

# Using dynamic transit times and StorAge Selection (SAS) functions to explore nitrate export from small agricultural catchments

J. Yang<sup>1,2</sup>, A. Musolff<sup>1</sup>, I. Heidbuechel<sup>1</sup>, J.H. Fleckenstein<sup>1,3</sup>

1) Department of Hydrogeology, Helmholtz Center for Environmental Research - UFZ, Leipzig, Germany, 2) Hohai University, Nanjing, China, 3) Division of Hydrologic Modeling, University of Bayreuth, Germany



UNIVERSITÄT  
BAYREUTH

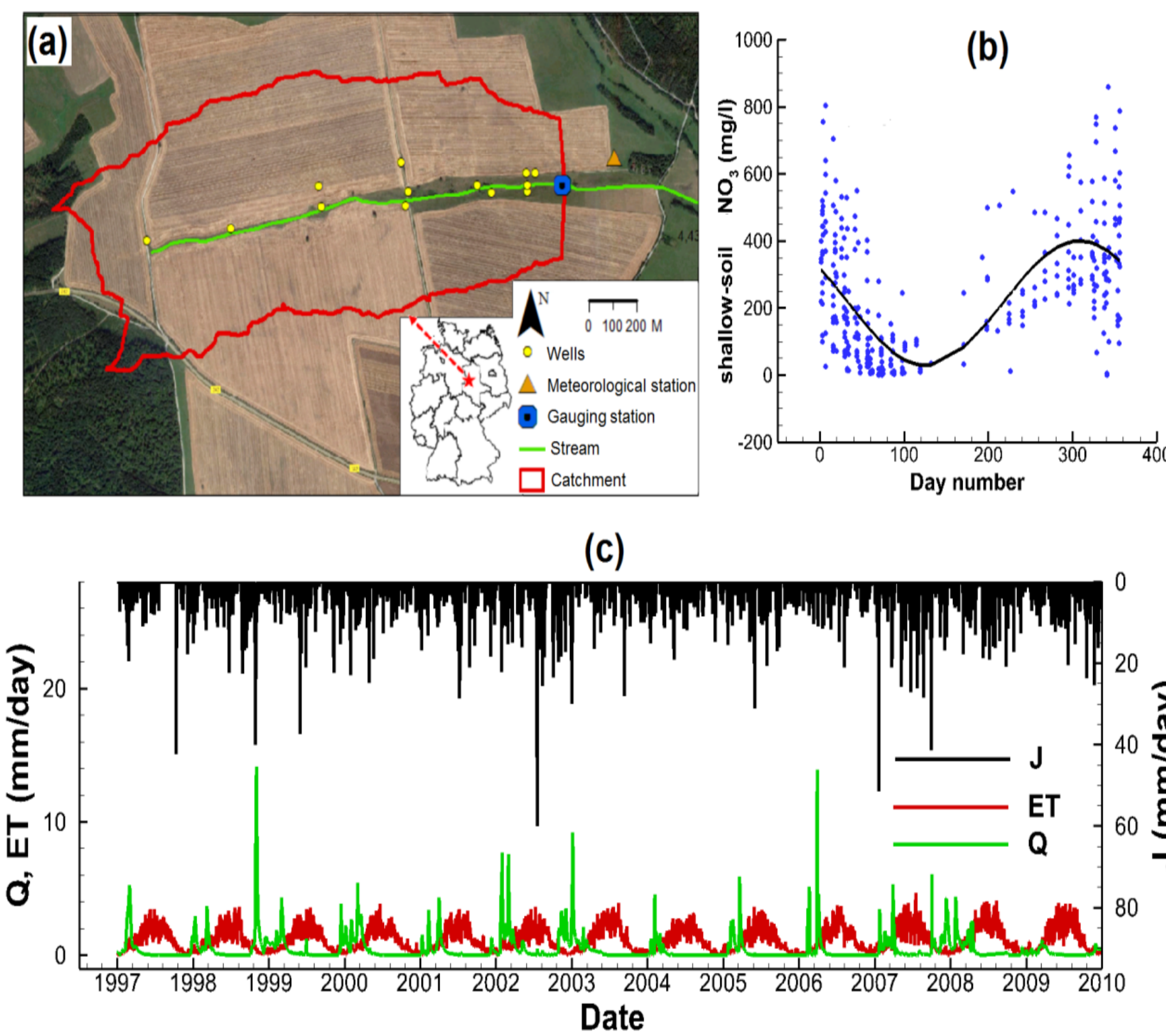


HELMHOLTZ  
