# QuantIm

# C/C++ Library for Scientific image processing

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1	Intr	oduction and concepts	1
<b>2</b>	Installation and Use in a LINUX/UNIX Environment		<b>2</b>
	2.1	Creating the QUANTIM Library	2
	2.2	Using QUANTIM	2
	2.3	New features of the actual QUANTIM version	2
3	Refe	erence Manual	3
	3.1	Basic image structure	3
	3.2	Image types	3
	3.3	Basic image handling (all types)	4
	3.4	Image conversions	8
	3.5	Image filtering	10
	3.6	Grey scale images (8 and 16 bit) <sup>8,16</sup> (2D and 3D) <sup>2D,3D</sup>	15
	3.7	Binary images	20
	3.8	RGB color images	27
	3.9	Graphics	29
	3.10	Special routines	31
	3.11	Useful stuff	34
	3.12	Functions of previous versions (still active)	37

# **1** Introduction and concepts

QUANTIM was created for analyzing 2-dimensional and 3-dimensional images. When using commercial or free software, it is often hard to understand what is going on exactly when pushing buttons which is unacceptable from a scientific point of view and is why the QUANTIM project was started. An other motivation for the ongoing development of QUANTIM is that it can be used on any computer system, the only requirement is a C/C++ compiler. There is no fancy GUI so you will need some basic knowledge of C/C++ - which actually is not too difficult. To communicate with the rest of the world, the input and output format of QUANTIM is TIFF which is the most common bitmap format. This is established in QUANTIM by using the standard library libtiff and the development files libtiff-dev which are available for any computer platform using a standard package manager or an external file server. It should be installed somewhere in the search path of your computer. 3D-images are handled by QUANTIM as grey level or binary data using an own format but can be converted to vgi or dx (data explorer). The only restriction for the size of images is the RAM of your system. The few routines to produce eps-graphics are based on the excellent library PSgraf3 of Kurt Roth which is automatically installed alongside QUANтIм.

The main features of QUANTIM are:

- Algorithms for 2D/3D grey scale image processing for image filtering and segmentation.
- Algorithms for the quantification of 2D/3D binary images, including methods of mathematical morphology, topological analysis and image intersection.
- Tools to generate 2D/3D random fields with predefined properties.

**Contributors:** Thanks to Uli Weller and Steffen Schlüter for adding some highly useful functions.

# 2 Installation and Use in a LINUX/UNIX Environment

To use the functions of QUANTIM in your own programs, you may directly include the corresponding source files. The preferable way, however, is to link the QUANTIM library to your programs.

# 2.1 Creating the QUANTIM Library

- Copy the directory quantim4\_distribution.tgz from the distribution medium to a convenient place in your file system.
- Extract the archive using
   tar -xvzf quantim4\_distribution.tgz
- Make sure that the libtiff and libtiff-dev packages are installed. These are standard package that you can retrieve from your prefered package manager or directly in a terminal (Debian or Ubuntu) by:
  - > sudo apt-get install libtiff4 libtiff4-dev
- Create the library by
  - $> cd quantim_distribution$
  - > sh install.sh

This will create the file libQuantim4.a in your source directory and move the library libQuantim4.a and the header file quantim4.h to the standard search path directories /usr/local/lib and /usr/local/include. This step requires root privileges.

Good luck!

# 2.2 Using QUANTIM

To use QUANTIM include the header quantim4.h into your program. Then, if the library libQuantim4.a has been copied to a place in the search path of the compiler, compile the program with the option -lQuantim4 -ltiff -lPSgraf3 -lm, for example

g++ -o program myProgram.c -lQuantim4 -ltiff -lPSgraf3 -lm If the compiler cannot find the library and/or the header file, you must include the paths explicitly. Assuming that you have copied the library to /a/b/c/d, and the header file to /x/y the program can be compiled as

g++ myProgram.c -L/a/b/c/d -I/x/y -lQuantim4 -ltiff -lPSgraf3 -lm

# 2.3 New features of the actual QUANTIM version

QUANTIM4 has been modified substantially so that programs written for previous versions may not compile with this version of QUANTIM. This has been sacrificed for a more intuitive structure of image variables, the possibility to handle 16-bit images and the usage of the same functions for different image types (2D, 3D, grey scale, color-rgb). Especially GetImage and SaveImage is now LoadImage and StoreImage, while most of the old function are still included.

# **3** Reference Manual

# 3.1 Basic image structure

All images are identified by a structure of variables defined in quantim4.h:

```
typedef struct
{
  char name[127];
  char itype[5];
  unsigned char *pix;
  unsigned int ndim;
  unsigned int nchannel;
  unsigned int *dim;
  double *res;
  unsigned int numbits;
  unsigned int numbits;
  limage_cc;
```

name	Image name without any extension.
itype	Image type gry=grey scale, gry16=16bit/pixel grey scale,
	rgb=RGB-image, ddd= 3D grey scale, ddd16= 3D grey scale
	16 bit/pixel, btd=3D  binary, doub= double precision  2D  (only)
	for internal use), doub3= double precision 3D (only for inter-
	nal use).
*pix	Pointer to the image data stored sequentially row by row.
ndim	Number of dimensions.
nchannel	Number of channels per pixel.
*dim	Array of ndim elements containing the size of the image in
	each dimension.
*res	Array of ndim elements containing the size of a pixel in each
	dimension.
numbits	Number of bits per pixel.
numbytes	Number of bytes per pixel.

Note that QUANTIM can only handle data in little Endian byte order (Intel byte order), i.e. where the most significant bit arrives last. Moreover, QUANTIM assumes an index order in which x changes fastest. 16-bit data has to be unsigned, i.e. the gray values are only allowed to be in the range [0;65535].

# 3.2 Image types

QUANTIM handles the following types of images:

- 2D grey-scale \*.tif 8 bits/pixels or 16 bits/pixels
- 2D binary \*.tif also 8 bit/pixels but the pixel values are typically only 0 (black) or 255 (white).

- 2D rgb-images \*.tif 3 channels á 8 bit/pixels, byte1=red, byte2=green, byte3=blue.
- **3D** grey scale \*.ddd 8 bit/voxel [0,255] (internal format of QUANTIM).
- **3D grey scale \*.ddd16** 16 bit/voxel [0,255] (internal format of QUAN-TIM).
- 3D grey scale \*.raw 16 bit/voxel unsigned int with \*.vgi or \*.mhd description file.
- **3D grey scale \*.vol** 32 bit/voxel float with \*.vgi description file. This type is internally converted to 16-bit integer.
- **3D binary \*.btd** 1 bit/voxel [0,1] (internal format of QUANTIM)

### **3.3** Basic image handling (all types)

### image\_cc \*LoadImage(char \*buf)

Loads images of any type.

bufName of the image to be loaded (with or without extension).return value:pointer to the loaded image.

#### image\_cc \*LoadMetaImage(char \*buf)

Loads 3D images in the standard file format of ITK, where \*.mhd contains the meta data and \*.raw contains the binary block of raw data.

buf Name of the image to be loaded (with or without .mhd extension).

return value: pointer to the loaded image.

#### 

Loads 3D raw images, where the meta information is given by arguments. Little Endian byte order and unsigned data required.

buf	Name of the image to be loaded (with extension).
cols	Number of columns (voxels in x dimension).
rows	Number of rows (voxels in y dimension).
layers	Number of layers (voxels in z dimension).
offset	Byte offset to the first voxel, e.g. 64 for *.ddd images.
nbytes	Number of bytes per voxel (1 for 8-bit, 2 for 16-bit).
return value:	pointer to the loaded image.

#### void StoreImage(image\_cc \*im, char \*buf)

Saves the images of any type.

im Pointer to the image.

buf Name of the image to be saved.

#### void StoreMetaImage(image\_cc \*im, char \*buf)

#### void StoreMetaImage(image\_cc \*im)

Saves a 3D image of any type in ITK MetaImage format (\*.mhd and \*.raw). Images with btd format (1-bit) are converted into ddd images (8-bit).

im	Pointer to the image.
buf	Name of the image to be saved. When function is used with
	*buf, im-¿name is used as file name instead.

# void StoreRaw(image\_cc \*im, char \*buf) void StoreRaw(image\_cc \*im)

Saves a 3D image of any type in raw format (\*.mhd and \*.raw). Images with btd format (1-bit) are converted into ddd images (8-bit). Important meta information is stored in a textfile with the same name.

im	Pointer to the image.
----	-----------------------

buf Name of the image to be saved. When function is used with \*buf, im-¿name is used as file name instead.

#### void SavePaletteImage(image\_cc \*im, char \*buf)

Saves an 8-bit image (only 2D grey scale) to a Palette Color TIFF-file.

im	Pointer to the image.
buf	Name of the tiff-image to be saved.

#### void SavePrinciplePlanes(image\_cc \*im, char \* name)

Saves the central 2D planes (xy, xz, yz) of a 3D image using the given name.

im	Pointer to the 3D image.
name	Name of resulting 2D images: 'plane_[xy,xz,yz]_name'

#### image\_cc \*InitImage(int x, int y, int val, char \*type)

image\_cc \*InitImage(int x, int y, int z, int val, char \*type)

#### image\_cc \*InitImage(image\_cc \*im, int val)

#### image\_cc \*InitImage(image\_cc \*im)

Initiates a new image and allocates the required memory.

x,y,(z)	Number of pixels in x, y, and z direction.
val	Initial value of each pixels.
im	image whose structure (dimensions aso) is copied.
type	Type of image (optional): gry=grey scale, gry16=16 bits grey
	scale, rgb=RGB-image, ddd= 3D grey scale, , xxd= multi-
	dimensional grey scale, $btd = 3D$ binary. The default type is
	8-bit grey scale for 2D and 3D.
return value:	Pointer to the new image.

#### image\_cc \*InitRandImage(int col, int row, double rx, double ry, double cx, double cy, int mode, double \*cdf)

- image\_cc \*InitRandImage(int col, int row, int dep, double rx, double ry, double rz, double cx, double cy, double cz, int mode, double \*cdf)
- Returns a random 2D or 3D image optionally with defined grey distribution function (equal distribution, Gauss or predefined by a given cdf), defined correlation length and defined correlation model (Gauss, Lorentz, Exponential, von Karman).

col, row, dep	dimensions of the generated image
rx, ry, rz	size of pixel in x, y, z
cx, cy, cz	correlation lengths (number of pixel) in x, y, z
mode	0: equal distribution without any correlation (cx,cy,cz and cdf
	have no meaning here)
	1: equal grey distribution with gaussian correlation
	2: predefined grey distribution (cdf) and gaussian correlation
	3: Gaussian correlation (cdf have no meaning here)
	4: Lorentz-Correlation model (cdf have no meaning here)
	5: Exponential-Correlation model (cdf have no meaning here)
	6: von Karman-Correlation model (cdf have no meaning here)

*cdf	cdf of grey levels
return value:	pointer to the generated image

#### image\_cc \*CopyImage(image\_cc \*im)

Makes a copy of an image.

\*im Pointer to the original image.return value: Pointer to the copy.

