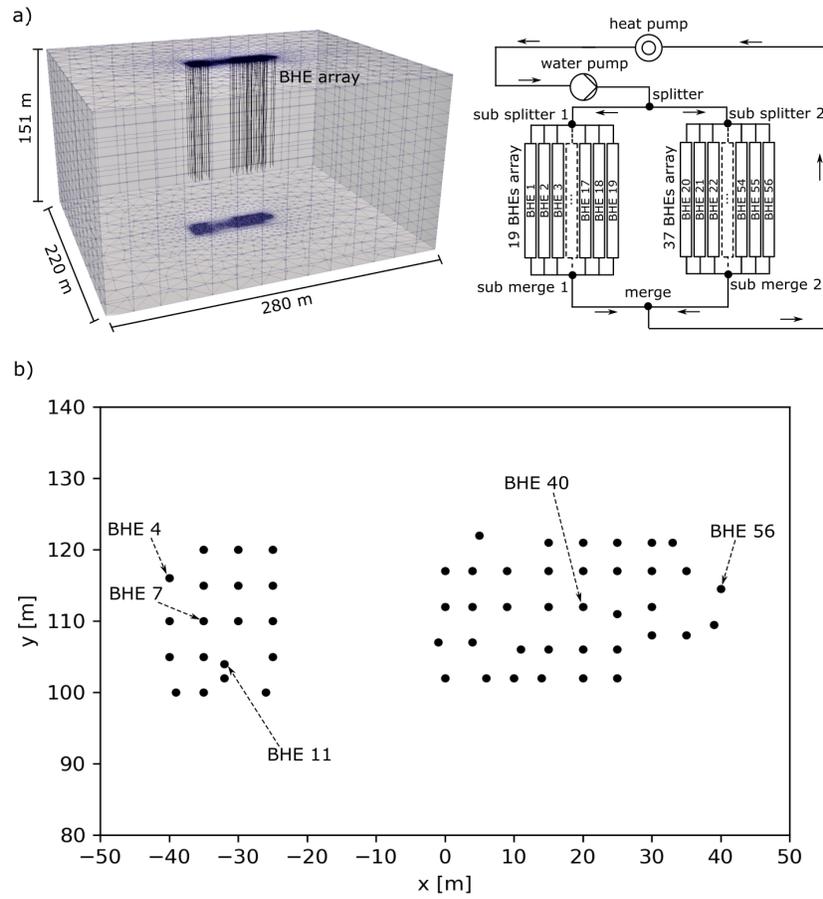


Figure 1: (a) Left: 3D model domain representing the Leicester project in OGS; Right: 56 BHEs pipeline network model; (b) Arrangement of 56 BHE array.

Table 1: Model parameters

Parameter	Symbol	Value	Unit
Initial soil temperature	T_{ini}	11.7	$^{\circ}\text{C}$
Soil thermal conductivity	λ_s	3.4	$\text{W m}^{-1} \text{K}^{-1}$
Soil heat capacity	$(\rho c)_s$	2576	$\text{kJ m}^3 \text{K}^{-1}$
Length of the BHE	L	100	m
Diameter of the BHE	D	0.125	m
Pipe inner diameter	d_p	0.026	m
Wall thickness of pipe	b_p	0.003	m
Wall thermal conductivity of pipe	λ_p	0.4	$\text{W m}^{-1} \text{K}^{-1}$
Grout thermal conductivity	λ_g	0.656	$\text{W m}^{-1} \text{K}^{-1}$
Grout heat capacity	$(\rho c)_g$	2700	$\text{kJ m}^3 \text{K}^{-1}$
Circulating fluid density	ρ_f	1020	kg m^{-3}
Circulating fluid heat capacity	$(\rho c)_f$	3962	$\text{kJ m}^3 \text{K}^{-1}$
Circulating fluid thermal conductivity	λ_f	0.485	$\text{W m}^{-1} \text{K}^{-1}$
Circulating fluid dynamic viscosity	η	0.0024	Pas
Length of the pipe for BHEs in the network	l	200	m
Diameter of the pipe for BHEs in the network	d_p	0.026	m
Pipe Roughness coefficient for pipes in the network	k_s	0.00001	m

256 *3.3. Initial and boundary conditions*

257 **Subsurface Part**

258 Initially, the soil temperature is set to 11.7 °C in the whole model domain. A
 259 Dirichlet-type boundary condition is assigned on the surface of the domain
 260 with a ground surface temperature curve, which follows the corresponding
 261 measured daily mean air temperature in Naicker et al. [25]. The lowest
 262 air temperature reaches −5 °C in the winter and the peak temperature in
 263 summer is about 24 °C.

264 **BHE Array Part**

265 In TESP_y, the Darcy-Weisbach equation (Eq. (1)) is adopted to quantify
 266 the hydraulic head loss caused by the friction in the U-pipe within the BHE.

$$\begin{aligned}
 p_{in} - p_{out} &= \frac{\rho_f}{2} \cdot v^2 \cdot \frac{\zeta(\text{Re}, k_s, d_p) \cdot l}{d_p} \\
 &= \frac{8 \cdot \dot{m}_{in}^2 \cdot l \cdot \zeta(\text{Re}, k_s, d_p)}{\rho_f \cdot \pi^2 \cdot d_p^5}.
 \end{aligned}
 \tag{1}$$

267 where the calculating flow velocity v is deduced through the pipe’s di-
 268 mensions, the fluid’s density and mass flow rate \dot{m} in TESP_y. The fluid’s
 269 density ρ depends on pressure and enthalpy. The Reynolds number Re is a
 270 function of pressure, enthalpy and flow rate.

271 At each time step, the measured inflow temperature and flow rate (Eq. 2)
 272 are assigned as the boundary conditions for the simulation in TESP_y. In
 273 the Leicester project, the measured inflow temperature and flow rate are
 274 given by every minute. These measured values can not be directly imposed
 275 in the numerical model, as the time step size is fixed to be 1 hour (see our
 276 description in the following section). To resolve this discrepancy, minute-
 277 wise monitoring data is aggregated. First, those noise readings, the values
 278 of which are way beyond a reasonable range, are removed. The data set,
 279 containing ca. 1.02 million entries altogether, are aggregated to an averaged
 280 value per hour. The average is achieved by calculating the weighted mean
 281 of the measured inflow temperature values,

$$T_{aver} = \frac{\sum_{i=1}^{60} T_i \dot{m}_i}{\sum_{i=1}^{60} \dot{m}_i},
 \tag{2}$$

282 where T_i and \dot{m}_i are the measured inflow temperature and flow rate at each
 283 measurement interval ($\Delta T = 1 \text{ min}$). At the same time, the average flow

284 rate is calculated by the arithmetic mean of the measured values.

