

# Soil moisture parameter regionalization in a mesoscale hydrologic model

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## 1. Introduction

Regional climate modeling and integrated water resources management require, among other things, of a robust, distributed, and parsimonious hydrologic model able to estimate the magnitude of the hydrologic consequences of the land cover and climatic changes on a mesoscale river. This model should also provide reasonable estimates of a number of state variables required for other related processes. Soil moisture is one of these state variables. Current state-of-the-art in estimating and validating soil moisture is not quite satisfactory though. This study presents a comparison of two regionalization approaches that may help improving the estimation of daily estimates made with the distributed hydrologic model HBV-UFZ. Plausibility tests were carried out with a proxy obtained from MODIS images.

## 2. Facts and research questions

The spatial-temporal distribution of the soil moisture plays a crucial role on:

- Lateral flows and streamflow generation
- Evapotranspiration and plant growth dynamics
- Response (feedbacks) of the regional climate models

⇒ How to better regionalize the parameters of the soil infiltration model?  
 ⇒ How to constrain its parameters during calibration?

## 3. Mesoscale hydrological model

State equations: cell (i), t:

$$\begin{aligned} \dot{x}_1 &= P - F - E_1 \\ \dot{x}_2 &= F - M \\ \dot{x}_3 &= R + M - E_2 - I - q_1 \\ \dot{x}_4 &= I - q_2 - q_3 - C \\ \dot{x}_5 &= C - K - q_4 \end{aligned}$$

Output: Runoff Q(t):

$$\hat{Q}(t) = \langle \hat{Q}_r(t) \rangle = g(\mathbf{x}, \mathbf{v}, \boldsymbol{\beta}) + \epsilon(t)$$

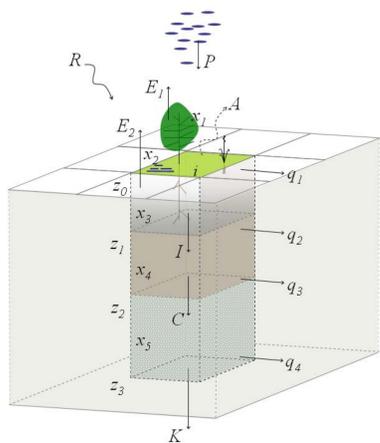
Transfer functions:

$$\begin{Bmatrix} \beta_1 \\ \vdots \\ \beta_n \end{Bmatrix}_{(i,t)} = f \left[ \begin{Bmatrix} \gamma_1 \\ \vdots \\ \gamma_m \end{Bmatrix}, \begin{Bmatrix} v_1 \\ \vdots \\ v_k \end{Bmatrix}_{(i,t)} \right] \quad n \times N \times T \gg m$$

where

$\dot{x}_i \equiv \frac{\partial x_i}{\partial t} \quad \forall i$   
 $i, t$  Indexes for cell and time respectively  
 $N$  Number of cells  
 $T$  Number time intervals  
 $n$  Number model parameters  
 $m$  Number transfer function parameters  
 $q_k$  Surface runoff component,  $k = 1, \dots, 4$   
 $v_1$  [1] Land cover  
 $v_2$  [mm] Soil texture class

$v_3$  [1] Fraction of impervious areas in floodplains.  
 $v_4$  [1] Fraction of clay content.  
 $v_5$  [1] Fraction of sand content.  
 $v_6$  [ $kgm^{-3}$ ] Bulk density.  
 $\Theta$  [1] Modeled soil moisture.  
 $\Theta_s$  [1] Saturated soil moisture.  
 $z_k$  [m] Depth of the horizon  $k$ .  
 $\beta$  regionalized model parameters.  
 $\gamma$  transfer function parameters (to be calibrated).



Grid based HBV-UFZ

## 4. Soil moisture process

Assuming only vertical flows and Brook & Corey (1964) parametrization of the soil hydraulic conductivity.

$$\begin{aligned} \dot{x}_3 &= F + M - E_2 - I \\ E_2 &= \begin{cases} \inf \{x_3, (V - E_1)\} & x_3 > \beta_2 \\ \inf \left\{ x_3, \frac{x_3}{\beta_2 - \beta_1} (V - E_1) \right\} & \beta_1 < x_3 \leq \beta_2 \\ 0 & \text{otherwise} \end{cases} \\ \frac{I}{R + M} &= \left( \frac{x_3}{\beta_3} \right)^{\beta_4} \approx \left( \frac{\Theta}{\Theta_s} \right)^{\frac{2}{\lambda} + 3} \end{aligned}$$

## 5. Regionalization approaches

**R1: Based on land cover and soil classes:** It discriminates land cover classes and soil texture types into subsets, each of them exhibiting unique parameters.