#### void DeleteImage(image\_cc \*im)

Delete an image and deallocate memory.

im Pointer to the image.

int rPixel(unsigned long i, image\_cc \*im)

int rPixel(int x, int y, image\_cc \*im)

int rPixel(int x, int y, image\_cc \*im, unsigned char \*value, unsigned char \*value, unsigned char \*value)

- int rPixel(int x, int y, image\_cc \*im, unsigned char \*value)
- int rPixel(int x, int y, int z, image\_cc \*im)

Reads the value of a pixel.

i	offset of the pixel within the stored 1-D array of image data
	(for 2d and 3d images).
x, y, z	Coordinates of the pixel.
im	Pointer to the image.

*value	Address to which the pixel values are written. For RGB im-
	ages a pointer to a 3-element array containing the RGB values
	is also possible.

return value: Value of the pixel, or 1/3(R+G+B) for rgb-images.

void wPixel(unsigned long i, image\_cc \*im, int value)

void wPixel(int x, int y, image\_cc \*im, int value)

void wPixel(int x, int y, image\_cc \*im, int value, int value, int value)

void wPixel(int x, int y, image\_cc \*im, int \*value)

void wPixel(int x, int y, int z, image\_cc \*im, int value)

Write a value to a pixel.

offset of the pixel within the stored 1-D array of image data
(for 2d and 3d images).
Coordinates of the pixel.
Pointer to the image.
value(s) to be written, number of given values corresponds to
the number of channels per pixel
For RGB images a pointer to a 3 element array containing the
RGB values.

#### void InvertImage(image\_cc \*im)

Inverts an image.

im Pointer to the image.

void FlipImage(image\_cc \*im, int mode)

Flips an image (only 2D).

im	Pointer to the image.
mode	0=horizontal, $1=$ vertical flip.

#### void RotateImage(image\_cc \*im, int mode)

Rotates an image (only 2D) by  $90^{\circ}$  or  $180^{\circ}$ .

im Pointer to the image. mode  $-1=90^{\circ}$  counter clock wise,  $1=90^{\circ}$  clock wise,  $0=180^{\circ}$ .

void TurnImage(image\_cc \*im, double grad)

Rotates an image (only 2D) by a given angle.

im	Pointer to the image.
grad	angle in degrees.

image\_cc \*ImageSegment(image\_cc \*image, int ulx, int uly, int dx, int dy)

image\_cc \*ImageSegment(image\_cc \*image, int ulx, int uly, int ulz, int dx, int dy, int dz)

Cut a rectangular segment out of an image.

image Pointer to the image.

ulx,uly,(ulz) x,y,z coordinates of the upper left corner of the segment.dx,dy,(dz) size of the segment in x,y,z direction (number of pixels).return value: Pointer to the segment.

image\_cc \*GetPlane(image\_cc \*im, int plane, int mode) Extracts a 2D plane from a 3D image

im	Pointer to the 3D image.
plane	x,y or z coordinate of the plane.
mode	direction of the plane $0=xy$ , $1=yz$ , $2=xz$ .
return value:	Pointer to the 2D image.

#### void SetFrame(image\_cc \*im, int value)

Writes the edges of an image to a certain value.

*im	Pointer to the image.
value	Value to be written at the edges

#### image\_cc \*ChangeResolution(image\_cc \*image, int newx, int newy)

Rescales an image to the new dimensions **newx** and **newy**. (Only for 2D images, rgb and grey).

*image	Pointer to the original image
newx, newy	new dimensions in x and y direction
return value:	pointer to a rescaled image

#### image\_cc \*Diff(image\_cc \*wnd1,image\_cc \*wnd2)

Returns an image of the absolute differences between two images.

*wnd1,*wnd2	Pointer to the original images of any type.
return value:	Pointer to the resulting image.

#### **3.4** Image conversions

#### image\_cc \*bit16to8(image\_cc \*image)

Converts a 16-bit grey scale image to a 8-bit image

*image	Pointer to the original image.
return value:	Pointer to the resulting image.

#### image\_cc \*Btd2Ddd(image\_cc \*image)

Converts a btd-image (1 bit/voxel) to a ddd-image (1 byte/voxel).

*image	Pointer to the binary image
return value:	Pointer to the corresponding ddd-image

#### image\_cc \*RGBtoGray(image\_cc \*image)

Converts a RGB-3byte-color image to a 8bit-grey scale image.

image	Pointer to the RGB-image
return value:	pointer to the converted grey scale image.

# void DDD2Dx(image\_cc \*image, char \*buf);

Generates a description file for DX named toto.general. The file name (toto) which is provided through **buf** must be the same name as was used to save the ddd image using StoreImage(). Note that the image resolution should be set correctly.

*image	Pointer to the ddd-image
*buf	name of the ddd images (without extension)
return value:	no return value, a dx description file *.general is produced.

### image\_cc \*Ddd2Btd(image\_cc \*im);

Converts a ddd-image to a btd-image. All non-zero voxels are set to 1 the others stay at 0.

*image	Pointer to the ddd-image
return value:	pointer to the resulting btd-image.

### 3.5 Image filtering

#### void Mean(image\_cc \*im, int size)

Mean filter using a squared window

im	Pointer to the image.
size	sidelength of squared filter: $2 \cdot \text{size} + 1$ pixel.

#### image\_cc \*MeanVar(image\_cc \*im, int size)

Same as Mean but the variance within the squared window is returned as a new image

im	Pointer to the image.
size	sidelength of squared filter: $2 \cdot \text{size} + 1$ pixel.
return value:	Pointer to the image of variances

#### void Gauss(image\_cc \*im, int size, double sig)

Gauss filter using a squared window with side length  $2 \cdot \text{size} + 1$  pixel.

im	Pointer to the image.
size	Sidelength of squared filter: $2 \cdot \text{size} + 1$ pixel.
sig	Variance of Gauss filter.

#### void DiffGauss(image\_cc \*im, int size, double sig, double sig2)

Difference of Gaussian (DoG) filter using a squared window with side length 2.size+1 pixel. At the same time the image is smoothed by a Gauss filter with low sig while edges are enhanced by adding the difference to a strongly smoothed image sig2 at each location (The difference is highest at edges).

im	Pointer to the image.
size	Sidelength of squared filter: $2 \cdot \text{size} + 1$ pixel.
sig	Small variance of Gauss filter.
sig2	Big variance of Gauss filter.

#### void UnsharpMask(image\_cc \*im, int size, double sig)

Edge enhancement filter using a squared window with side length 2·size+1 pixel. Same rationale as a Difference of Gaussian filter (see above) but here the local grey value difference due to convolution with Gaussian kernel of sig is directly added to the image. This is faster but may enhance noise at the same time.

im	Pointer to the image.
size	Sidelength of squared filter: $2 \cdot \text{size} + 1$ pixel.
sig	Variance of Gauss filter.

#### void MinMax(image\_cc \*im, double size, int mode)

Minimum-Maximum filter for grey scale images with a circular/spherical kernel where size is in length units of the image according to im - >res[0]. This filter corresponds to grey scale erosion/dilation

im	Pointer to the image.
size	Radius of the circular/sherical filter

mode 0 is minimum filter, else maximum.

#### void Luul(image\_cc \*im, double size)

Combined Minimum-Maximum filter: lower-upper-upper-lower for grey scale images with a circular/spherical kernel where size is in length units of the image according to im - >res[0]. This filter corresponds to grey-scale opening, the result is similar to the median but Luul is more efficient.

im	Pointer to the image.
size	Radius of the circular/sherical filter in pixel

#### void Ullu(image\_cc \*im, double size)

Combined Minimum-Maximum filter: upper-lower-lower-upper for grey scale images with a circular/spherical kernel where size is in length units of the image according to  $im - \operatorname{res}[0]$ . This filter corresponds to grey-scale closing, the result is similar to the median but Ullu is more efficient (The result of the Median filter is between Luul and Ullu).

im	Pointer to the image.
size	Radius of the circular/sherical filter in pixel

#### void pseudoMad(image\_cc \*orig, double size)

#### void pseudoMad(image\_cc \*orig, image\_cc \*\*pMed, double size)

pseudo Median absolute deviation The median absolute deviation is the median of the absolute differences towards the median. For reason of speed the median is replaced by the luul filter.

orig	pointer to original image
pMed	pointer to pointer to image containing the luul filtered image.
	If NULL, this will be created (and the pointer set to the new
	image).
size	radius of spherical window to use.

# image\_cc \*MajorityFilter(image\_cc \*im, image\_cc \*roi, int nr, int wnd, double maj, double rel)

The current label is replaced by the most representative label among all neighbors in a cubic kernel, if (i) the most representative label exceeds a certain majority and (ii) the number exceeds that of the current label at the central voxel by a certain percentage

im	Pointer to the image.
roi	Pointer to the binary image that represents the region of in-
	terest (optional).
nr	Number of labels in the image
wnd	sidelength of cubic window: $2 \cdot \text{wnd} + 1$ pixel.
maj	majority [0-1]
rel	relative majority with respect to current label

return value: Pointer to the filtered image

#### void FastMedian(image\_cc \*im, int size)

Median filter using a cubic window with fast updating of entries when the window is moved by one position. The running median method is adapted from Ashelly and distributed under the MIT License (MIT) (https://gist.github.com/ ashelly/5665911)

im	Pointer to the image.
size	sidelength of cubic filter: $2 \cdot \text{size} + 1$ pixel

# void TotVarFilter(image\_cc \*im, double timestep, double lambda, int maxstep, int interval, int function)<sup>3D</sup>

This filter minimizes the total variation while keeping a maximal fidelity to the original image (only 3D). The strength of fidelity is given by lambda. Method is according to Rudin, Fatemi, Osher (1992): Physica A,60,259-268.

im	Pointer to the image.
timestep	timestep for each filtering. If negative, will be handled dy-
	namically0.1 normally works well.
lambda	fidelity parameter. 5 is a good start.
maxstep	maximal number of filtering steps.
interval	number of steps after which the image in memory will be
	updated.
function	kernel functions for filtering. 0: classical Total variation, 1:
	Entropy, 2: Enhanced entropy

# void AnisoDiffFilter(image\_cc \*im, int maxstep, double threshold, double sigma)<sup>3D</sup>

Anisotropic (or non-linear) diffusion filter according to Catté et. al (1992) SIAM Journal on Numerical Analysis, 29(1), 82-193.

maxstep	maximal number of filtering steps.
threshold	diffusion stop criterion - gradients larger than this are con-
	served
sigma	standard deviation of the Gaussian kernel for smoothing prior
-	to edge evaluation

#### void Bin(image\_c \*im, int thresh)

void Bin(image\_cc \*im, int thresh, int lower, int upper)

Binarization of an image according to a threshold value. Grey values  $\leq$  thresh are set to lower the others to upper. If no explicite values for lower and upper are given, this is equivalent to lower=0 and upper= maximum grey level. If the value of upper is larger than the maximum possible grey value, the original grey values above thresh are maintained.

im	Pointer to the image.
thresh	Threshold value
lower	Value written to pixel $\leq$ thresh

Value written to pixel > thresh

#### void BinBand(image\_cc \*im, int lthresh, int uthresh)

Binarization of an image according to 2 threshold values. Values  $\geq$  1thresh and  $\leq$  uthresh are set to 0, the others to the maximum grey level.

im	Pointer to the image.
lthresh	Lower threshold value
uthresh	Upper threshold value

upper

#### void BinBilevel(image\_cc \*im, int lower, int upper)

Segmentation of an image according to 2 thresholds which are regarded to be the limits of a fuzzy region within which the 'true' threshold is expected. The threshold is chosen locally according to the values of the neighboring pixel values. All pixel of a grey level  $\leq 1 \text{ower}$  are written to 0 as well as all pixel  $\leq \text{upper}$  having at least one direct neighbor  $\leq 1 \text{ower}$ . The other pixel keep their original values. This rule is applied iteratively until no pixel has to be changed anymore.

im	Pointer to the image.
lower	Lower threshold.
upper	Upper threshold.