285 As mentioned in Sec 3.2, since the time step size in this model is set to 1
286 hour, the model is not capable of predicting short-term behaviour of the BHE
287 array. However, despite of more than 130,128 mesh elements and a total
288 of 17,237 time steps, it is possible to complete the two-year long validation
289 simulation (cf. Sec 3.4) within 129 hours using a small workstation equipped
290 with a 3.40 GHz CPU and 16 GB of memory.

291 3.4. Model validation

292 To validate the OGS-TESPy numerical model, the two years long op-
293 eration phase of BHE array is simulated with the aforementioned config-
294 urations. The simulated outflow temperature, as well as the amount of
295 exchanged heat, is compared with the corresponding measurements and pre-
296 sented in Fig 2. The exchanged amount of heat in each month is estimated
297 using the following equation,

$$Q = \int c_f \dot{m} (T_{in} - T_{out}) dt, \quad (3)$$

298

299 where c_f is the specific heat capacity of the circulating fluid. As men-
300 tioned in Sec 3.1, although the measured inflow temperature has been ag-
301 gregated in order to be used as the model input, the simulation predicted
302 outflow temperature evolution still fits the monitored values very well. As
303 stated in [25], a modest year-by-year increase in the outflow temperature
304 is observed between the first and second year. This phenomena can also
305 be seen in our modelling results. Moreover, both the calculated and mea-
306 sured amount of heat have a consistent tendency in the temporary evolu-
307 tion, which corresponds well to the evolution of the outflow temperature.
308 The slight discrepancies between the measured and computed amount of
309 heat in some months, e.g. in the 15-th, 16-th, 20-th and 21-st month, are
310 most likely caused by the averaging of the measured inflow temperature val-
311 ues. Quantitatively speaking, the accumulated amount of heat injected in
312 the simulation (using the processed data) is about 3.2% higher than in the
313 original data measured data.

314 3.5. Analysis of the Model Predictions

315 3.5.1. Subsurface Thermal Imbalance

316 Through the two-year long operation of Leicester project, the subsurface
317 part was dominated by heat injection process, which can lead to thermal ac-
318 cumulation especially in the centre field of the BHE array. In Fig. 3, the

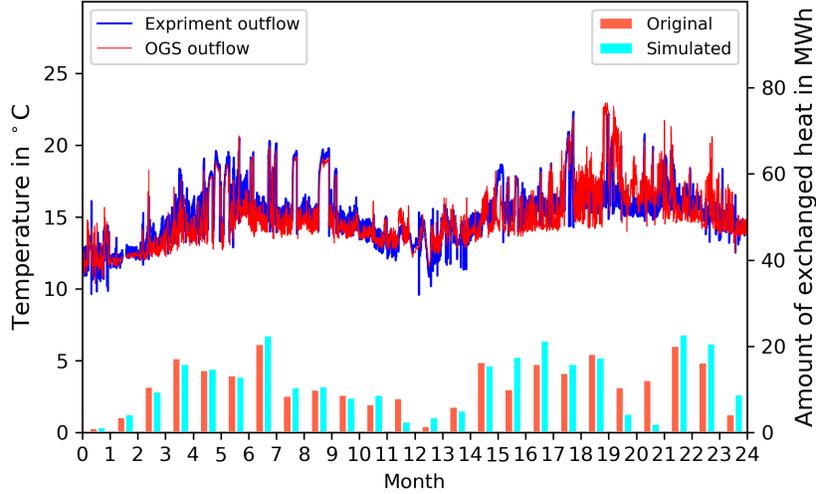


Figure 2: Comparison of the numerical result for the the evolution of the outflow temperature over 2 years with the original data.

319 computed soil temperature distribution after 2 years of operation is illus-
 320 trated. Our suspicion is confirmed by the model prediction, as the elevated
 321 temperature in the centre area of the array can be clearly recognised. In
 322 Fig. 3 lower figure, the maximum temperature increment in the centre is
 323 about 2.6°C . Obviously, the thermal accumulation in the right array is
 324 more intensive than that in the left array, as the former part has more
 325 BHEs installed than the latter one.

326 To investigate the temporal evolution of the soil temperature over time,
 327 five points (#P4, #P7, #P11, #P40 and #P56) (Fig. 3) are selected. They
 328 are located at a depth of $z = -51$ m, and 1 m away from their closest BHEs
 329 (BHE #4, #7, #11, #40 and #56 in Fig. 1(b) accordingly).

330 Fig. 4 illustrates the soil temperature at all five points at the end of each
 331 month over 2 years' operation. Compared to the temperature evolution
 332 at points #P4 and #P56, the temperature increase at #P7 and #P40 is
 333 more intensive. This indicates that the thermal accumulation effects are
 334 concentrated in the centre of each array, where #P7 and #P40 are located.
 335 After 2 years' operation, a 1°C temperature difference is predicted between
 336 #P4 and #P7 in the left array, while a greater difference of 1.3°C is found
 337 between #P40 and #P56 in the right array. Meanwhile, #P40, which is