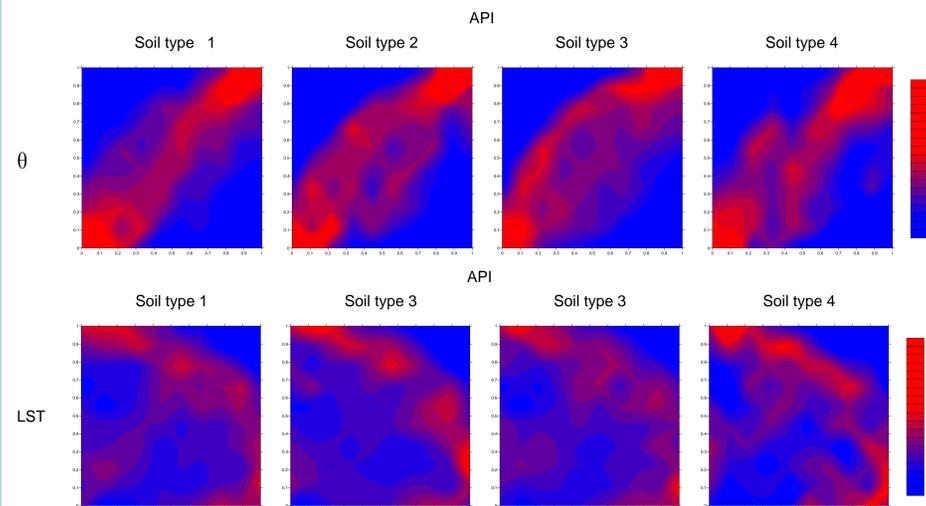
$$\begin{aligned} \beta_3 &= f(v_1, v_2, \gamma) \\ \beta_4 &= f(v_1, \gamma) \end{aligned}$$

**R2: Based on pedotransfer functions:** Takes into account the fraction of clay, sand and the bulk density. The latter, in turn, depends on the organic matter content which is land cover specific.

$$\begin{aligned} \Theta_s &= f(v_1, v_4, v_5, v_6, \gamma) \\ \lambda &= f(v_1, v_6, \gamma) \end{aligned}$$

## 6. Stochastic dependence using copulas

$$F(x_1, x_2) = P[X_1 \leq x_1, X_2 \leq x_2] = C(F_1(x_1), F_2(x_2))$$

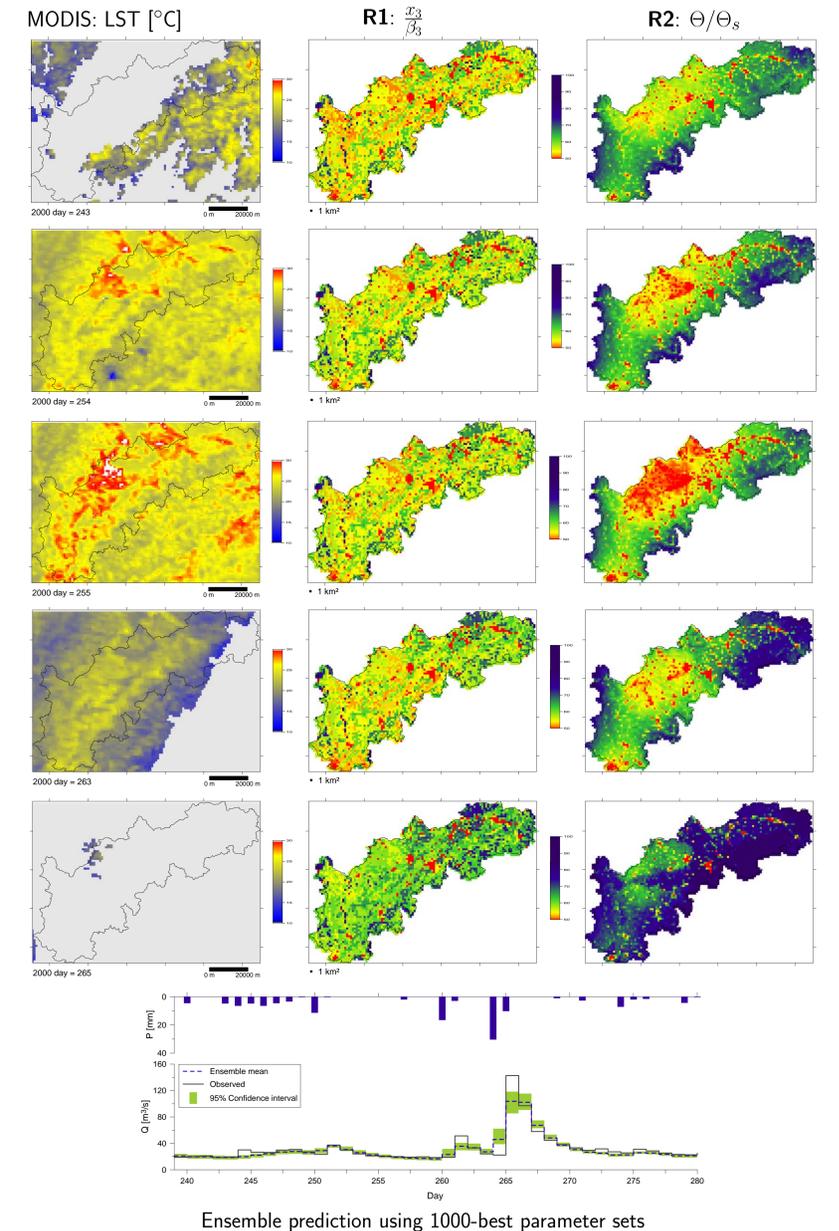


$$\Theta \sim f(\text{LST}, \text{NVDI}, \beta)$$

API = Antecedent Precipitation Index

LST = Land and Surface Temperature, <http://modis.gsfc.nasa.gov/>

## 7. Results



## 8. Conclusions

- Regionalization (R2) produced a significant improvement in model performance (NSE=0.90).
- R2 produced more plausible spatial patterns than the R1 approach.
- Proxies such as API and LST (see copulas) are stochastically dependent on the modeled soil moisture.