#### image\_cc \*DddBin(image\_cc \*im, int thresh)

Binarization of a ddd-image according to a single threshold values. The result is converted to a btd-image voxels are set to 0 for values  $\leq$  thresh and t 1 else.

im	Pointer to the ddd-image.
thresh	threshold value
return value:	Pointer to the binary btd-image

#### image\_cc \*Sobel(image\_cc \*im)

#### image\_cc \*Sobel(image\_cc \*im, image\_cc \*maskim)

Sobel filter (first derivative of local grey levels). The image border is set to 0. If an additional binary image maskim of same dimensions is provided, the evaluation is only done for regions where maskim is non-zero.

\*im Pointer to the image.return value: Pointer to the filtered image

#### image\_cc \*Laplace(image\_cc \*im, int mode)

#### image\_cc \*Laplace(image\_cc \*im, int mode,image\_cc \*maskim)

Laplace filter (second derivative of local grey levels). The image border is set to 0. For mode=1 only positive Laplacians are stored, for mode=2 only negative and for mode=3 both. If an additional binary image maskim of same dimensions is provided, the evaluation is only done for regions where maskim is non-zero.

\*im Pointer to the image.

modeindicates which sign is to be considered (bit1=positive, bit2=negative).return value:Pointer to the filtered image

# 3.6 Grey scale images (8 and 16 bit)<sup>8,16</sup> (2D and 3D)<sup>2D,3D</sup>

#### double \*Histo(image\_cc \*im)<sup>8</sup> <sup>2D,3D</sup>

#### double \*Histo(image\_cc \*im, image\_cc \*mask)

Returns the histogram (pdf) of an image (16-bit images are converted to 8-bit prior to the evaluation). Optionally, a histogram is only calculated for locations where the mask image is white.

*image	Pointer to the grey image.
*mask	Pointer to the mask image
return value:	Pointer to the histogram (256 element array).

# double \*GreyCdf(image\_cc \*im)<sup>8</sup> <sup>2D,3D</sup>

#### double \*GreyCdf(image\_cc \*im, image\_cc \*mask)

Returns a 256 element array containing the cdf (cumulative histogram) of grey levels. Optionally, a cdf is only calculated for locations where the mask image is white.

*im	Pointer to the grey image
*mask	Pointer to the mask image
return value:	cdf array (256 elements)

### void StretchHisto(image\_cc \*image, int Low, int High) void StretchHisto(image\_cc \*image, double th) void StretchHisto(image\_cc \*image)

Scales the histogram of a grey scale images (2D and 3D, 8-bit and 16-bit). Grey values between Low and High are mapped on a grey scale between 0 and the maximum value  $2^8$  or  $2^{16}$  for 8-bit or 16-bit images respectively. Values lower than Low are set to 0, values higher than High are set to the maximum value. If the parameters Low and High are replaced by th the limits are set to lower and upper th percent of existing values. If no additional argument is given, the histogram ist rescaled according to the minimum and maximum value of the original image (corresponding to th=0). To match the grey values to a smooth histogram a suitable random value is added to rescaled values.

*image	Pointer to the image
Low	lower threshold
High	upper threshold

#### void HistoMatch(double \*cdf, image\_cc \*image)<sup>8</sup>

Transforms the histogram of an image according to a predefined cdf, typically optained from a source image using the function GreyCdf().

*cdf	predefined cdf of grey levels
*image	Pointer to the 2D grey scale image
return value:	no return value

#### int UnimThresh(double \*histo, int mode);

Threshold detection in a unimodal histogram typically obtained by Histo via triangulation according to Rosin(2001):Pattern Recognition,34,2083-2096. The threshold is located at the characteristic knee of the histogram, which has the largest perpendicular distance to an imaginary line connecting the mode with the brightest grey value (mode=1) or the darkest grey value (mode=0).

*histo	8bit grey value frequency distribution
mode	0=right tail, 1=left tail
return value:	threshold value

#### int KMeansThresh(double \*histo, int nr);

Iterative Threshold Selection Method according to Ridler & Calvard (1978): IEEE Transactions on Systems, Man, and Cybernetics,8(8),630-632. Starting from an arbitrary set of thresholds, the arithmetic mean of adjacent class means is iteratively set as a new threshold until all thresholds converge to a stable values.

*cdf	8bit grey value frequency distribution
return value:	threshold value

# int \*ShapeThresh(double \*cdf, int nr, double tau)

#### int \*ShapeThresh(double \*cdf, int nr, double tau, double perc)

Multilevel thresholding by local minima search according to Tsai (1995): Pattern Recognition ,16(6),653-666. Local maxima of histogram curvature are detected in addition, if there are less peaks than the specified number of classes.

*cdf	8bit cumulative grey value frequency distribution
nr	number of classes
perc	percentile that sets a fuzzy region around the optimal grey
	threshold
return value:	pointer to vector of nr-1 thresholds or 3(n-1) thresholds if
perc	is set

#### int \*FuzzyCMeansThresh(double \*cdf, int nr, double tau)

## int \*FuzzyCMeansThresh(double \*cdf, int nr, double tau, double perc)

Multilevel thresholding by fuzzy c-means clustering according to Jawahar et al. (1997): Pattern Recognition ,30(10),1605-1613.

*cdf	8bit cumulative grey value frequency distribution
nr	number of classes
tau	fuzzyness index $[1,\infty)$ . Method equals k-means clustering if
	au = 1.
perc	percentile that sets a fuzzy region around the optimal grey
	threshold
return value:	pointer to vector of nr-1 thresholds or 3(n-1) thresholds if
perc	e is set

### int \*MaxVarThresh(double \*cdf, int nr);

#### int \*MaxVarThresh(double \*cdf, int nr, double perc)

Multilevel thresholding by maximizing between-class variance (Otsu method) according to Liao et al. (2001):Journal of Information science and Engineering, 17, 713-727.

*cdf	8bit cumulative grey value frequency distribution
nr	number of classes
perc	percentile that sets a fuzzy region around the optimal grey
	threshold
return value:	pointer to vector of nr-1 thresholds or 3(n-1) thresholds if
pero	z is set

#### int \*MaxEntroThresh(double \*cdf, int nr) int \*MaxEntroThresh(double \*cdf, int nr, double po

# int \*MaxEntroThresh(double \*cdf, int nr, double perc)

Multilevel thresholding by maximizing the sum of histogram entropy of each class according to Kapur et al. (1985):Computer Vision, Graphics and Image Processing, 29, 273-285.

*cdf	8bit cumulative grey value frequency distribution
nr	number of classes
perc	percentile that sets a fuzzy region around the optimal grey
	threshold
return value:	pointer to vector of nr-1 thresholds or 3(n-1) thresholds if
perc	is set

### int \*MinErrThresh(double \*cdf, int nr)

int \*MinErrThresh(double \*cdf, int nr, double perc)

Multilevel thresholding by minimizing the overlap error of fitted Gaussians according to Kittler & Illingworth (1986): Pattern Recognition ,19(1),41-47.

*cdf	8bit cumulative grey value frequency distribution
nr	number of classes
perc	percentile that sets a fuzzy region around the optimal grey
	threshold
return value:	pointer to vector of nr-1 thresholds or 3(n-1) thresholds if
perc	is set

# int \*GradMaskThresh(image\_cc \*image, double alpha)

 $int \ *GradMaskThresh(image\_cc \ *image, \ double \ alpha, \ image\_cc \ *mask)$ 

Thresholding with gradient masks according to Schlüter et al. (2010): Computers & Geosciences, 36, 1246-51. Only locations along edges are taken into consideration for detection of an upper threshold. The lower threshold is calculated subsequently from simple histogram statistics.

\*image Pointer to the grey value image

alpha	defines the width of a fuzzy threshold range. Usually set be-
	tween one and two.
*mask	Pointer to the mask image (optional)
return value:	pointer to vector of two thresholds (lower and upper thresh-
old)	

### image\_cc \*WaterShed(image\_cc \*image, int conmode)<sup>8</sup> <sup>2D,3D</sup>

Calculates the watershed lines for a grey image (only 8-bit images). The different basins separated by the watershed lines are marked by different grey values (2D) or by a single grey value (3D), the watershed line is 0. This may be applied to a distance map of a binary image to separate overlapping grains.

*image	Pointer to the grey image
conmode	Connectivity mode: either 4 or 8 $(2D)$ and 6 or 26 $(3D)$ .
return value:	Pointer to the image containing the watershed and the basins

double \*Acov(image\_cc \*im, double \*corl, int lag, int mode)<sup>8</sup>  $^{2D,3D}$ Returns the autocovariance function of a 2D grey image

*im	Pointer to the image
*corl	address to write the correlation length as result
lag	maximum distance to evaluate $(\# \text{ pixels})$
mode	indicates which directions are to be considered (bit1=x, bit2=y,
	bit3=z)
return value:	pointer to an array of dimension lag where the autocovariance
function is stored	

double \*SemiVar(image\_cc \*im, int lag, int mode)<sup>8</sup>  $^{2D,3D}$ 

Returns the semi-variance function of a grey scale image.

*im	Pointer to the image
*corl	address to write the correlation length as result
lag	maximum distance to evaluate $(\# \text{ pixels})$
mode	indicates which directions are to be considered (bit1=x, bit2=y,
	bit3=z)
return value:	pointer to an array of dimension lag where the semi-variance
funct	tion is stored

# long \*GreyConFunc(image\_cc \*image, int mode)<sup>8</sup> <sup>2D,3D</sup>

Returns the connectivity function of a grey scale image. The image is binarized for all possible thresholds [0,255] and the corresponding Euler number is dermined which is returned as a vector of 255 elements. The Euler numbers are not normalized by the size of the image.

*image	Pointer to the grey image
mode	Connectivity mode for values $<$ grey threshold: 4 or 8 (2D),
	6 or 26 (3D)

return value: array of 255 Euler numbers

image\_cc \*CircMask(image\_cc \*im, int xmid, int ymid, int rad)<sup>8,16</sup> <sup>2D,3D</sup> Cuts out a circular (2D) or cylindrical (3D) image with center xmid, ymid and radius rad. All pixels outside the circle are set to the maximum grey level.