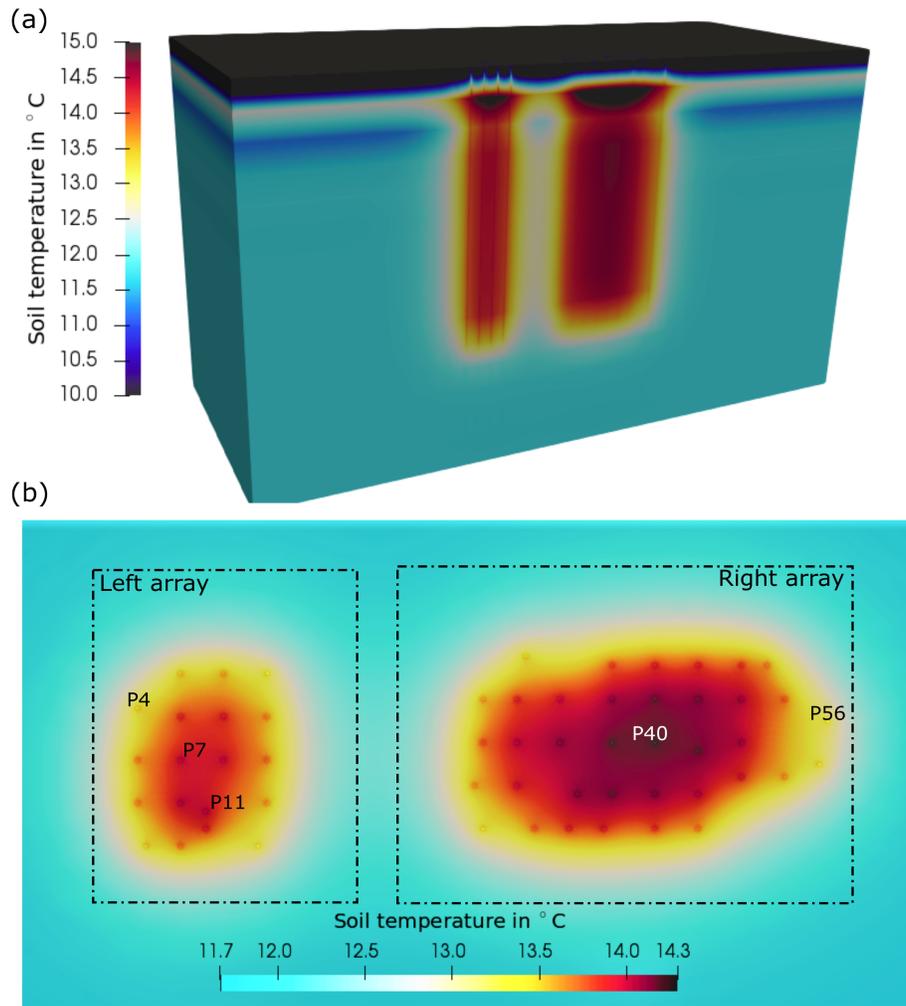


Figure 3: (a): Vertical cross-section of the 3D soil temperature distribution in the middle of the array after 2 years; (b): Horizontal view of temperature distribution at a depth of -51 m .

338 located in the centre of the right sub-array, is predicted to have a slightly
 339 higher temperature of 0.3°C than that at #P7, which locates in the left sub-
 340 array. This strong variation at #P40 could have resulted from the influences
 341 of BHEs from both sub-arrays sides. It can be seen from the upper part of
 342 Fig. 3 that thermal accumulation does happen between the left and right
 343 arrays. Overall, the modelling result indicates that the array with more
 344 BHEs could produce more intensive imbalance in the underground. Among
 345 the five points, the strongest temperature variation is found at #P11. It
 346 increases more intensively during the first 6 months since it is affected by two
 347 nearby BHEs at the same time. To sum up, the soil temperature is not solely
 348 affected by the nearby BHEs. Further, the accumulative thermal process in
 349 a BHE array could have strong influence on the temperature distribution as
 350 well in the long term.

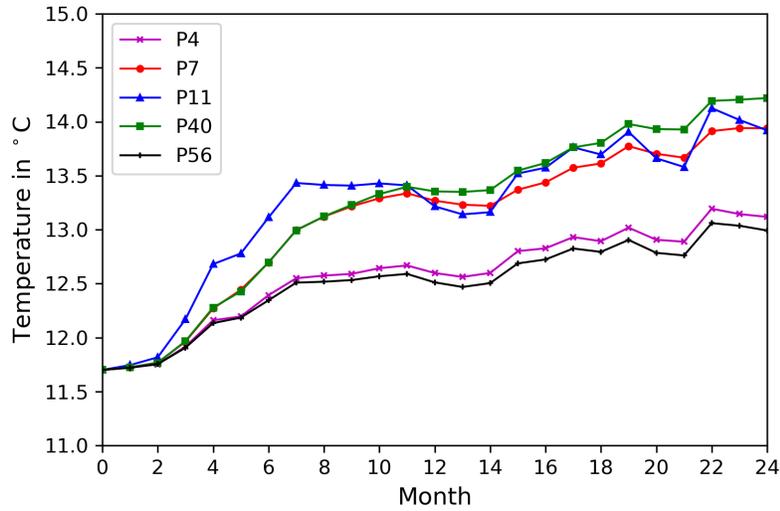


Figure 4: Evolution of the soil temperature on the selected points in the end of each month over 2 years.

351 *3.5.2. Load shifting behaviour*

352 As stated in our previous work (Chen et al. [19]), the interactions among
 353 the BHEs during long-term system operation can lead to load shifting in the
 354 BHE field. The monitoring data obtained from Leicester project provides an
 355 excellent opportunity for us to further investigate the trend of load shifting

356 under realistic conditions. The heat injection rate at four represent BHEs,
 357 i.e. BHE #4, #7, #40 and #56 is quantified based on the simulated inflow
 358 and outflow temperature on each BHE. In Fig. 5, the percentage of the
 359 shifted thermal injection rate (hereafter as PSTL) on BHE is calculated by

$$\text{PSTL}_i = \frac{\dot{Q}_i - \dot{Q}_{mean}}{\dot{Q}_{mean}} \times 100, \quad (4)$$

360 where i refers to the index of the BHE. \dot{Q}_i and \dot{Q}_{mean} are the heat injection
 361 rate at i -th BHE and the mean heat injection rate, respectively.

362 In Fig. 5(a), a general trend can be observed that the thermal load is
 363 gradually shifted away from the centre to the outer edge of the array. The
 364 heat injection rates on the centre BHEs (#7 and #40) are lower than the
 365 designed average value (PSTL < 0), while they become higher than the
 366 mean value (PSTL > 0) at the edge BHEs (#4 and #56). The reason
 367 behind is that the soil temperature in the centre part is generally higher
 368 than that in the outer area (cf. Fig. 3). Moreover, the thermal shifting is
 369 found to be stronger in the right sub-array (BHE #56 and #40) than in
 370 the left part, as more BHEs are installed in the right area. In Fig. 2(a),
 371 the most intensive shifting (PSTL value of 60.7%) is found in the 12-th
 372 month of the first year, where the system has the lowest thermal demand.
 373 This phenomena is consistent with the observations reported in our previous
 374 work [19].

375 In Fig. 5(b), the load shifting phenomenon between the left and right sub-
 376 array is further investigated. If there is no thermal interaction, each BHE
 377 should deliver same amount of heat, as they are connected in a parallel
 378 manner. Following this assumption, the rate of extracted heat from the
 379 left or right sub-array should be according to the corresponding number of
 380 installed BHEs, i.e. following a ratio of 19 : 37. Using this proportion as
 381 a reference, the amount of shifted heat ΔQ of the left or right sub-array
 382 can be quantified by first integrating the amount of extracted heat on each
 383 BHE, and then comparing it with the reference value. In Fig. 5(b), the
 384 monthly change of ΔQ and its corresponding percentage of deviation PSTL
 385 is depicted for each sub-array. It can be found that, after 4 months of heat
 386 injection, the heat extraction rate shifts gradually from the right towards
 387 the left array. The reason behind is the soil temperature difference in the
 388 left and right part during the system operation. As shown in Fig. 3(b), a
 389 higher soil temperature can be found in the right array after 2 years. This
 390 is mainly caused by the more number of BHEs on the right side. As the
 391 inflow temperature is kept consistent by the pipe network for all BHEs, the

392 actual heat injection rate on each BHE is dependent on the temperature
393 difference in comparison to the surrounding soil. By comparing the actual
394 simulated value with the design reference, the shifting phenomenon is well
395 observable. With regard to the shifted percentage, the maximum value is
396 found to be about 8.6% in the left sub-array and it is observed in the 12-th
397 month. This is in good agreement with the result shown in the Fig. 5(a).
398 The amount of heat shifted away from the right array is fully transferred to
399 the left part. Therefore, due to the fact the original designed load on the left
400 is only about half (19 : 37) of that on the right, the percentage of elevated
401 extraction rates on the left is about twice as much as that on the right side.