Centre for Environmental Research

## 1 Background and Objectives

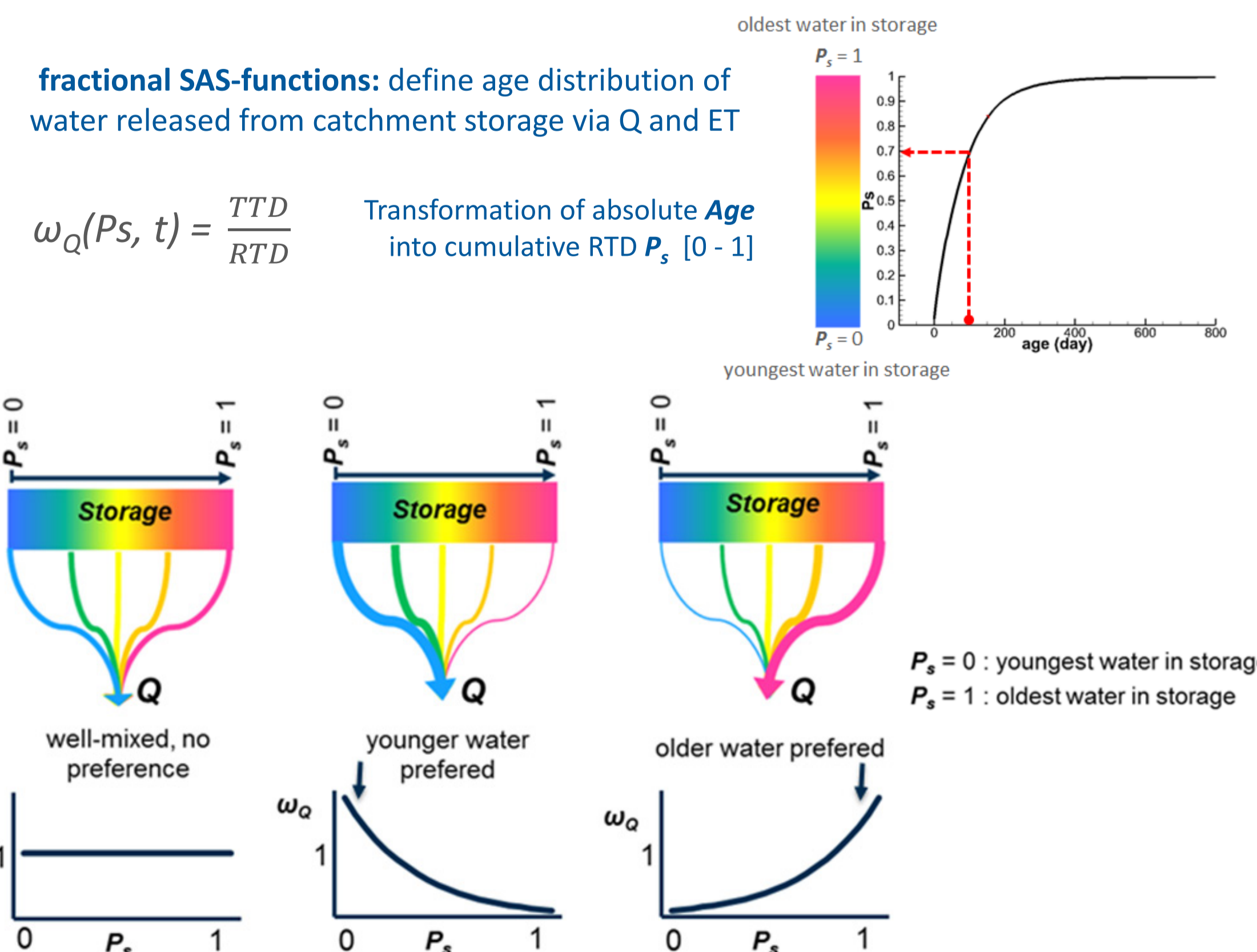
- Mechanistic transport models at catchment scale challenging
- Transit time distribution based models as potential alternative
- StorAge Selection (SAS) functions to define age distribution and concentration in catchment outflow (Q)
- Objective I:** test SAS-function based nitrate export model
- Objective II:** explore NO<sub>3</sub> export dynamics for different catchment types using SAS-function based model → scenarios