*image	Pointer to the grey image
xmid, ymid	center coordinates of the circle
rad	radius of the circle
return value:	Pointer to the resulting image

#### **3.7** Binary images

# image\_cc \*ErodeCirc(image\_cc \*image, double rad, int mode) image\_cc \*ErodeDist(image\_cc \*image, double rad, int mode)

Performs an erosion or dilation of a binary image using a circular/spherical structuring element. The radius of this element is given in number of pixels in xdirection (this might be relevant for unisotropic pixel geometry). The function ErodeDist is based on the entire distance map of the image and is more efficient for large structuring elements, while ErodeCirc evaluates only individual structuring elements which is more efficient for small rad

*image	Pointer to the image.
step	radius of the structuring element (in x-pixel)
mode	0 = erosion, $1 =$ dilation of the black phase
return value:	Pointer to the resulting image

# image\_cc \*OpenCirc(image\_cc \*im, double rad, int mode) image\_cc \*OpenDist(image\_cc \*im, double rad, int mode)

Performs a morphological opening or closing of a binary image using a circular/spherical structuring element. The radius of this element is given in number of pixels in x-direction (this might be relevant for unisotropic pixel geometry). The function OpenDist is based on the entire distance map of the image and is more efficient for large structuring elements, while OpenCirc evaluates only individual structuring elements which is more efficient for small rad

*image	Pointer to the image.
step	radius of the structuring element
mode	0 = opening of the black phase, $1 = $ closing of the black phase
return value:	Pointer to the resulting image

#### image\_cc \*GetDistMap(image\_cc \*image)

Generates the distance map of a binary image, which is a grey scale image where the grey value of each pixel indicates the orthogonal distance to the black-white interface. The resulting image is in 16bit grey scale. The Euclidian distance is calculated in number of pixels in x-direction and is rounded up to the next integer x. Hence the distance map has values of 32768+/-x while the value 32768 representing the black-white interface does not exist. This function can also be used for anisotropic pixel geometry (different resolution in x,y,z). In this case the calculated distances are always in units of number of pixel in x-direction.

*image	Pointer to the binary image.
return value:	Pointer to the resulting image (16bit grey)

#### image\_cc \*GetOpenMap(image\_cc \*distmap, int smax)

Generates the 'opening map' for the black phase of a binary image. This is a grey scale image where the grey value of each pixel indicates the maximum size of

a circle (2D) or a sphere (3D) which is a complete subset of the black phase. The size of the circle/sphere is in number of pixels in x-direction. As input the distance map is used which is generated by GetDistMap(). The generated opening map can be used to calculate the 'opening size distribution' using the function MinkowskiOpenFunctions

*distmap	Pointer to the distance map (16bit grey).
smax	number of opening steps
return value:	Pointer to the resulting opening map

#### void MinkowskiFunctions(image\_cc \*image, char \*outfile)

Calculates all Minkowski-Functions, i.e. Minkowski functionals in dependency of the grey threshold. All possible thresholds are evaluated. This function is typically used for the evaluation of distance maps generated by GetDistMap. The results are written to the file outfile.

*image	Pointer to the input image.
outfile	file name where the results are written to

#### void MinkowskiOpenFunctions(image\_cc \*image, char \*outfile)

void MinkowskiOpenFunctions(image\_cc \*image, image\_cc \*maskim, char \*outfile)

Calculates all Minkowski-Functions for an opening map generated by GetOpenMap, i.e. Minkowski functionals in dependency of the opening size. If an additional binary image maskim of same dimensions is provided, the evaluation is only done for regions where maskim is non-zero. The results are written to the file outfile.

*image	Pointer to the input image.
gstep	scaling of the grey levels of the opening maps
pixstep	evaluated sizes in unit of pixel
outfile	file name where the results are written to

#### long int \*m2Quant(image\_cc \*image)

#### long int \*m2Quant(image\_cc \*image, image\_cc \*maskim)

Calculates the frequency distribution of 16 different pixel configurations in a 2x2 square. The returned pointer is input for the routines to calculate Minkowski functionals: volume density, surface density, length density, and Euler number. If another binary 'mask' is provided (maskim) having the same dimensions as image, the evaluation is done only for regions where maskim is not zero.

*im	Pointer to the binary 2D-image.
*maskim	Pointer to the image containing a mask.
return value:	Pointer to the 16-element array containing frequencies of pixel
configurations	

long int \*m3Quant(image\_cc \*image)

#### long int \*m3Quant(image\_cc \*image, image\_cc \*maskim)

Calculates the frequency distribution of 256 different voxel configurations in a 2x2x2 cube. The returned pointer is input for the routines to calculate Minkowski functionals: volume density, surface density, curvature density and Euler number. If another binary 'mask' is provided (maskim) having the same dimensions as image, the evaluation is done only for regions where maskim is not zero. NOTE THAT 3-dimensional Minkowski functionals treat the white phase (btd values = 1) as foreground which is in contrast to the 2-dimensional version (just to keep you flexible).

\*im Pointer to the binary 3D-image in btd-format.
 return value: Pointer to the 256-element array containing frequencies of voxel configurations

#### double m2areadens(image\_cc \*image, long int \*h);

Returns the area density of a 2D binary structure (black phase) which corresponds to the volume density of a 3D structure as estimated from the 2-dimensional section.

**\*h** Pointer to the array of pixel configurations obtained by m2Quant() return value: Volume density  $[L^2/L^2]$ 

#### double m2lengthdens(image\_cc \*image, long int \*h);

Returns the length density  $B_A$  [L/L<sup>2</sup>] of the boundary per area of a 2D binary structure. The units of L are given in the units of image resolution (image - >res[]).

\*hPointer to the array of voxel configurations obtained by m2Quant()\*imagePointer to a 2D binary image (0=black, 255=white)return value:Length density [L/L<sup>2</sup>]

#### double m2surfdens(image\_cc \*image, long int \*h);

Returns the surface density  $S_V [L^2/L^3]$  of the black-white interface of a 3D binary structure. The evaluated image is considered to be a 2-dimensional section through that 3D structure. The units of L are given in the units of image resolution (image – >res[]).

*h	Pointer to the array of pixel configurations obtained by m2Quant()
*image	Pointer to a 2D binary image (0=black, 255=white)
return value:	Surface density $[L^2/L^3]$

#### double m2euler4(image\_cc \*image, long int \*h);

- Returns the Euler number  $\chi_A$  [1/L<sup>2</sup>] of a 2D binary structure considering 4connectivity of the black phase. The units of L are given in the units of image resolution (image->res[]).
  - \*hPointer to the array of pixel configurations obtained by m2Quant()\*imagePointer to a 2D binary image (0=black, 255=white)

return value: Euler number  $[1/L^2]$ 

#### double m2euler8(image\_cc \*image, long int \*h);

Returns the Euler number  $\chi_A$  [1/L<sup>2</sup>] of a 2D binary structure considering 8connectivity of the black phase. The units of L are given in the units of image resolution (image – >res[]).

*h	Pointer to the array of pixel configurations obtained by m2Quant()
*image	Pointer to a 2D binary image (0=black, 255=white)
return value:	Euler number $[1/L^2]$

#### double m3voldens(long int \*h);

Returns the volume density of a 3D binary structure (white phase).

*h	Pointer to the array of voxel configurations obtained by m3Quant()
*image	Pointer to a 3D binary image in btd-format $(0=black, 1=white)$
return value:	Volume density $[L^3/L^3]$

#### double m3surfdens(image\_cc \*image, long int \*h);

Returns the surface density  $S_V [L^2/L^3]$  of the black-white interface of a 3D binary structure. The units of L are given in the units of image resolution (image->res[i]).

*h	Pointer to the array of pixel configurations obtained by m3Quant()
*image	Pointer to a 3D binary image in btd-format (0=black, 1=white)
return value:	Surface density $[L^2/L^3]$

#### double m3meancurv(image\_cc \*image, long int \*h);

Returns the mean curvature density  $C_V$  [L/L<sup>3</sup>] of the black-white interface of a 3D binary structure. The units of L are given in the units of image resolution (image – >res[]).

*h	Pointer to the array of pixel configurations obtained by m3Quant()
*image	Pointer to a 3D binary image in btd-format (0=black, 1=white)
return value:	Curvature density $[L/L^3]$

#### double m3euler6(image\_cc \*image, long int \*h);

Returns the Euler number  $\chi_V$  [1/L<sup>3</sup>] of a 3D binary structure considering 6connectivity of the white phase. The units of L are given in the units of image resolution (image – >res[]).

*h	Pointer to the array of voxel configurations obtained by m3Quant()
*image	Pointer to a 3D binary image in btd-format (0=black, 1=white)
return value:	Euler number $[1/L^3]$

#### double m3euler26(image\_cc \*image, long int \*h);

Returns the Euler number  $\chi_V$  [1/L<sup>3</sup>] of a 3D binary structure considering 26connectivity of the white phase. The units of L are given in the units of image resolution (image – >res[]).

*h	Pointer to the array of voxel configurations obtained by m3Quant()
*image	Pointer to a 3D binary image in btd-format (0=black, 1=white)
return value:	Euler number $[1/L^3]$

#### image\_cc \*LogAnd(image\_cc \*wnd1, image\_cc \*wnd2)

Logical AND relation (intersection) of two binary images.

wnd1	Pointer to the first image description structure.
wnd2	Pointer to the second image description structure.
return value:	Pointer to the resulting image

#### image\_cc \*LogOr(image\_cc \*wnd1, image\_cc \*wnd2)

Logical OR relation (unification) of two binary images.

wnd1	Pointer to the first image description structure.
wnd2	Pointer to the second image description structure.
return value:	Pointer to the resulting image

# image\_cc \*Intersection(image\_cc \*wnd1, image\_cc \*wnd2, int gv1, int gv2)

Intersection of two binary images. The black phase of the two images is set to gv1 and gv2 respectively, their intersection is set to black.

wnd1	Pointer to the first image description structure.
wnd2	Pointer to the second image description structure.
gv1	grey level to be set for phase in wnd1.
gv2	grey level to be set for phase in wnd2.
return value:	Pointer to the resulting image

#### void bThinning(image\_cc \*im);

Thinning of 0-phase of a binary image, considering 4-connectivity.

\*im Pointer to the image.

#### void bThinning8(image\_cc \*im);

Thinning of 0-phase of a binary image, considering 8-connectivity.

\*im Pointer to the image.

#### void bConCom(image\_cc \*im,int xv,int yv,int val)

Marking of th connected component which includes the seed point xv yv in a binary image.

*im	Pointer to the image.
xv yv	Seed point of the component.
val	Grey value to mark the conected component.

#### int bConCom2(image\_cc \*image,int xv,int yv);

Determines the size of the connected object identified by greylevel 0 around point xv/yv considering 8-connectivity. Return value is the number of pixels attributed to the object. The original image is not changed.

*image	Pointer to the binary image
xv, yv	coordinates for seed point of the connected component
return value:	number of pixels attributed to the object considering 8-connectivity

#### int isPercol(image\_cc \*image, int backbone, int mode);

returns 1 if the 0-values of a binary structure percolate in the directions indicated by mode (bit1=x, bit2=y, bit3=z). if backbone is not 0 the backbone (or in case of no percolation the continuous part with respect to plane x/y/z=0 indicated by mode) is stored as additional image named 'backbone' if backbone is 0 the calculation is interupted as soon as percolation was detected (which is faster).

*image	Pointer to the binary image	
backbone	if not 0 an image of the continuous part is stored (file name	
	'backbone')	
mode	direction in which percolation is tested	
return value:	1 if the structure percolates, 0 else	

#### image\_cc \*Cluster(image\_cc \*image, int \*nr)

Fast object detection with the Hoshen-Kopelman algorithm, as implemented by Tobin Fricke and distributed under GNU public license (http://www.ocf. berkeley.edu/~fricke/projects/hoshenkopelman/hoshenkopelman.html). Each isolated white objects gets a different grey value label and the label image is returned.