402 Fig. 5(c) shows the performance of two BHEs, i.e. BHE #40 and #56 at
403 two selected moments. At time $t_1 = 17,007$ hour, the system is dominated
404 by heat injection, while at $t_2 = 17,011$ hour heat extraction is the main
405 process. BHE #40 is located at the centre of the right sub-array, while
406 BHE #56 is at the edge. At t_1 , the heat injection rate of BHE #40 drops
407 by about 39%, while it increases by about 43% on BHE #56. In the heat
408 extraction dominated period (t_2), the corresponding values at BHE #40
409 and #56 are switched to +56% and -62%, respectively. It indicates that in
410 the long-term operation of a BHE array, when both heating and cooling are
411 applied, the thermal recharge of the subsurface can partially mitigate the
412 shifting phenomenon.

413 4. Extended numerical experiment

414 4.1. Scenarios description

415 In the Leicester project reported by Naicker and Rees [25], the cooling-
416 dominant system was designed with a 360 kW peak capacity. However, if
417 one looks into the monitored data, it can be found that the maximum heat
418 injection rate imposed on the BHE array was only 73 kW, which accounts
419 for only 20.3% of the peak designed capacity. Considering the energy con-
420 sumption on the heat pump, this rate could be much lower with respect to
421 the actual thermal load at the ground side during the system peak cooling
422 capacity. Since there is no reported information for both the actual COP
423 curve and the peak cooling capacity of the BHE array in the project, we
424 assumed the (360 kW) peak cooling capacity of building as the peak cooling
425 load on the BHE array at the ground side. Therefore, it is interesting to
426 see the long-term behaviour of the system, if the actual heat injection rate
427 is gradually approaching the designed peak. In this context, five additional
428 scenarios (numbered from #1 to #5) are numerically simulated with grad-
429 ually increasing heat injection rates. We choose to lift the total amount

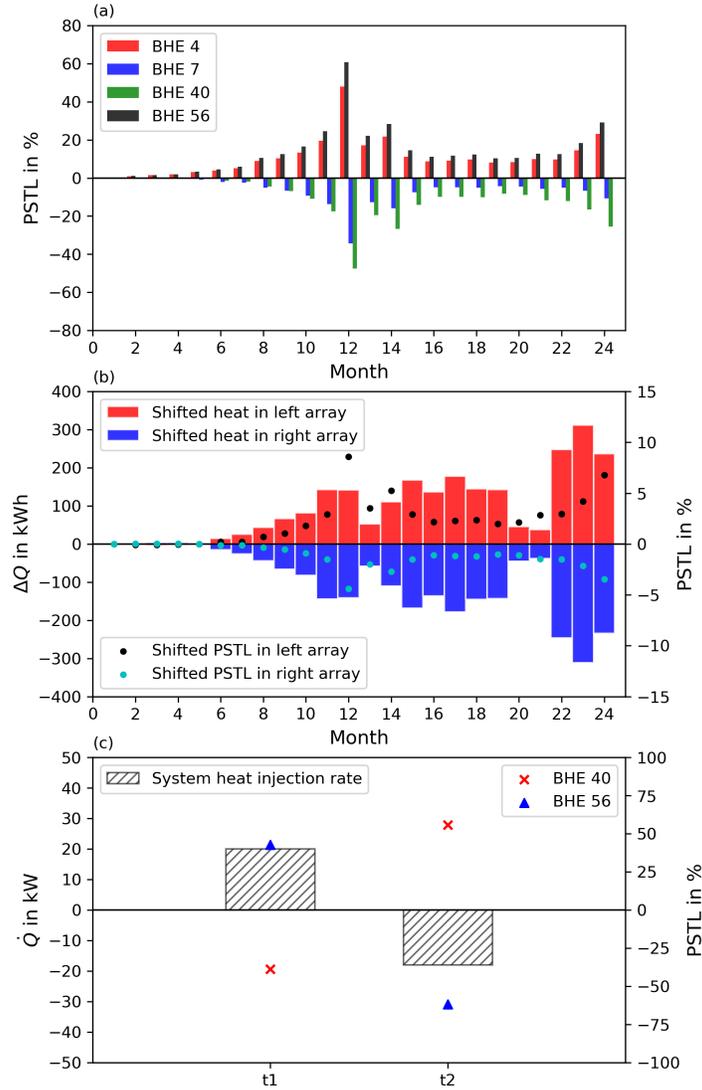


Figure 5: (a) Monthly averaged percentage of shifted thermal injection rate on the selected BHEs over the 2-year period; (b) Monthly total amount of shifted heat and the corresponding averaged percentage values in the left and right sub-array; (c) Percentage of shifted thermal injection rate on the selected BHEs at time $t_1 = 17,007$ hour and $t_2 = 17,011$ hour.

430 of exchanged heat imposed on the array to 100%, 197%, 296%, 395% and
 431 493% of the real observed value in the first year operation of the Leicester
 432 project. Under these conditions, the original designed peak capacity could
 433 be reached, while the characteristics of the load profile remains unchanged.
 434 From the second year forward, the annual system thermal load profile is
 435 specified to follow that of the first year and repeats itself until the end of
 436 20-th year. All five scenarios are then simulated to reveal the long-term
 437 behaviour of the BHE array.

438 Since the simulation aims to investigate the long-term behaviour and
 439 does not focus on its short-term responses, a monthly averaged system ther-
 440 mal load is specified in each scenario. The original measured values are
 441 reported in every minute, thus a conversion calculation is performed. By
 442 executing two steps, the resulting load profile specified in scenario #1 (The
 443 red line in Fig. 6(b)) is generated. The minute-wise extracted (heating mode,
 444 in negative MWh values) or injected (cooling mode, in positive MWh) heat is
 445 integrated separately over each month using the equation (Eq. (3)). Sum-
 446 ming the absolute values of heat exchanged in these two modes into the
 447 total amount of heat exchanged ($Q_{exchanged} = Q_{cooling} + |Q_{heating}|$) in each
 448 month. Subsequently the monthly averaged system thermal load $Q_{average}$ is
 449 obtained dividing by the duration of the month t_m (Eq. (5)). The positive
 450 and negative of this averaged value are then defined as the cooling and heat-
 451 ing loads in that month, respectively. The duration of the cooling or heating
 452 period in each month could be calculated using equation (6), where $Q_{cooling}$,
 453 $Q_{heating}$, and $Q_{exchanged}$ are the amount of the injected heat, extracted heat
 454 and total exchanged heat of the system in one month, respectively.

