

Modellierung von Hydrosystemen

"Numerische und daten-basierte Methoden"

BHYWI-22-04 @ 2018

Catchment-Übung im Detail

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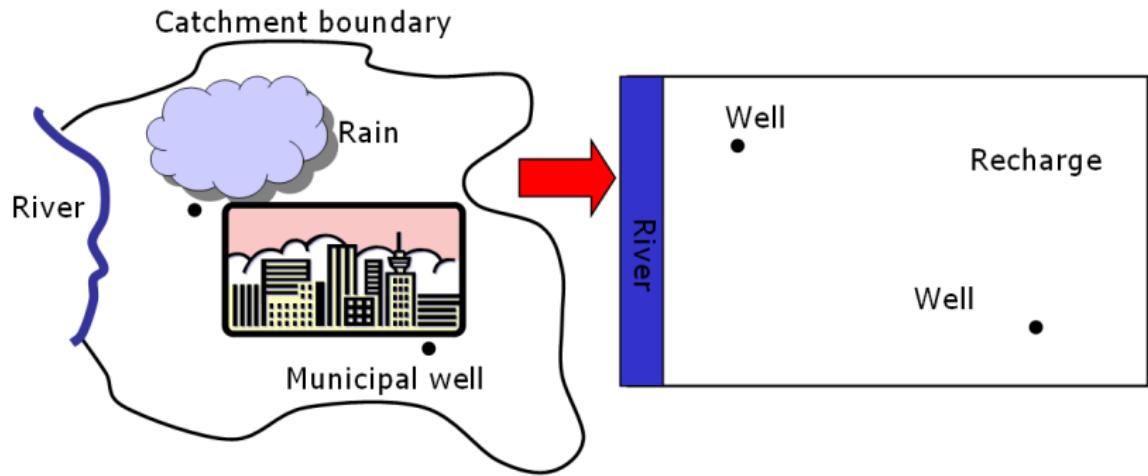
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27.04./04.05.2018 - Dresden

Prinzip-Beispiel



River:
Fixed head
boundary
condition
 $H = 10 \text{ m}$

No flow – e.g. fault

- Pumping well
 $Q_{P2} = 0.001 \text{ m}^3/\text{s}$

Recharge: homogeneous and constant
 $R = 1.0e-8 \text{ m}^3/(\text{m}^2\text{s})$

- Pumping well
 $Q_{P6} = 0.005 \text{ m}^3/\text{s}$

No flow - streamline

No flow – water divide

Figure: Definition der Randbedingungen

Prinzip-Beispiel

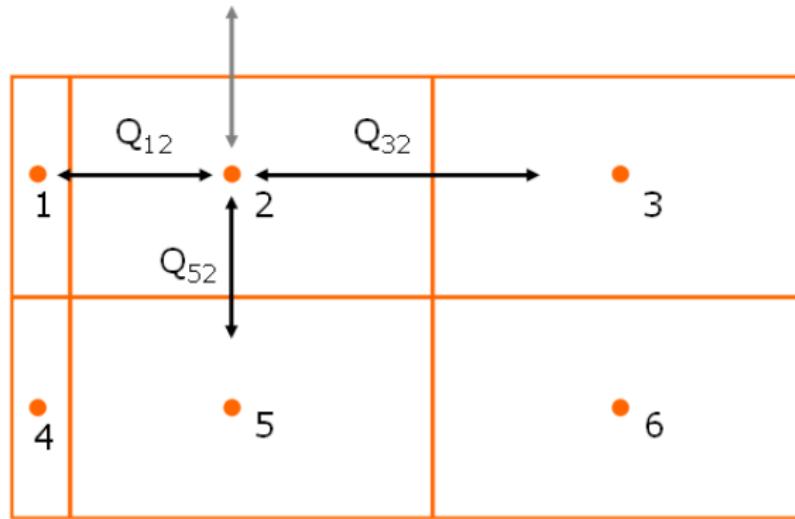


Figure: Knoten-Bilanz aufstellen

$$Q_{12} + Q_{32} + Q_{52} + Q_R + Q_{P2} = 0$$

Knotenbilanzen

$$2 : Q_{12} + Q_{32} + Q_{52} + Q_R + Q_{P2} = 0 \quad (2)$$

$$3 : Q_{23} + Q_{63} + Q_R = 0 \quad (3)$$

$$5 : Q_{25} + Q_{45} + Q_{65} + Q_R = 0 \quad (4)$$

$$6 : Q_{36} + Q_{56} + Q_R + Q_{P6} = 0 \quad (5)$$

$$2 : Q_{12} + Q_{32} + Q_{52} + Q_R + Q_{P2} = 0 \quad (6)$$

$$Q_{12} = C_{121} * h_1 + C_{122} * h_2 \quad (7)$$

$$Q_{32} = C_{323} * h_3 + C_{322} * h_2 \quad (8)$$

$$Q_{52} = C_{525} * h_5 + C_{522} * h_2 \quad (9)$$

$$Q_R = R * \Delta x_2 * \Delta y_1 \quad (10)$$

$$Q_{P2} = -0.001; \quad (11)$$

$$2 : C_{121} * h_1 + (C_{122} + C_{322} + C_{522}) * h_2 + \\ C_{323} * h_3 + C_{525} * h_5 + Q_R + Q_{P2} = 0$$

Knotenbilanzen

$$2 : Q_{12} + Q_{32} + Q_{52} + Q_R + Q_{P2} = 0 \quad (13)$$

$$\begin{aligned} 2 : C_{121} * h_1 + (C_{122} + C_{322} + C_{522}) * h_2 + \\ C_{323} * h_3 + C_{525} * h_5 + Q_R + Q_{P2} = 0 \end{aligned} \quad (14)$$

$$2 : a_{21} * h_1 + a_{22} * h_2 + a_{23} * h_3 + a_{25} * h_5 + a_{20} = 0 \quad (15)$$

$$a_{21} = C_{121} \quad (16)$$

$$a_{22} = C_{122} + C_{322} + C_{522} \quad (17)$$

$$a_{23} = C_{323} \quad (18)$$

$$a_{25} = C_{525} \quad (19)$$

$$a_{20} = Q_R + Q_{P2}$$

$$2 : a_{21} * h_1 + a_{22} * h_2 + a_{23} * h_3 + a_{25} * h_5 + a_{20} = 0 \quad (21)$$

$$3 : a_{32} * h_2 + a_{33} * h_3 + a_{36} * h_6 + a_{30} = 0 \quad (22)$$

$$5 : a_{52} * h_2 + a_{54} * h_4 + a_{55} * h_5 + a_{56} * h_6 + a_{50} = 0 \quad (23)$$

$$6 : a_{63} * h_3 + a_{65} * h_5 + a_{66} * h_6 + a_{60} = 0 \quad (24)$$

Knotenbilanzen

$$2 : h_2 = -(a_{21} * h_1 + a_{23} * h_3 + a_{25} * h_5 + a_{20}) / a_{22} \quad (25)$$

$$3 : h_3 = -(a_{32} * h_2 + a_{36} * h_6 + a_{30}) / a_{33} \quad (26)$$

$$5 : h_5 = -(a_{52} * h_2 + a_{54} * h_4 + a_{56} * h_6 + a_{50}) / a_{55} \quad (27)$$

$$6 : h_6 = -(a_{63} * h_3 + a_{65} * h_5 + a_{60}) / a_{66} \quad (28)$$