## 2 Reference catchment and field data

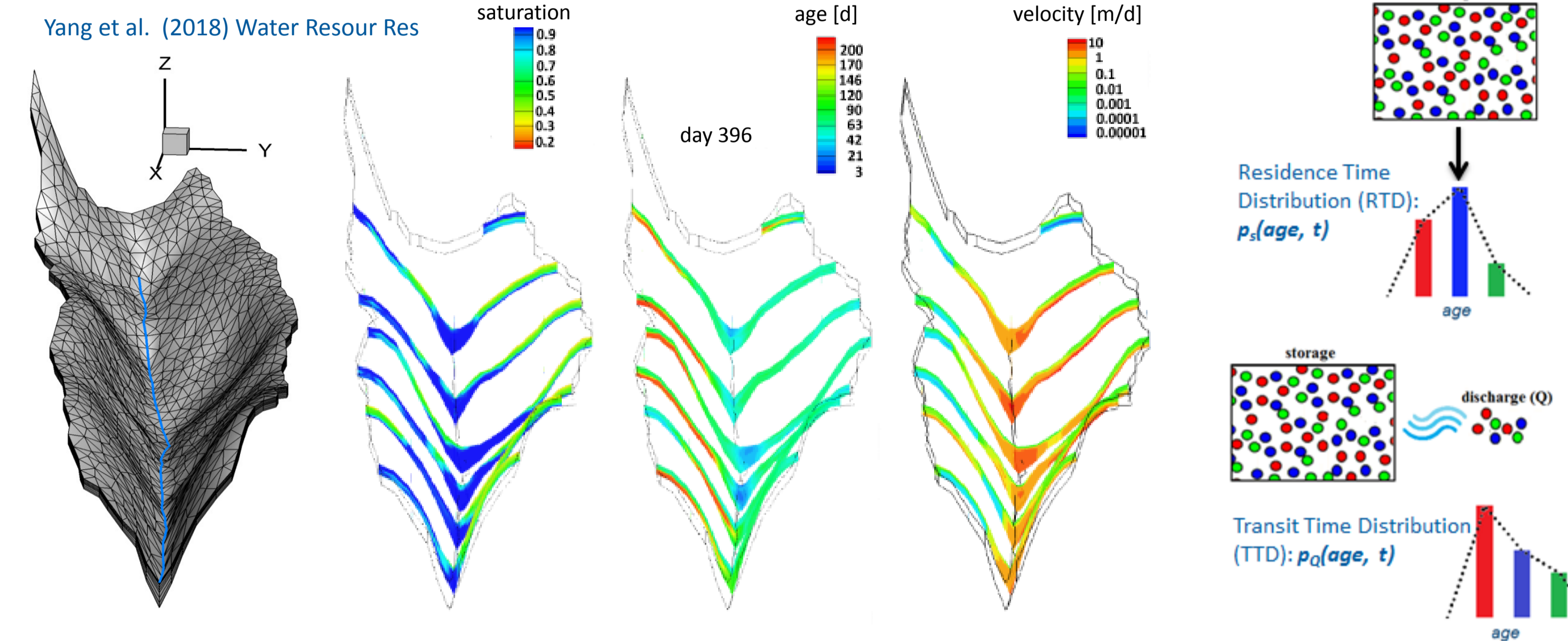


- Schäferal catchment in Central Germany (1.44 km<sup>2</sup>)
- Nitrate percolation below root zone (from lysimeter data)
- Precipitation (J), evapotranspiration (ET) and discharge (Q)