*image	Pointer to the binary image
*nr	Pointer to integer where number of objects is written
return value:	image with object labels

#### void RemoveObjects(image\_cc \*image, int size, int mode)

void RemoveObjects(image\_cc \*image, image\_cc \*mask, int size, int mode)

Removes objects or fills holes smaller than a certain size limit. Objects are internally labeled with the Hoshen-Kopelman algorithm.

*image	Pointer to the binary image
*mask	Pointer to the binary mask for region of interest (optional)
size	size limit in number of voxels
mode	fill holes [0] or remove objects[1]

double ConLength(image\_cc \*image, int phase, int every, char \*outfile);

Calculates the pair connectivity as a function of distance considering 8-connectivity. Return value is the mean connectivity length. The step size has be higher than one, especially in 3D, because the evaluation of voxel pairs is rather slow.

*image	Pointer to the binary image
phase	black $[0]$ or white $[1]$
every	step size
*outfile	file name where the pair connectivity data is written to
return value:	mean connectivity length

# 3.8 RGB color images

unsigned char Red(image\_cc \*image, int x, int y);

Reads the red value at given coordinates.

*image	Pointer to the image
х, у	coordinates
return value:	red value

unsigned char Green(image\_cc \*image, int x, int y); Reads the green value at given coordinates.

*image	Pointer to the image
х, у	coordinates
return value:	green value

unsigned char Blue(image\_cc \*image, int x, int y);

Reads the blue value at given coordinates.

*image	Pointer to the image
х, у	coordinates
return value:	blue value

#### void WRed(image\_cc \*in, int x, int y, unsigned char val); Writes the red value val at given coordinates.

*image	Pointer to the image
х, у	coordinates
val	written red value
return value:	no return

void WGreen(image\_cc \*in, int x, int y, unsigned char val); Writes the green value val at given coordinates.

*image	Pointer to the image
х, у	coordinates
val	written green value
return value:	no return

void WBlue(image\_cc \*in, int x, int y, unsigned char val); Writes the blue value val at given coordinates.

*image	Pointer to the image
х, у	coordinates
val	written blue value
return value:	no return

# void StretchRGBHisto(image\_cc \*in, int Rlow, int Rhigh, int Glow, int Ghigh, int Blow, int Bhigh)

Stretches the color histogram according the given limits. The source-image is overwritten.

in	Pointer to the RGB-image.
Rlow, Rhigh	Lower and upper limit for the red channel.
Glow, Ghigh	Lower and upper limit for the green channel.
Blow, Bhigh	Lower and upper limit for the blue channel.

# void StretchRGBBright(image\_cc \*in, int Low, int High)

Stretches the brightness of a RGB-color image between Low and High  $\in [0, 255]$ . The source-image is overwritten.

Low, High Lower und upper limit of brightness

# 3.9 Graphics

The following routines use the library  $\mathtt{PS\_graf}$  to generate nice postscript graphics.

void psPlot(char \*fname, int n, double \*xdat, double \*ydat, int mode) Draws a x-y graphic and stores it to fname.eps.

*fname	Name of output file.
n	Number of data points.
*xdat, *ydat	Arrays of x- and y-data.
mode	Draws symbols for $mode=0$ and lines else.

void psPlotTit(char \*fname,char \*xtitle,char \*ytitle, int n, double \*xdat, double \*ydat, int mode)

Draws a x-y graphic and stores it to fname.eps.

*fname	Name of output file.
*xtitle	title for x axis.
*ytitle	title for y-axis.
n	Number of data points.
*xdat, *ydat	Arrays of x- and y-data.
mode	Draws symbols for mode=0 and lines else.

### void psMultiPlot(char \*fname, int \*ndat, int nplot, double \*\*xdat, double \*\*ydat, int mode)

Draws a x-y graphic of multiple data sets and stores it to fname.eps.

*fname	Name of output file.
*ndat	Array of size nplot containing the number of data points of
	each data set.
nplot	Number of data sets.
**xdat,	<b>**ydat</b> Arrays of size nplot of pointers to the x- and y-data sets.
mode	Draws symbols for $mode=0$ and lines else.

#### void psMultiPlotTit(char \*fname,char \*xtitle,char \*ytitle, int \*ndat, int nplot, double \*\*xdat, double \*\*ydat, int mode)

Draws a x-y graphic of multiple data sets and stores it to fname.eps.

*fname	Name of output file.
*xtitle	title for x axis.
*ytitle	title for y-axis.
*ndat	Array of size nplot containing the number of data points of
	each data set.
nplot	Number of data sets.
**xdat, **yda	tArrays of size nplot of pointers to the x- and y-data sets.
mode	Draws symbols for $mode=0$ and lines else.

# void psDddCircHisto(image\_cc \*im, char \*buf, int prec);

Draws the histogram of a 3D greylevel image considering only the central cylinder of the image.

*im	Pointer to the image.
*buf	Name of output file.
*prec	Only a fraction $(1/\text{prec})$ of the total number of voxels are
	considered.

## void psHisto(image\_cc \*im, char \*buf, int prec);

Draws the histogram of a 2D greylevel image.

*im	Pointer to the image.
*buf	Name of output file (eps format).
*prec	Only a fraction $(1/\text{prec})$ of the total number of voxels are
	considered.

void ps3Dview(char \*fname, image\_cc \*image, double min, double max); Draws a 3D colored view of a ddd-image and write an eps-file.

*fname	name of the resulting eps-file
*image	Pointer to the ddd-image.
min, max	miniumum and maximum greylevel inbetween which the color
	is scaled.

### **3.10** Special routines

void DLine(int x1,int y1,int x2,int y2,image\_cc \*image, int val) Draws a line from x1/y1 to x2/y2.

x1,y1	Coordinates of one end of the line
x2,y2	$\ldots$ and the other.
image	Pointer to the image.
val	Pixel value of the line $\in [0, 255]$ .
return value:	р
	•

ointer to the new image.

# $image_cc *GetVoronoiTes(int Xdim, int Ydim , int Nump)^8$

Generates a Voronoi tesselation based on NumP random seed point. In the resulting image the Voronoi-cells are marked by different grey levels [1-254], the edges between the cells are white [255].

Xdim	x-size of resulting image
Ydim	y-size of resulting image
Nump	number of seed points
return value:	pointer to the resulting image

# image\_cc \*GetPercolClus(int width, int height, double lamx, double lamy, int mode)<sup>8</sup>

Returnes a percolation cluster based on the excursion set of a random greyscale image

width, height size of image

lamx, lamy	Correlation length in x and y
mode	0: random (correlation lengths have no meaning)
	1: gaussian covariance with correlation lengths
return value:	pointer to the binary image of resulting percolation cluster

#### void bObjects(image\_cc \*image,unsigned long \*o,unsigned long \*l)

Counts the number of objects (disconnected parts) and the number of loops (holes within the objects for the dark phase (0) of a binary image.

image	Pointer to the image description structure.
0	Pointer to the number of objects.
1	Pointer to the number of loops.

The edges of the image should be set to non phase (255)

#### int bContour(int x, int y, unsigned char mark, image\_cc \*image)

Marks the edge of an object of the dark phase (0) of a binary image and determines if it is the outer edge of an object or the edge of a hole within the object.

- **x** x coordinate at the edge of an object.
- y y coordinate at the edge of an object.

mark	value to mark the edge $0 < \text{mark} < 255$ .	
image	Pointer to the image description structure.	
return value:	n	
egativ if the marked edge is a hole, positiv else.		

# int bContourCent(int x, int y, int mark, image\_cc \*image, int \*xx, int \*yy)

Determines the geometrical center of an object or a hole within an object, where an object is defined by a values < mark. The value of the center is set to mark+1, the pixels at the borders to mark.

x,y	Coordinates at the border of an object.
mark	Threshold defining the objects.
xx, yy	Adresses to which the coordinates of the object are written.
return value:	> 0 for real objects, $<= 0$ if the contoured border line de-
scribes a hole in an object.	

#### double pDisector(image\_cc \*wnd1, image\_cc \*wnd2)

Calculates an unbiased estimate for the volumetric 3D Euler number  $[L^{-3}]$  of the dark phase (0) from a pair of parallel binary images (a disector). Note that the resolution of the images must be set. The separation of the parallel images should be smaller than the objects considered.

wnd1	Pointer to the first image description structure.
wnd2	Pointer to the image description structure of a parallel image.
return value:	V
olumetric Euler n	umber.

# double BtdDiffusionZ(image\_cc \*in, FILE \*dif, unsigned long max, unsigned long min, int fluxstep, double sens);

Calculates diffusion through phase [1] in z-direction. The concentration at one side is kept fixed, C(z = 0) = const, while the opposite side is fixed at zero  $C(z = z_{max}) = 0$ . Diffusive flow across the plane  $z_{max}$  is calculated iteratively using explicite finite differences.

*in	Pointer to the 3D binary image
*dif	Pointer to the file where the diffusive flow is stored in intervals
	indicated by fluxstep
max	Maximum number of iterations (depends on sample size, may
	be $50.000$ to $1.000.000$ )
min	Minimum number of iterations
fluxstep	Interval of iterations to store the diffusive flux at $z=zmax$ (e.g.
	100)
sens	$\label{eq:interval} Interupt \ criteria: \ stop \ iterations \ if \ flux[j]-flux[j-1] < flux[j]*sens$
return value:	Relative apparent diffusion coefficient $D_s/D_0$

#### void BtdSkelet(image\_cc \*im, int mode, int deadends);

Transform the image to its 3D skeleton.

*im	Pointer to the 3D binary image.
mode	0 = 6 neighbors are considered to be connected, 26 else
deadends	0 = the minimum skeleton without any dead ends is calcu-
	lated, else, dead ends are preserved

#### void BtdContinuity(image\_cc \*im,int mode)

Filter for the continuous part of the phase coded by [1] within a binary 3D-image. The bit-sequenze of mode determines the faces of the 3D-image to which the phase must be connected. (mode=1: face at x=0; mode=63: any face).

im	Pointer to the 3D image
mode	bit position: face $1:x=0, 2:x=xmax, 3:y=0, 4:y=ymax, 5:z=0,$
	6:z=zmax

- Draws a sphere at center xmid/xmid/zmid with radius rad and value 0 if val= 0 and 1 else.

*image		Pointer to the 3d binary image
xmid,	xmid,	zomiordinates of sphere center
rad		radius of sphere
val		value to be written for the sphere
## 3.11 Useful stuff

... typically for internal use

## image\_cc \*LoadRaw(char \*buf, int cols, int rows, int layers, int offset, int nbyte)

Loads grey images of 8-bit or unsigned 16bit. Byte order has to be little Endian and data index is assumed to be x-fastest.

buf	Name of the image to be loaded (with extension).
cols	Number of voxels in x-direction.
rows	Number of voxels in y-direction.
layers	Number of voxels in z-direction.
offset	Header size in bytes.
nbyte	Number of bytes per voxel - 1 for char, 2 for unsigned int.
return value:	pointer to the loaded image.

## void StoreRaw(image\_cc \*im)

Saves a 3D grey image to a raw file and writes file information to a txt file.

im Pointer to the image.