$$\dot{Q}_{average} = \frac{Q_{exchanged}}{t_m} \quad (5)$$

$$t_{cooling/heating} = \frac{|Q_{cooling/heating}|}{Q_{exchanged}} \cdot t_m, \quad (6)$$

455 According to Ahmadfard and Bernier [13], the monthly total flow rate
 456 could be set to 0.25 L s^{-1} per kW of the thermal load (Fig. 6(b)). By observ-
 457 ing the data reported by Naicker et al. [25], the minimal and maximal flow
 458 rates of the system were between 2 L s^{-1} and 30 L s^{-1} , respectively. In our
 459 numerical model, the circulation flow rate is then set to be linearly depen-
 460 dent on the absolute value of system thermal load, while being kept within
 461 the same minimum and maximum range. On the upper boundary of the
 462 model domain, an averaged monthly air temperature curve is imposed as
 463 Dirichlet boundary condition, based on the data reported in the first year

464 operation [25] (cf. Fig. 6(a), black line). Following the designed logic de-
 465 scribed above, the annual system thermal load and flow rate in scenario #2
 466 to #5 are adjusted proportionally, i.e. 197%, 296%, 395%, 493% based on
 467 scenario #1. As a consequence, the monthly exchanged heat in each scen-
 468 ario is also lifted proportionally, as illustrated in Fig. 6(a). In scenario #5,
 469 the peak system thermal load is set to be 173.6 kW, which is still only ca.
 470 half of the original design. All other settings of scenario #2 to #5 remain
 471 the same as those presented in Sec 3.

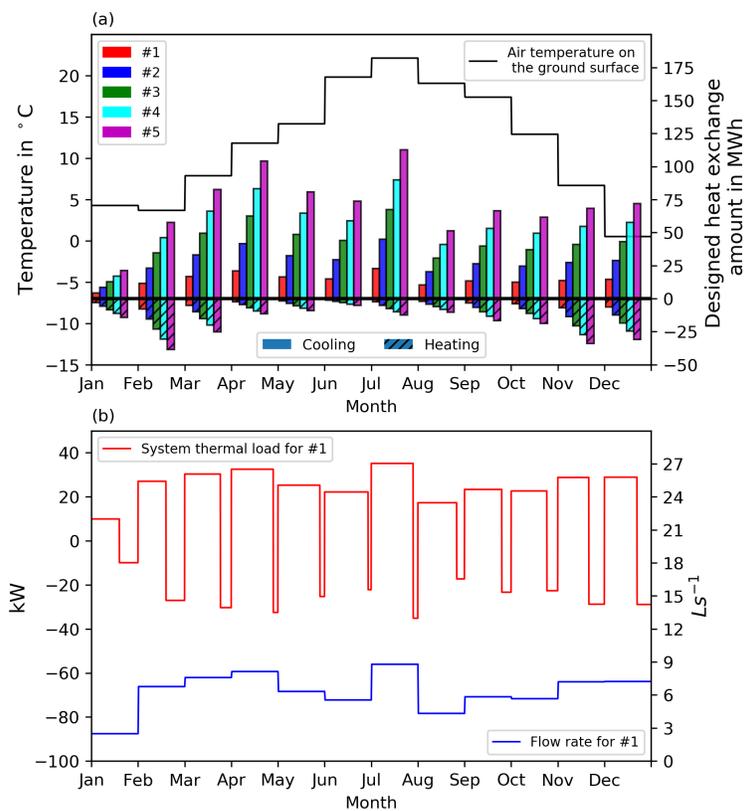


Figure 6: (a) Designed monthly heat exchange amount in the 5 scenarios and the annual air temperature on the ground surface. (b) Profile curve of system thermal load and flow rate specified in scenario #1.

472 *4.2. Results and analysis*

473 Fig. 7(a) illustrates the simulated temporal evolution of the outflow tem-
474 perature in all five scenarios. To ensure a sustainable performance of the
475 BHE array, the temperature of circulation fluid at the inlet of the heat
476 pump should usually be kept below 35 °C in the cooling mode [13]. This
477 35 °C threshold is indicated with a dotted line in this figure. Since the sys-
478 tem is dominated by heat injection, a gradual but steady increasing trend
479 in the outflow temperature is observed in all five scenarios, although with
480 different magnitudes. Among the five scenarios, the lowest temperature of
481 16.3 °C is observed after 20 years in scenario #1, where the amount of ex-
482 changed heat is minimum. The most intensive increase happens in scenario
483 #5, where the thermal load is the highest. After 20 years' operation, the
484 highest outflow temperature in scenario #5 reached 34.5 °C, which is already
485 approaching the 35 °C threshold. This suggests that the BHE array can be
486 sustainably utilised for 20 years, but not much longer, if the actual imposed
487 thermal load is close to the designed maximum heat capacity as reported
488 in [25]. However, in our model the peak cooling load at the ground site is
489 assumed to be identical as the reported designed peak load from the building
490 side. When considering the energy consumption on the heat pump, a higher
491 peak cooling load at the ground site could be expected. Therefore under
492 real working condition, the designed peak cooling load at building site may
493 cause an elevated outflow temperature from the BHE array to exceed 35 °C.

494 In Fig. 7(a), with the alternating cooling and heating load imposed,
495 the outflow temperature shows a monthly fluctuation pattern. In scenario
496 #1, with the lowest heat extraction rate (6.3 W m^{-1} on each BHE), the
497 temperature fluctuation is found to be the weakest with a magnitude of
498 about 1.5 °C. The strongest fluctuation is observed in scenario #5, with
499 the highest heat exchange rate in all 5 scenarios (31 W m^{-1}). The deviation
500 between the annual highest and lowest outflow temperature accounts for
501 11.5 °C. As aforementioned, the imposed system thermal load is averaged on
502 a monthly basis, hence a much stronger fluctuation in the fluid temperature
503 could be expected in real operations, especially when a high peak cooling
504 load is imposed.

505 The maximum rise in outflow temperature from all five scenarios are
506 evaluated and presented in Fig. 7(b). Assuming the subsurface is thermally
507 not disturbed, i.e. there is no additional heat injected or extracted, then
508 the outflow temperature from the BHE array should equal to the initial
509 soil temperature. This reflects the physical meaning of the origin point
510 in Fig. 7(b). From scenario #1 to #5, the amount of additional heat is
511 gradually increased. As a result, the increment in outflow temperature is

512 also rising accordingly. In Fig. 7(b), both the maximum and mean outflow
513 temperature rise in each scenario are plotted against the total amount of
514 accumulated heat at the end of 20-th year. It is interesting to find that,
515 the rise in both maximum (red dots) and mean (blue crosses) temperature
516 increments follow strict linear relationships with the amount of accumulated
517 heat injected into the subsurface through the BHE array. Meanwhile, it is
518 also noticed that the two slopes are distinctly different. This suggest that
519 even with the same amount of accumulated heat, the outflow temperature
520 can also be fluctuating due to the peak load imposed on the array. Based
521 on the simulated data, the correlation between ΔT and ΣQ can be fitted
522 perfectly with two linear regression lines with R-squared values of 99.989%
523 (maximum ΔT) and 99.982% (mean ΔT). Both temperature trends hint us
524 that when other factors, such as the distance between the boreholes and the
525 soil heat capacity is considered, it is possible to develop a simplified formula
526 to estimate the change of system outflow temperature in response to the total
527 amount of imbalanced heat accumulated over the years. Moreover, once
528 the linear relationship is identified, the acceptable amount of accumulative
529 imbalanced heat for a particular BHE array can be inversely estimated by
530 giving a threshold value of the working fluid temperature.