## 3 StorAge Selection (SAS) functions



## 4 Mechanistic reference model (HydroGeoSphere + PARTRACE)



velocity fields (HGS) → random-walk particle tracking (PARTRACE) – water ages → SAS-functions

## 5 Formulation of SAS-function based nitrate export model

age master equation (Botter et al. (2011) Geophys Res Lett)

$$\frac{\partial s(T, t)}{\partial t} = -Q(t) \cdot p_Q(T, t) - ET(t) \cdot p_{ET}(T, t) - \frac{\partial s(T, t)}{\partial T}$$

solute mass balance equation (following: Quéloz et al. (2015) Water Resour Res)

$$\frac{\partial C_s(T, t) s(T, t)}{\partial t} = C_s(T, t) [Q(t) \cdot p_Q(T, t) + \alpha ET(t) \cdot p_{ET}(T, t)] - \frac{\partial C_s(T, t) s(T, t)}{\partial T} - \lambda \cdot C_s(T, t) s(T, t)$$

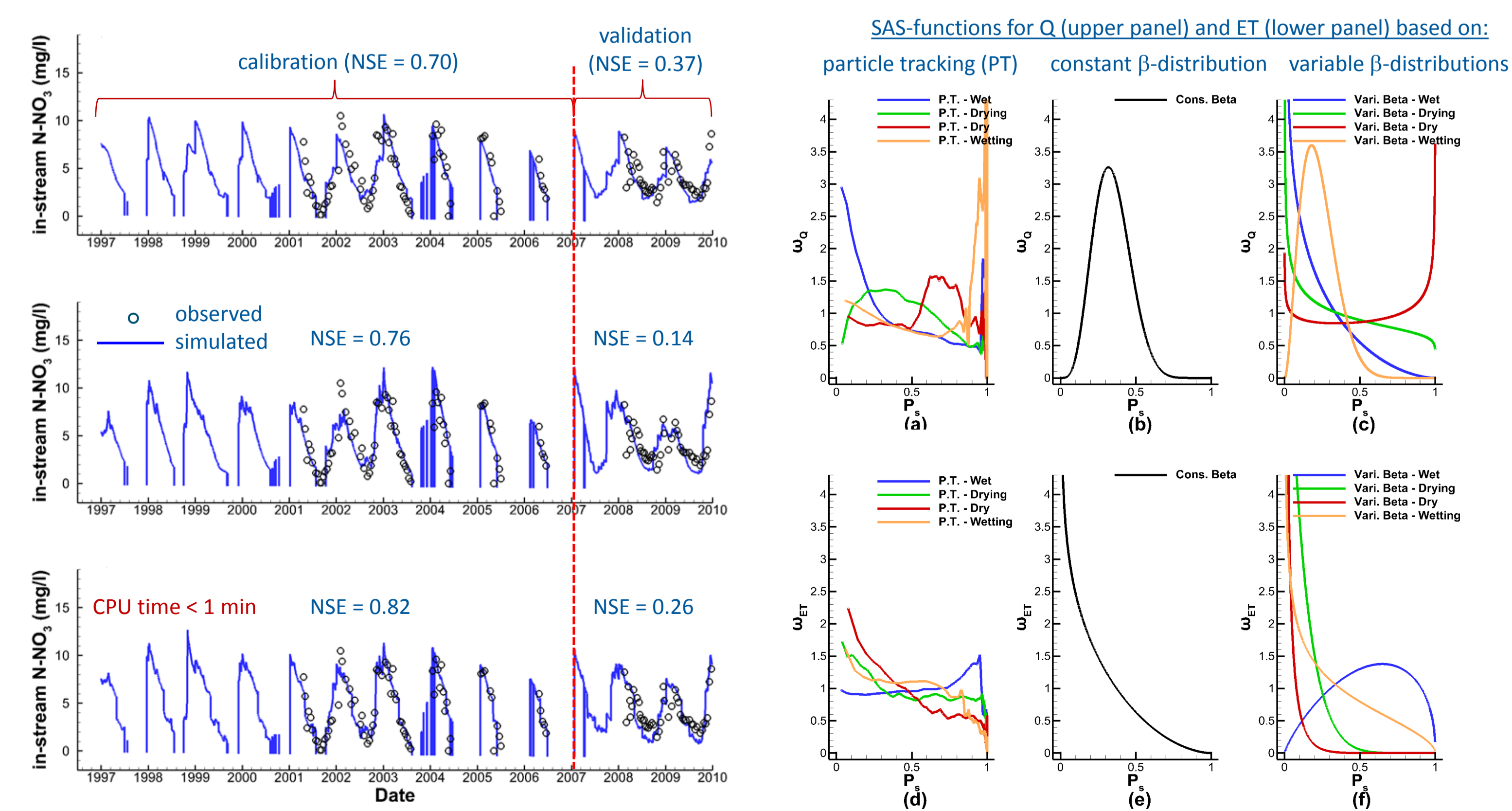
solute concentration in Q by integration  $C_Q(t) = \int_0^\infty C(T, t) p_Q(T, t) dT$