## char \*GetCircElement(int rad, double rx, double ry)

Generates a 2D circular structuring element with radius rad [pixel]. Returns a pointer to an array, a (char), containing the structuring element: a[0] =radius in x-direction [pixel], a[1] = radius in y-direction. a[2...] contains all pixel of the smallest square containing the structuring element with dimension  $(2a[0] + 1) \times (2a[1] + 1)$ . Each pixel is coded by 1 bit which has the value 1 if it is part of the structuring element and 0 else. The position of a pixel (x,y) is identified by pos = y \* (2a[0] + 1) + x. For a given pos you find its value by \*(a + 2 + pos/8) & 1 << pos%8.

rad	radius of the structuring element [voxels]
rx, ry	Resolution (pixel size) in different dimensions [L]
return value:	pointer to the structuring element

char \*GetSphereElement(int rad, double rx, double ry, double rz) Generates a spherical structuring element with radius rad [voxels].

rad	radius	of the	e structuring	element	[voxels]

rx, ry, rz Resolution in different dimensions [L]

return value: pointer to an array, a (char), containing the structuring element: a[0] = radius in x-direction [voxel], a[1] = radius in ydirection, a[2] = radius in z-direction. a[3...] contains all voxels of the smallest cube containing the structuring element with dimension  $(2a[0] + 1) \times (2a[1] + 1) \times (2a[2] + 1)$ . Each voxel is coded by 1 bit which has the value 1 if it is part of the stucturing element and 0 else. The position of a voxel (x,y,z) is identified by pos = z \* (2a[0] + 1) \* (2a[1] + 1) + y \* (2a[0] + 1) + x. For a given pos you find its value by \*(a + 3 + pos/8) & 1 << pos%8.

## char \*GetSphereElementDouble(double rad, double rx, double ry, double rz, int \*vol)

Same as GetSphereElement but with non-integer radius rad [voxels].

rad	radius of the structuring element [voxels]
rx, ry, rz	Resolution in different dimensions [L]
vol	the size of the structuring element [number of voxels] is writ-
	ten to this address
return value:	same as GetSphereElement.

long int \*bQuantMask(image\_cc \*image, int xm, int ym, char \*mask)

Calculates the frequency distribution of 2x2 pixel configurations for a region identified by mask. The format of mask corresponds to that returned by Get-CircElement. The returned pointer is input for the routines to calculate the Minkowski functionals.

*im	Pointer to the binary 2D-image.
int xm, ym	Coordinates of the center of the region described by mask.
*mask	Mask for the region to be analyzed.
return value:	Pointer to the 16-element array containing the frequencies of
pixel	configurations

## float ran3(long \*idum);

Genetrates a random number  $\in [0,1]$ .

*idum	Pointer to the initialization value.
return value:	Random number.

## void GetMinMax(image\_cc \*image, int \*max, int \*min);

Determines the maximum and the minimum value of an image.

*image	Pointer to the image.
*min, *max	The resulting minimum and maximum values.

## int GetMaxGrey(image\_cc \*im)

Determines the maximum grey value of an image not considering the absolut possible maximum of the image type.

*image	Pointer to the image.
return value:	maximum grey value.

## int GetMinGrey(image\_cc \*im)

Determines the minimum grey value of an image not considering the value zero.

\*image Pointer to the image.

return value: minimum grey value.

## void MinMaxf(double \*ar, int n, double \*min, double \*max);

calculates the minimum and maximum value of a double array

*ar	Pointer to the array
n	dimension of the array
*min	addresse to store minimum
*max	addresse to store maximum
return value:	Euler number $[1/L^3]$ in units of image-¿rcol

## double \*\*dmatrix(int n, int m);

allocates a 2D double array with dimensions n x m

n, m	dimensions of the array
return value:	pointer to the allocated memory

## int \*\*imatrix(int n, int m);

allocates a 2D int array with dimensions n x m

n, m	dimensions of the array
return value:	pointer to the allocated memory

## **3.12** Functions of previous versions (still active)

#### void gBin(int LOW, int value1, int value2, image\_cc \*image)

Segmentation of a 8-bit grey scale images according to a threshold. The grey levels smaller or equal to LOW are written to value1 the others are written to value2. If value2 is larger than 255 the original values are maintained for grey levels > LOW.

LOW	Threshold
value1	grey level $[0-255]$
value2	grey level $[0-255]$
image	Pointer to the image

#### void gBibin(int LOW,int HIGH,image\_cc \*image)

Segmentation of a 8-bit grey scale image according to 2 thresholds which are regarded to be the limits of a fuzzy region of the grey scale histogram where the true threshold is expected. The threshold is chosen locally according to the values of the neighboring pixel values (Conditional Dilation).

LOW	lower threshold.
HIGH	upper threshold.
image	Pointer to the image

All pixel of a grey level smaller or equal than LOW are written to 0 as well as all pixel having values smaller than HIGH and at least one direct neighbour smaller than LOW. This algorithm is repeated iteratively until no pixel has to be changed anymore. The other pixel keep their original value.

## int gBilevel(int \*th\_high,int \*th\_low,image\_cc \*image)

Calculates the limits of a fuzzy region on the grey scale of an 8-bit grey level image as required by gBibin for thresholding. The image should have a bimodal grey level histogram where the different modes are not clearly separated (a typical case).

pointer to the upper limit.
pointer to lower limit.
Pointer to the image.
-

- 1 if the histogram is not bimodal, 1 if sucessful
- The bimodal grey level histogram h(x) is analysed to get the lower and upper maxima max1 and max2 as well as the minimum min in between. Then a Gaussian distribution  $\hat{h}(x)$  is fitted to the upper mode. The lower limit is calculated as (max1+min)/2, the upper limit as (p+min)/2 where p is the location on the grey scale where  $\hat{h}(p) = h(min)$ . The resulting values th\_high and th\_low may be used in the function gBibin for conditional dilation.

## image\_cc \*GetDddSegment(image\_cc \*im, int ulx, int uly, int ulz, int nx, int ny, int nz)

Cuts out a segment of a 3D grey level image.

*im	pointer to the original image.
ulx, uly, ulz	coordinates of the upper left corner of the Segment.

nx, ny, nz	number of voxels of the segment in different directions.
return value:	pointer to the segment.

## double \*GetGreyCdf(image\_cc \*im)<sup>8</sup>

Returnes a 255 element array containing the cdf of grey levels

*im	Pointer to the 2D grey image
return value:	cdf array (255 elements)

## image\_cc \*gWaterShed(image\_cc \*image, int conmode)<sup>8</sup>;

Calculates the watershed lines for a grey image (only 8-bit images). The different basins separated by the watershed lines are marked by different grey values, the watershed line is 0. This may be applied to a distance map of a binary image to separate overlapping grains.

*image	Pointer to the grey image
conmode	Connectivity mode: either 4 or 8.
return value:	Pointer to the image containing the watershed and the basins

#### double \*GetAcov(image\_cc \*im, double \*corl, int lag, int mode)<sup>8</sup>

Returnes the autocovariance function of a 2D grey image

*im	Pointer to the image
*corl	address to write the correlation length as result
lag	maximum distance to evaluate ( $\#$ pixels)
mode	indicates which directions are to be considered (bit1=x, bit2=y)
return value:	pointer to an array of dimension lag where the autocovariance
func	tion is stored

## double \*GetSemiVar(image\_cc \*im, int lag, int mode)<sup>8</sup>

Returnes the semivariogram of a 2D grey image

*im	Pointer to the image
lag	maximum distance to evaluate $(\# \text{ pixels})$
mode	indicates which directions are to be considered (bit1=x, bit2=y)
return value:	pointer to an array of dimension lag where the semivariogram is
store	ed

#### void gErode(image\_cc \*image,int step, int mode)

Minimum/maximum filter for 8-bit grey scale images.

image	Pointer to the image.
step	radius of the considered environment
mode	$0 = \min $ minimum, $1 = \max $ filter

Each pixel is set to the minimum/maximum value of its direct neighbours. This is iteratively done **step** times considering the 4 and 8 nearest neighbours alternant starting with 4. The edges of the image are written to 255.

## image\_cc \*gMean2(image\_cc \*image, int mode)

As Mean but returns an image of the variance at each pixel within the defined window of size mode  $\times$  mode

image	Pointer to the image.
mode	side length of the squared operating window (number of pixel)
return value:	Pointer to the image of variances

#### image\_cc \*gSobel(image\_cc \*im, int mode)

Sobel filter (first derivative of local grey levels). The image border is set to 0. For mode=1 the histogram of the resulting image is rescaled to the entire grey scale [0 - max-grey]. (only for 2D images).

*im	Pointer to the image.
return value:	Pointer to the filtered image

#### image\_cc \*gLaplace(image\_cc \*im, int mode)

Laplace filter (second derivative of local grey levels). The image border is set to 0. For mode=1 the histogram of the resulting image is rescaled to the entire grey scale [0 - max-grey]. (only for 2D images).

*im	Pointer to the image.
mode	Rescaling of the result if non-zero.
return value:	Pointer to the filtered image

## double \*gHisto(image\_cc \*im, int precision);

Calculates the grey level histogram (pdf).

*im	Pointer to the image.
precision	only a fraction $(1/\text{precision})$ of pixels is considered
return value:	Pointer to a 255-element array containing the histogram

## image\_cc \*GetRandImage(int col, int row, double rx, double ry, double cx, double cy, int mode)<sup>8</sup>

Returnes a random 2D image with defined correlation lengths in x and y direction

*cdf	cdf of grey levels
col, row	dimensions of resulting image
rx, ry	size of pixel in x and y
cx, cy	correlation lengths ( $\#$ pixel) in x ynd y
mode	0: Gaussian correlation
	1: Lorentz-Correlation model
	2: Exponential-Correlation model
	3: von Karman-Correlation model

return value: pointer to the created image

# image\_cc \*GetCorImage(double \*cdf, int col, int row, double rx, double ry, double cx, double cy, int mode)<sup>8</sup>

Returnes a random 2D image optionally with defined grey distribution function (equal, Gauss or predefined cdf), defined correlation length and defined correlation model (Gauss, Lorentz, Exponentila, von Karman).

\*cdf cdf of grey levels

col, row	dimensions of reulting image
rx, ry	size of pixel in x and y
cx, cy	correlation lengths ( $\#$ pixel) in x ynd y
mode	0: equal distribution without any correlation (cx,cy,cz and cdf
	have no meaning here)
	1: equal grey distribution with gaussian correlation
	2: predefined grey distribution (cdf) distribution and gaussian
	correlation
	3: Gaussian correlation (cdf have no meaning here)
	4: Lorentz-Correlation model (cdf have no meaning here)
	5: Exponential-Correlation model (cdf have no meaning here)
	6: von Karman-Correlation model (cdf have no meaning here)
	<b>**acov</b> covariance in x and y direction (acov[2][lag])
return value:	pointer to the created image

## long \*gConfunc(image\_cc \*image)<sup>8</sup>

Returns the connectivity function of a 2D grey image. The image is binarized for all possible thresholds [0,255] and the corresponding Euler number is dermined which is returned as a vector of 255 elements. The Euler numbers are not normalized by the size of the image.

*image	Pointer to the grey image
return value:	array of 255 Euler numbers

image\_cc \*gCircMask(image\_cc \*im, int xmid, int ymid, int rad, int val)<sup>8,16</sup>
Cuts out a circular image with center xmid, ymid and radius rad. All pixels outside the circle are set to grey level val. The size of the returned image is reduced to

 $2^*$ rad+1.