531 4.3. Temporal change of stored heat

532 In the previous part, it is clearly demonstrated that the elevated soil and
533 circulation fluid temperature, caused by the annually imbalanced thermal
534 load, are the controlling factors whether a BHE array can be sustainably
535 operated in the long-term. Since the elevated soil temperature reflects the
536 amount of heat accumulated in the subsurface, it is important to know how
537 much heat is stored in the subsurface, and also its percentage in comparison
538 to the amount of heat transferred to the building. The amount of stored heat
539 in the subsurface can be quantified by integrating the amount of sensible
540 heat in each element of the soil compartment in one time step, and then
541 comparing that total value with the one at the beginning of the simulation.

542 Fig. 8(a) illustrates the evolution of the annual amount of stored heat in
543 scenario #3 and its percentage with respect to the total amount of system
544 imbalanced heat. The stored heat increases gradually over the years, from
545 360 MWh in the first year up to 5043 MWh in the 20-th year. Meanwhile,
546 its percentage drops from nearly 100% at the beginning and stabilises at
547 ca. 70% in the end. This suggests that there is an increasing proportion
548 of imbalanced heat dissipating to the atmosphere through the ground sur-
549 face. This trend is consistent as the behaviour found in our previous work
550 [30, 19], where a heating-only scenario was analysed. There the thermal

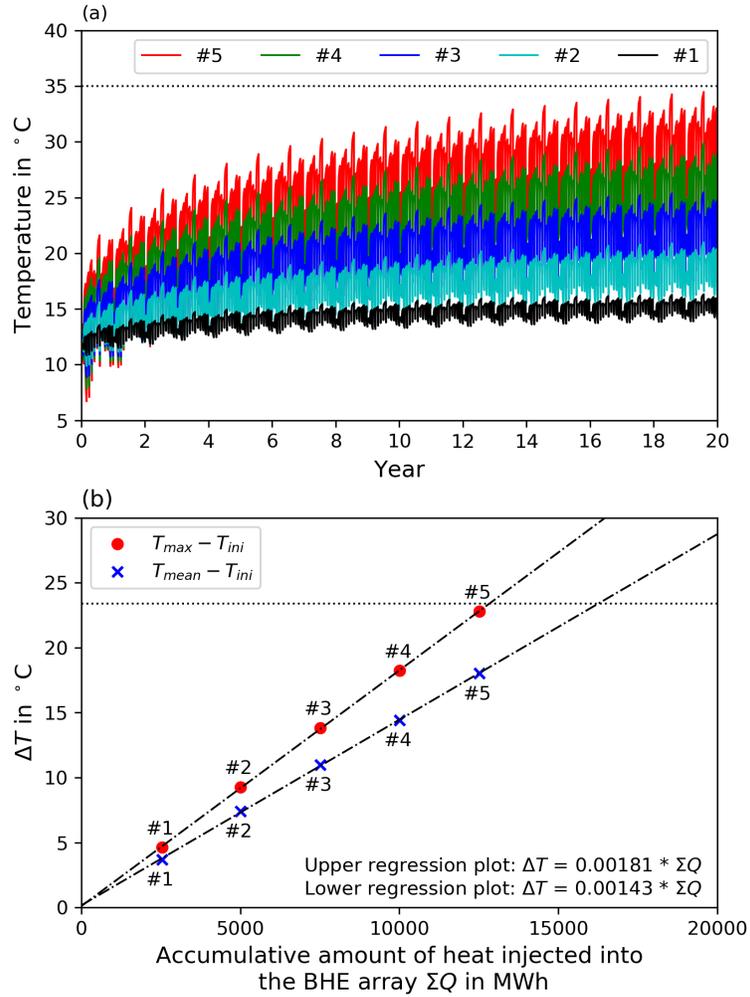


Figure 7: (a) Temperature evolution of the working fluid flowing out from the BHE array in the 5 scenarios over 20 years; (b) Regression plot for the correlation between the maximum and mean outflow temperature against the total amount of accumulated heat injected into the BHE array at the end of the 20-th year.

551 recharge through the ground surface has a cumulative influence on the soil
552 temperature distribution in and around the BHE array. More specifically,
553 the area with elevated soil temperature will extend itself over the long-term
554 heat injection, thus enhancing the thermal gradient from the subsurface to-
555 wards the ground surface. Therefore, the amount and proportion of thermal
556 discharge are also elevated over time. Despite of the elevated thermal dis-
557 charge, analysis on the scenario #3 result reveals that there is still 67.2% of
558 the total imbalanced heat stored in the subsurface after 20 years. When the
559 amount of imbalanced heat increases from 2534 MWh to 12 512 MWh from
560 scenario #1 to #5, the amount of stored heat is also increasing accordingly
561 (see the blue bars in Fig. 8(b)). However, due to the elevated thermal dis-
562 charge mentioned above, its percentage slightly drops from 70.8% down to
563 65.6%. Based on the above analysis, one can conclude that over the long-
564 term operation of a BHE array, the majority of the annual imbalanced heat
565 will be stored in the subsurface, and its percentage is less dependent on the
566 amount of heat injected.

567 4.4. Spatial distribution of stored heat

568 To further investigate the spatial distribution of the stored heat in the
569 subsurface, we have created two controlled spaces. Each contains a BHE
570 sub-array inside. The boundary of the space is drawn with a 2.5 m distance
571 from the BHE located at the peripheries of the array (see that dark grey
572 area marked in Fig 9(a)). This setup results in a space of 50 000 m³ for the
573 left sub-array and 158 000 m³ for the right part. With both parts considered
574 together, the specific stored heat (kWh m⁻³) is quantified by normalising
575 the total amount of stored heat over the volume. These specific heat values
576 for 5 different scenarios are depicted in Fig 9(b). These values have been
577 also compared against the total amount of imbalance heat, and the resulting
578 percentages are presented in the same figure.