inverse model subject to:

- Initial conditions:  $S(0), p_s(T, 0), C(T, 0)$
- Boundary conditions:  $Q(t), ET(t), J(t), C_{in}(t)$
- $p_Q(T, t) = \omega_Q p_s(T, t)$  &  $p_{ET}(T, t) = \omega_{ET} p_s(T, t)$

SAS-functions defined by  $\beta$ -distributions:  $f(x, a, b) = x^{a-1} \cdot (1-x)^{b-1}$

## 6 Results – nitrate concentrations in Q and SAS-functions



## 7 Results – mass removal, reactivity, mean transit times

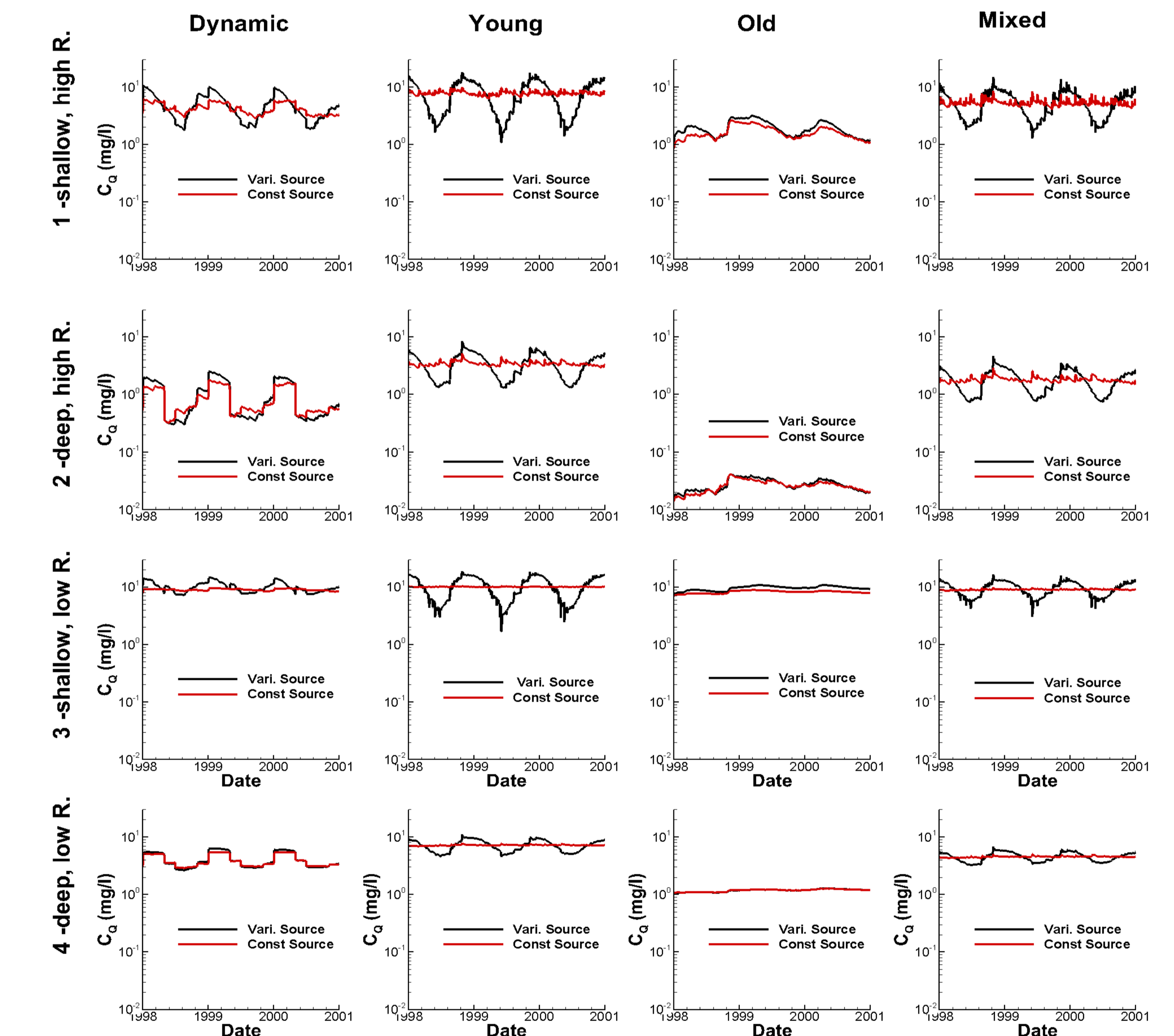
Summary statistics for the different models:

	PT-model	constant $\beta$	variable $\beta$
NSE (calibration)	0.70	0.76	0.82
NSE (validation)	0.37	0.14	0.26
Mass removal by reactions [kg/ha/year]	37.0	34.7	34.8
Mass export by discharge [kg/ha/year]	11.5	12.9	13.0
Half-life time reaction [days]	126.1	79.6	84.1
Mean $T_Q$ [days]	296.9	122.3	219.6
Mean $T_{ET}$ [days]	288.3	143.4	247.7

- Model fits and mass balances similar between models
- Reaction rates and mean ages of Q and ET quite different
- Constant  $\beta$ -model produces younger mean Q and ET
- Variable  $\beta$ -model reproduces seasonal shifts in selection preference well

## 8 Scenario simulations – different catchment types

Differing in: age preference (AP), reactivity (R), aquifer depth (AD), source variability (SV)\*



## 9 Conclusions – „take home messages“

- Observed NO<sub>3</sub>-concentrations in Q reasonably reproduced by SAS-models
- Modeling suggests denitrification as a significant mass removal process
- Seasonal shifts in SAS-functions needed to match water ages from PT-model
- Interplay between AP, R, AD and SV\* controls seasonal NO<sub>3</sub>-variability in Q
- NO<sub>3</sub>-concentrations in Q alone may not fully constrain SAS-based inverse model

References:  
 Yang, Heidbuechel, Musolff, Reinstorf, Fleckenstein (2018) Exploring the Dynamics of Transit Times and Subsurface Mixing in a Small Agricultural Catchment, *Water Resour Res*, 54(3)  
 Botter, Bertuzzo, Rinaldo (2011), Catchment residence and travel time distributions: The master equation, *Geophys Res Lett*, 38  
 Quéloz, Carraro, Benettin, Botter, Rinaldo, Bertuzzo, (2015) Transport of fluorobenzoate tracers in a vegetated hydrologic control volume: 2. Theoretical inferences and modeling. *Water Resour Res*, 51