*image xmid, ymid	Pointer to the grey image center coordinates of the circle
rad	radius of the circle
val	grey level written to the background
return value:	Pointer to the resulting image

### void gHistoMatch(double \*cdf, image\_cc \*image)<sup>8</sup>

Transforms the histogram of an image according to a predefined cdf, typically optained from a source image using the function GetGreyCdf().

*cdf	predefined cdf of grey levels
*image	Pointer to the 2D grey scale image
return value:	no return value

#### void bRemObjects(image\_cc \*image, int size);

Removes all objects (grey level=0) smaller than 'size' (number of pixels)

*image	Pointer to the binary image
size	maximum size of objects (number of pixels) to be removed
return value:	no return value, the original image is changed

### long int \*bQuant(image\_cc \*image);

Calculates the frequency distribution of 16 different pixel configurations in a 2x2 square. The returned pointer is input for the routines to calculate volume density, surface density, length density, curvature and Euler number.

*im	Pointer to the binary 2D-image.
-----	---------------------------------

return value: Pointer to the 16-element array containing frequencies of pixel configurations

## double bVoldens(image\_cc \*image, long int \*h);

Returnes the Area density of a 2D binary structure (0 phase) which corresponds to the Volume density of a 3D structure as estimated from the 2-dimensional section

\*h Pointer to the array of pixel configurations obtained by bQuant() Volume density [-]

## double bSurfdens(image\_cc \*image, long int \*h);

Returnes the Surface density  $S_V \, [\text{cm}^2/\text{cm}^3]$  of the boundary of a 3D binary structure, as estimated from a 2-dimensional binary section.

*h	Pointer to the array of pixel configurations obtained by bQuant()
return value:	Surface density $[L^2/L^3]$ in units of image-¿rcol

#### double bEuler4(image\_cc \*image, long int \*h);

Returnes the Euler number of a 2D binary structure considering 4-connectivity of phase [1]

*h	Pointer to the array of voxel configurations obtained by bQuant()
return value:	Euler number $[1/L^2]$ in units of image-¿rcol

#### double bEuler8(image\_cc \*image, long int \*h);

Returnes the Euler number of a 2D binary structure considering 8-connectivity of phase [1]

*h	Pointer to the array of voxel configurations obtained by bQuant()
return value:	Euler number $[1/L^2]$ in units of image-¿rcol

### double bLengthdens(image\_cc \*image, long int \*h);

Returnes the Lengthdensity  $B_A$  [cm/cm<sup>2</sup>] of the boundary of a 2D binary structure

*h	Pointer to the array of voxel configurations obtained by bQuant()
return value:	Length density $[L/L^2]$ in units of image- $i$ rcol

#### double b2DEuler(image\_cc \*image)

Calculates the 2D Euler number [-] of the dark phase (0) of a binary images.

image Pointer to the first image description structure. return value: d imensionless Euler number.

#### void bErode(image\_cc \*image,int step, int mode)

Performs an erosion or dilation of a binary image (0/255).

image	Pointer to the image description structure.
step	radius of the hexagonal structuring element
mode	0 = erosion of the dark phase $(0), 1 = $ dilation

Erosion or dilation is iteratively performed **step** times considering the 4 and 8 nearest neighbours alternant starting with 4. Note that the original image is replaced and the outer shell (1 pixel) is written to 255.

#### void bErodeMir(image\_cc \*image,int step, int mode)

as bErode but the outer shell of width **step** is mirrored so that the complete image is treated.

image	Pointer to the image description structure.
step	radius of the hexagonal structuring element
mode	0 = erosion of the dark phase (0), $1 = $ dilation

## image\_cc \*bErodeMirCirc(image\_cc \*image,int step, int mode)

as bErodeMir but optimal circles are used as structuring elements for erosion. The original image is not replaced, the pointer to the resulting image is returned.

image	Pointer to the image description structure.
step	radius of the hexagonal structuring element
mode	0 = erosion of the dark phase $(0), 1 = $ dilation
return value:	Pointer to the eroded image

#### image\_cc \*bGetDistMap(image\_cc \*image, int \*n, int gval, int gstep);

Converts a binary image to its distance map: Each pixel in the white phase (255) is written to a grey value which corresponds to the distance of that pixel to phase 0. The closest distance gets grey value

tt gval which increases ba steps gstep with distance. The phase 0 is not changed. The total number of distance classes is written to n. Note that it is a good idea to chose the parameters such that n

cdotgstep > 255 - gval. The resulting distance map can be used as input to a watershed segmentation e.g. to separate sintered grains or to calculate Minkowski functions.

ary image
ed distance classes
first distance class
tween adjacent distance classes
age containing the distance map

## image\_cc \*bGetFullDistMap(image\_cc \*image, int \*nblack, int \*nwhite, int gstruc, int gval, int gstep);

Converts a binary image to its full distance map: Each pixel in the white phase (255) is written to a grey value which corresponds to the distance of that pixel to phase 0 and each pixel in the black phase (0) is written to a grey value which corresponds to the distance of that pixel to the white phase (255). The boundary of the black phase is set to gstruc, the closest distance gets grey value gstruc+/-gval where the sign depends on whether the distance is in the white or in the black phase. It

is increased by steps gstep with distance. The total number of distance classes is written to nblack and nwhite respectively. Note that it is a good idea to chose the parameters such that nwhite·gstep < 255 -(gstruc+gval) and nblack·gstep<gstruc-gval. The maximum number of classes is limited by MAXDILAT=100 (parameter can be changed in quantim4.h). The resulting distance map can be used to calculate Minkowski functions.

*image	Pointer to the binary image
*nblack	Number of detected distance classes in the black phase
*nwhite	Number of detected distance classes in the white phase
gstruc	Grey level written to the boundary of the black phase
gval	Grey level for the first distance class
gstep	Grey level step between adjacent distance classes
return value:	Pointer to the image containing the distance map

## 

As bGetDistMap(), this function converts a binaryimage to its distance map. Additionally a 'granulometry map' is calculated where each pixel in phase 1 (255) is written to a grey value which corresponds to the diameter of the maximum circle that can be placed inside phase 1 at that location (corresponding to the 'opening size'). The smallest circle is marked by the grey value

tt gval which increases by steps

tt gstep with the size of the ball.

*image	Pointer to the binary image
*distance	Must initially be a copy of
	tt image and contains the resulting distance map after execution
*opened	Must initially be a copy of
-	tt image and contains the resulting granulometry map after exe-
	cution
gval	Grey level for the smallest size class
gstep	Grey level step between subsequent size classes
return value:	Number of detected size classes

## image\_cc \*GetDistOpenCloseMap(image\_cc \*im, double gstep)

image\_cc \*GetDistOpenCloseMap(image\_cc \*im, double gstep, int maxdist) Generates an opening-map (black phase) and a closing-map (white phase) of a binary image, which is a greyscale image where the grey value of each pixel indicates the 'opening size' ('closing-size') of the black (white) phase. gstep is the difference in grey level for the opening/closing of 1 pixel. This function is valid for isotropc pixel geometry. This function requires considerable computation time, so the maximum size for openings(closings) can be limited by maxdist.

*image	Pointer to the binary image.
gstep	scaling of the grey levels of the opening/closing map
maxdist	maximum opening size to be considered
return value:	Pointer to the resulting image

## unsigned long bErodeMark(image\_cc \*image, int mark, int step);

Performs a dilation (0-phase) of a binary image with a circular structuring element of radius **step**. The dilated area is marked with the greylevel **mark**. The number of marked pixel is returned.

*image	Pointer to the binary image
step	Radius of structuring element
mark	Greylevel to mark dilated pixel
return value:	Number of marked pixel

#### void bLogAnd(image\_cc \*wnd1, image\_cc \*wnd2)

Logical AND relation (intersection) of two binary images.

wnd1	Pointer to the first image description structure.
wnd2	Pointer to the second image description structure.

The result is written to wnd1

## void bLogOr(image\_cc \*wnd1, image\_cc \*wnd2)

Logical OR relation (unification) of two binary images.

wnd1	Pointer to the first image description structure.
wnd2	Pointer to the second image description structure.

The result is written to wnd1

## void bAddition(image\_cc \*wnd1, image\_cc \*wnd2, int gv1, int gv2) Addition of two images.

wnd1	Pointer to the first image description structure.
wnd2	Pointer to the second image description structure.
gv1	grey level to be set for phase in wnd1.
gv2	grey level to be set for phase in wnd2.

the 0-values of the two images are set to gv1 and gv2 respectively, their intersection is set to 0. The result is written to wnd1

### void bHitMiss(image\_cc \*im, int Mx, int My, long MP, long MNP)

Hit or Miss Transform of a binary image. Structuring elemnts are still restricted to a size  $\leq 5 \times 5$  pixel (Mx, My  $\in [1,2]$ ).

*im	Pointer to the image.
Mx My	Operating window of the structuring element in x and y direction, $(2Mx+1) \times (2My+1)$
MP	Each nonzero bit of MP indicates membership to the structuring element at position $x = bitpos/(2Mx+1)$ and $y = bitpos modulo (2Mx+1)$ .
MNP	Each nonzero bit of MNP indicates explicit non-membership to the structuring elemnt at position $x = bitpos/(2Mx+1)$ and $y = bitpos$ modulo (2Mx+1). Coordinates which are neither described by MP nor MNP (the corresponding bits are zero in both variables) are not significant.

## long int \*bQuantRecMask(image\_cc \*image, int xdim,int ydim, int xul, int yul);

- Calculates the frequency distribution of 16 different pixel configurations within a 2x2 square for a rectangular region. The returned pointer is input for the routines to calculate volume density, surface density, length density, curvature and Euler number.
  - \*im Pointer to the binary 2D-image.

int xdim, ydimmExtension of the rectangular region [pixel].

int xul, int yuCoordinates of the upper left corner.

return value: Pointer to the 16-element array containing frequencies of pixel configurations

# void SaveRGBImageSeg(image\_cc \*image, char \*buf, int ulx, int uly, int drx, int dry)

Saves a rectangular segment of a RGB image.

image	Pointer to the image description structure.
buf	Name of the tif-image to be saved without extension.
ulx	x coordinate of the upper left corner of the segment
uly	y coordinate of the upper left corner
drx	x coordinate of the lower right corner
dry	y coordinate of the lower right corner

### ddd stuff $\mathbf{ddd}\ \mathbf{images}$

#### void SetDddShell(image\_cc \*im, int thick, int val);

Writes the complete shell of thickness thick to val

thick	Thickness of the shell
val	Value written to the shell
return value:	no return value

### image\_cc \*DddResRed(image\_cc \*image, int mode)

Reduces image size and herewith resolution by averaging over regions of size  $(2 \mod +1)^2$ .

*im	pointer to the original image.
mode	mode of reduction.
return value:	pointer to the resulting image.

## image\_cc \*GetRandDDDImage(int col, int row, int dep, double rx,, double ry, double rz)

Creates a 3D grey scale image in which the values of voxels are set randomly.

col,row,dep	Size of the image $(x,y,z)$ .
rx,ry,rz	Resolution (size of voxels) in different dimensions (x,y,z).
return value:	pointer to the created image.