579 In the five scenarios, the specific stored heat values increase along with
580 the elevated amount of imbalance heat. In scenario #5, a maximal spe-
581 cific stored heat of 20.0 kWh m⁻³ is achieved. According to the findings
582 in Sec 4.2, the temperature of the outflow fluid is already approaching the
583 35 °C threshold in this case. One can concluded that with the current system
584 design, 20.0 kWh m⁻³ can be considered as the upper-limit in the capacity
585 of storing imbalanced heat in the subsurface. When normalising this value
586 by the total amount of imbalanced heat, its ratio remains at around 25%.
587 Combined with the analysis in the previous section, it can be concluded
588 that heat actually dissipates far way from the array location and the ther-
589 mal plume spreads into a much larger area. For all the heat stored in the

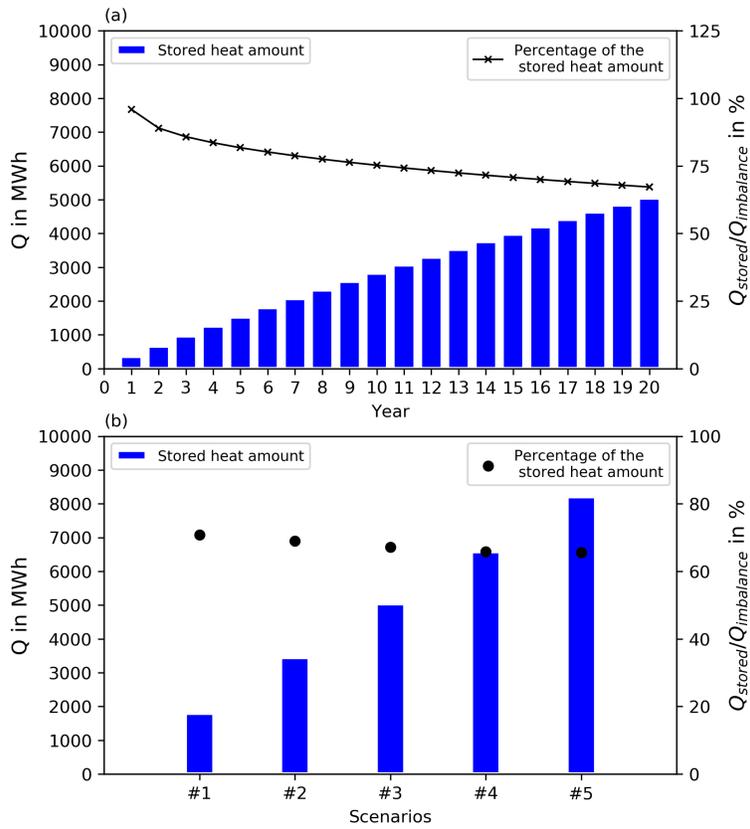


Figure 8: (a) Evolution of the amount of stored heat in the entire domain over 20 years, based on simulated result of scenario #3; (b) Total amount of stored heat and their proportion from scenarios #1 to #5.

590 subsurface, around 37% is stored in the array area, while the rest goes to
591 the surrounding subsurface.

592 Nevertheless, if the distance among adjacent BHEs is enlarged, the above
593 specific heat values and ratios may change as well. Here, a preliminary re-
594 lationship can be illustrated between the amount of stored heat and the
595 respective adjacent distance S . In scenario #5, a 7 m instead of 5 m BHE
596 distance is specified. After 20 years operation, a maximum outflow temper-
597 ature of 30.5 °C is being predicted, which is lower than the 34.5 °C value
598 when the model is specified with 5 m distance. The reason behind this is
599 the decreasing of the specific stored heat value in the BHE array. As shown
600 in Fig. 9(c), the value decreases from 20.0 kWh m⁻³ to 12.9 kWh m⁻³ when
601 S is enlarged to 7 m. Meanwhile, 32.2% of system total amount of imbal-
602 ance heat is stored in the enlarged BHE array, which is higher than the
603 25% value calculated in the 5 m model. Therefore one can conclude that the
604 adjacent distance has an important role in determining the long-term oper-
605 ation behaviour of a large BHE array. To be specific, the adjacent distance
606 is as important as the length of BHE. Thus, the subsurface volume around
607 the BHE array, which is determined by the adjacent distance as well as the
608 length of the BHE, should be considered as one of the characteristic factors
609 in the designing of the BHE array.

610 5. Discussions

611 5.1. Pipeline network design

612 As shown in Sec 3.2, a simplified pipeline network model is built ac-
613 cording to the ground loop design reported in the Leicester project. By
614 adopting this coupled feature, the hydraulic states within the entire ground
615 loop could be captured. In all scenarios stated in Sec 4, the average hy-
616 draulic loss in the entire BHE array is below 1% compared to the amount
617 of the system thermal load over the long-term operation. A transient max-
618 imum percentage with 2.2% can be found in scenario #5, due to the high
619 flow rate there. It should be noticed that all the connection pipes in the
620 circulation loop are assumed to have no hydraulic loss in this study. When
621 detailed information on the material and diameter of the pipes are avail-
622 able, it is more reasonable to consider the hydraulic losses when predicting
623 the long-term behaviour of a large BHE array. In reality, both the form
624 of BHE array and the system operation strategy varies greatly from each
625 GSHP project [39, 21]. Regarding this point, the present numerical model
626 shows its advantage, because it is capable to consider pipeline network with
627 arbitrary connections. In the TESP network, the hydraulic states for each

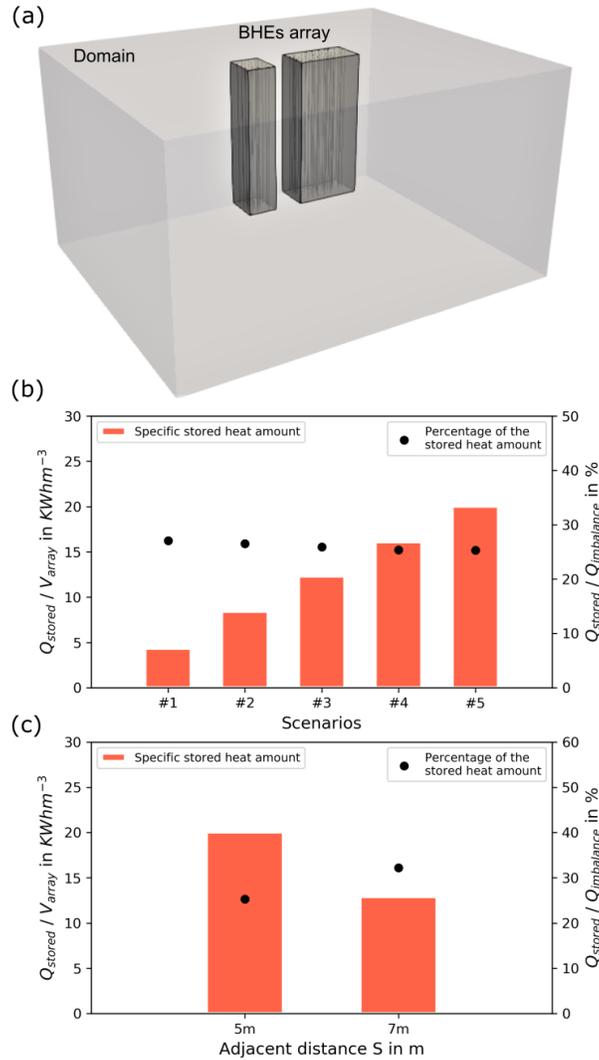


Figure 9: (a) Selected subsurface volume (marked with dark grey); (b) Specific heat stored in the selected volume and its percentage of over the amount of total imbalanced heat after 20 years' operation in the 5 scenarios; (c) Specific heat stored in the selected volume and its percentage of over the amount of total imbalanced heat after 20 years' operation in scenario #5, in models specified with a 5 m and 7 m adjacent distance.

628 pipe is automatically computed based on the mass and energy conservation.
629 In addition, a temperature dependent heat pump COP curve can also be
630 specified in TESP_y as one of the input parameters. With such information
631 at hand, a multiple BHE array system based on the amount of energy con-
632 sumption at building site can be predicted by our model in a more accurate
633 manner.

634 Besides, it should be noticed that the heat extraction rate shifting phe-
635 nomenon shown in Fig. 5 is the effect of current pipe network design. With
636 the parallel BHE array setup, all BHEs are receiving an identical inflow tem-
637 perature and then deliver different thermal load performances due to the soil
638 temperature imbalance in the array. It indicates that the pipe network itself
639 has an intrinsic feature of re-balancing the thermal load among different
640 BHEs. Therefore it is necessary to simulate a large BHE array system, with
641 the coupled pipeline network explicitly considered. Only in this way, the
642 system behaviour over the long-term operation can be correctly revealed.

643 *5.2. Optimisation of the system operation*

644 As shown in Fig. 5 and discussed in Sec 3.5.2, thermal shifting phe-
645 nomenon in a large BHE array system can be clearly observed over the
646 long-term operation. When the shifting happens, BHEs located at the edge
647 of each sub-array have larger heat injection rates than the mean designed
648 value, while those BHEs at the centre have lower rate. It should be noticed
649 that such seasonal shifting behaviour is not unique and has already been
650 reported by several researchers. For example, our previous research [19] has
651 investigated the shifting behaviour in detail. This phenomena has also been
652 confirmed in the study conducted by You et al. [20] through an analyti-
653 cal approach. Bayer et al. [40] observed similar pattern and developed an
654 optimisation strategy based on it. They suggested that a given number of
655 BHEs located at the centre of the array should be disconnected from the
656 pipe network in order to mitigate the thermal anomalies in the BHE array
657 subsurface.

658 Besides, as stated in Sec 3.5.2, when a heating phase is applied in between
659 the cooling seasons, the thermal recharge of the subsurface can partially
660 mitigate the shifting phenomenon. Based on our analysis in the previous
661 section, the heat dissipation pattern can be further utilised to improve the
662 array operation. More specifically, during the heating phase, only those
663 BHEs located at the array centre should be applied, because the elevated
664 soil temperature there allows them to deliver a higher specific heat extraction
665 rate. Also, the cold plume created by heating application can be utilised
666 later on by the BHEs at the peripheries. Such optimisation strategy requires

667 a series of numerical simulations and is currently being investigated by our
668 team.

669 *5.3. Unconsidered factors*

670 As this study is based on the monitoring data from the Leicester project,
671 the amount of heat injected into the subsurface is more than that extracted.
672 Most findings in this work should be considered as only effective for cooling
673 application dominated BHE arrays. However, in heating dominated systems,
674 a similar but inverse trend can be expected. A similar correlation between
675 the drop in fluid temperature and the accumulative amount of extracted
676 heat can also be expected over the long term operation. There, the limiting
677 factor could be the 0 °C temperature limit on the outflow circulation fluid,
678 which is imposed by the heat pump [13]. By considering this limit, the
679 acceptable total amount of extracted heat from the BHE array subsurface
680 for a sustainable system operation can also be estimated.

681 It is well known that groundwater flow could enhance the capacity of a
682 BHE array, by bringing in additional thermal recharge from the upstream
683 subsurface. In this work, information on groundwater flow is not reported by
684 Naicker et al. [25]. Although the OpenGeoSys code used here is capable of
685 simulating the BHE array under groundwater flow conditions (see e.g. Meng
686 et al. [41]), we assume that there is no groundwater present in the Leicester
687 site. For the majority of shallow geothermal GSHP projects, our assumption
688 is also conservative but safe. Therefore, the main findings and conclusions
689 achieved in this work are applicable to most BHE array projects.

690 **6. Conclusion and outlook**

691 In this work, the long-term behaviour of a large BHE array located in
692 Leicester, UK is investigated by conducting numerical simulations. The
693 model is validated against monitoring data through two years of operation
694 under real working conditions. It is found that heat starts to accumulate in
695 the centre of the BHE array due to higher amount of cooling load imposed
696 on the system. This results in the heat injection rate being gradually shifted
697 from the BHEs in the centre towards those at the edges. At the mean time,
698 the thermal load is also slowly transferred from the right-side array towards
699 the left side.

700 In the Leicester project, the actual heat injection rate is only 20.3% of
701 its peak designed value. Scenario simulation with gradually increasing heat
702 injection rates reveals that the BHE array can be sustainably utilised for 20
703 years even under the designed peak thermal load, but likely not any longer.

704 It is more interesting to find that the rise in outflow temperature follows a
705 perfect linear dependency on the amount of accumulated heat injected into
706 the BHE array. Moreover, it is found that around 37% of the total imbalance
707 heat can be stored in the subsurface volume around the BHE arrays. When
708 the circulation fluid temperature is approaching the 35 °C upper limit, a
709 maximum of 20.0 kWh m⁻³ specific heat can be stored in the subsurface.
710 Nevertheless, when the distance among the adjacent BHEs increases from
711 5 m to 7 m, the corresponding outflow temperature decreases from 34.5 °C
712 to 30.5 °C, and the specific heat value also decreases to 12.9 kWh m⁻³. It
713 indicates that the adjacent distance among BHEs has an important role to
714 determine how much imbalanced heat a multiple BHE array can sustain.

715 As discussed in section 5.2, based on the prediction of seasonal thermal
716 shifting, the operation strategies could be optimised to achieve a higher
717 specific heat extraction rate. More importantly, with the consideration of
718 other factors such as the distance between the boreholes and the soil heat
719 capacity, it is possible to develop a simplified formula to estimate the change
720 of system outflow temperature in response to the total amount of imbalanced
721 heat accumulated over the years. This relationship can help to prevent the
722 system from being overloaded in the long-term operation. However, the
723 exact relationship between the amount of imbalanced heat, the distance
724 between adjacent BHEs, and the increment in circulation fluid temperature,
725 needs to be further investigated in the future.

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