## void DddMinMax(image\_cc \*im,int mode);

Minimum/Maximum filter for a 3D grey scale image which operates within a 3x3x3 window.

*im	pointer to the image.
mode	if 0 minimum, else maximum.

#### image\_cc \*DddBin(image\_cc \*im, unsigned char thresh);

Converts a 3D grey scale image to a 3D binary image (btd-format) according to a threshold. Values <=thresh are coded by 0 and by 1 else.

im	Pointer to the 3D grey scale image.
thresh	Threshold on the grey scale.
return value:	pointer to the 3D binary image (btd-format).

#### void DddBibin(int LOW,int HIGH,image\_cc \*im);

Segments an 3D grey scale image according to 2 thresholds which are regarded to be the limits of a fuzzy region of the grey scale histogram of the image (Conditional Dilation). All pixel of a grey level smaller or equal than LOW are written to 0 as well as all pixel having values smaller than HIGH and at least one direct neighbour smaller than LOW. This algorithm is repeated iteratively until no pixel is to be changed. The other pixel keep their original value. This function overwrites the original image.

LOW	lower threshold.
HIGH	upper threshold.
image	Pointer to the image.

#### image\_cc \*DddWaterShed(image\_cc \*image, int conmode);

Calculates the watershed lines for a 3D grey image. The different basins separated by the watershed lines are marked by different grey values, the watershed is written to 0. This may be applied to a distance map of a binary image to separate overlapping grains. The distance map is obtained by BtdGetDistOpenMap() or BtdGetDistMap().

*image	Pointer to the grey image
conmode	Connectivity mode: either 6 or 26.
return value:	Pointer to the image containing the watershed and the basins

# void DddClas(image\_cc \*im, int Nclas, unsigned char \*th, unsigned char \*gval);

Transforms a 3D grey scale image by dividing the grey scale into a number (Nclas) of discrete classes. The upper limits of the grey values of the different classes are provided by **\*th** and the values to be written for each class by gval.

im	Pointer to the 3D grey scale image.
Nclas	Number of different classes.
*th	Array of Nclas thresholds $\in [0,255]$ starting with lower values at th[0].
*gval	Array of Nclas greylevels $\in [0,255]$ to be written for the corresponding classes.

#### double \*DddHisto(image\_cc \*im, int precision);

Returns the grey-histogram of a 3D grey scale image.

Pointer to the image.	
Only a fraction (1/precision) of the total number of voxels are	
considered.	
Array with 255 elements containing the relative frequency of the	
corresponding grey value.	

#### double \*DddCircHisto(image\_cc \*im, int precision, int rad);

Same as DddHisto but only consideres a central cylinder of radius rad.

*im	Pointer to the image.
precision	Only a fraction $(1/\text{precision})$ of the total number of voxels are
	considered.
rad	Radius of the central cylinder to be considered (number of pixel).
return value:	Array with 255 elements containing the relative frequency of the
corresponding grey value.	

#### double \*GetDddGreyCdf(image\_cc \*im)

Returns the cdf of grey levels for a 3D-grey scale image. This cdf can be used by GetCorDDDImage to generate a random structure accordingly.

*im	Pointer to the image.
return value:	Array with 256 elements describing the cdf

# void DddEulerFunc(image\_cc \*im, int \*num, double \*\*xdat, double \*\*ydat, int prec)

Calculates the connectivity function of a 3D grey scale image.(Take care that resolution of the image is set correctly!)

*im	Pointer to the image.
*num	Adress where the number of function value are written to.
**xdat, **ydat	Pointer to the adress where the function values are written to
-	<pre>(xdat[i]=threshold of greylevel, ydat[i]= Euler number).</pre>
	Step of grey thresholds for which the Euler number is calculated.
	Number of function values: 255/prec.

## image\_cc \*GetCorDDDImage(double \*cdf, int col,int row,int dep,double rx,double ry, double rz,double cx,double cy, double cz, int mode)

Generates a random 3D greylevel structure with predefined grey-histogram, correlation length and correlation model. The maximum size is restricted to  $64^3$ . The structure is periodic only for this maximum size. UNDER CONSTRUCTION!! NOT EVERYTHING WORKS!! USE WITH CARE!!

*cdf	Pointer to the 256-element array containing the cdf of grey levels.
col, row, dep	Size of the image (number of voxels in x, y and z).
rx, ry, ry	Size of the voxels in x, y and z.
cx, cy, cz	Correlation lengths (number of voxels in x, y and z).
mode	Correlation model: $0 =$ completely random without correlation
	(cx, cy, cz are ignored); $1 = $ Gaussian model; $2 = $ Mirrored gaus-
	sian (just try and you will get an idea or check the source to dig

out that strange guy); 3 = Lorentz; 4 = Exponential, 5 = von Karman.

return value: pointer to the generated image.

## image\_cc \*GetCorDDDImage2(double \*cdf, int col, int row, int dep, double rx, double ry, double rz, double cx, double cy, double cz, int mode);

Returns a random 3D grey image with predefined grey histogram and/or correlation lengths. The image is periodic only for dimensions = power of 2 UNDER CON-STRUCTION!! NOT EVERYTHING WORKS!! USE WITH CARE!!

*cdf	Pointer to the 256-element array containing the cumulative density $\$
	function of grey levels.
col, row, dep	Size of the image (number of voxels in x, y and z).
rx, ry, ry	Size of the voxels in x, y and z.
cx, cy, cz	Correlation lengths (number of voxels in x, y and z).
mode	Correlation model:
	0 = equal grey distribution without any correlation (cx,cy,cz and
	cdf have no meaning here)
	1 = equal grey distribution with correlation (correlation lengths
	of resulting image will be different from cx, cy, cz!)
	2 = predefined greylevel (cdf) distribution and gaussian correla-
	tion (correlation lengths of resulting image will be different from
	cx, cy, cz!)
	3 = Gaussian covariance (cdf have no meaning here and in the
	following modes)
	4 = Lorentz covariance
	4 = Exponential covariance
	5 = von Karman covariance
return value:	pointer to the generated image.

## double \*GetDddAcov(image\_cc \*im, double \*corl, int lag, int mode)

Calculates the autocovariance function and the correlation length of a 3D greylevel image the correlation length is written to \*corl. The first 3 bits of mode indicate which directions (x,y,z) are to be considered.

Pointer to the image.
Adress where the correlation length is written to.
Maximum distance considered (number of pixel).
indicates which directions are to be considered (bit1=x, bit2=y,
bit3=z)
pointer to an arry of dimension lag where the autocovariance func-
s stored.

## void DddDrawCylinder(image\_cc \*image, int xmid, int ymid, int rad, int len, int val);

Draws a cylinder at center tt xmid/xmid with length len and radius rad and value val.

\*image Pointer to the 3d binary image

coordinates of cylinder center
length of cylinder
radius of cylinder
value to be written for the cylinder

btd stuff btd images

#### void BtdErodeFilter(image\_cc \*im, int step, int mode)

Performs an erosion of the phase mode by a spherical structuring element of radius step. Note that an erosion of phase 1 corresponds to a dilation of phase 0. The outer shell of the eroded image (where the structuring element cannot be placed entirely into the image volume) is set to 0. This function is a filter, meaning the original image is lost after this operation (see \*BtdErode()).

im	Pointer to the 3D image
step	radius of the structuring element [voxels]
mode	phase to be eroded $[0,1]$

### image\_cc \*BtdErode(image\_cc \*im, int step, int mode)

Performs an erosion of the phase mode by a spherical structuring element of radius step. Note that an erosion of phase 1 corresponds to a dilation of phase 0. The outer shell of the eroded image (where the structuring element cannot be placed entirely into the image volume) is cut off.

im	Pointer to the 3D image
step	radius of the structuring element [voxels]
mode	phase to be eroded $[0,1]$
return value:	р

ointer to the 3D image containing erroded subvolume.

### image\_cc \*BtdErodeMir(image\_cc \*im, int step, int mode)

Same as BtdErode except that the shell is not cut off. To calculate the erosion at the border of the image, it is enlarged by mirroring the structure at the boundaries.

*im	Pointer to the 3D image
step	Radius of the structuring element[voxels]
mode	Phase to be eroded [0,1]
return value:	Pointer to the image containing the eroded structure

## image\_cc \*BtdErodeMirDouble(image\_cc \*im, double step, int mode)

Same as BtdErodeMir except that the radius of the structuring element is of type double (typically 0.5).

*im	Pointer to the 3D image
step	Radius of the structuring element[voxels]
mode	Phase to be eroded $[0,1]$
return value:	Pointer to the image containing the eroded structure

#### image\_cc \*BtdOpen(image\_cc \*im, int step, int mode)

Performs an opening (erosion followed by dilation) or closing (dilation followed by erosion) of a binary 3D image using a spherical structuring element of radius step. The outer shell of the eroded image (where the structuring element cannot be placed entirely into the image volume) is cut off.

im	Pointer to the 3D image
step	radius of the structuring element [voxels]
mode	opening or closing $[0,1]$
return value:	р
$\cdot$	

ointer to the 3D image containing opened (closed) 3D-image.

## image\_cc \*BtdGetDistMap(image\_cc \*image, int \*n, int gval, int gstep);

Converts a binary 3d image (btd-format) to its distance map (ddd-format): Each voxel in phase 1 is written to a grey value which corresponds to the distance of that voxel to phase 0. The closest distance gets grey value gval which increases ba steps gstep with distance. The phase 0 is not changed. The total number of distance classes is written to n. Note that it is a good idea to chose the parameters such that  $n \cdot gstep < 255 - gval$ . The resulting distance map can be used as input to a watershed segmentation e.g. to separate sintered grains.

*image	Pointer to the 3D binary image (btd-format)
*n	Number of detected distance classes
gval	Grey level for the first distance class
gstaep	Grey level step between adjacent distance classes
return value:	Pointer to the ddd-image containing the distance map

# int BtdGetDistOpenMap(image\_cc \*image, image\_cc \*distance, image\_cc \*opened, int gval, int gstep)

As BtdGetDistMap(), this function converts a binary 3d image (btd-format) to its distance map (ddd-format). Additionally a 'granulometry map' is calculated where each voxel in phase 1 is written to a grey value which corresponds to the diameter of the maximum ball that can be placed inside phase 1 at that location (corresponding to the 'opening size'). The smallest ball is marked by the grey value gval which increases by steps gstep with the size of the ball.

*image	Pointer to the 3D binary image (btd-format)
*distance	Must be a copy of image in ddd-format and contains the resulting
	distance map after execution
*opened	Must be a copy of image in ddd-format and contains the resulting
	distance map after execution
gval	Grey level for the smallest size class
gstep	Grey level step between subsequent size classes
return value:	Number of detected size classes

## int BtdGetDistOpenMapDouble(image\_cc \*image, image\_cc \*distance, image\_cc \*opened, int gval, int gstep, double step)

As BtdGetDistOpenMap(), but the diameter of the spherical structuring element is incremented by steps of 0.5 to get a better resolution of the size distribution. This function converts a binary 3d image (btd-format) to its distance map (ddd-format). Additionally a 'granulometry map' is calculated where each voxel in phase 1 is written to a grey value which corresponds to the diameter of the maximum ball that can be placed inside phase 1 at that location (corresponding to the 'opening size'). The smallest ball is marked by the grey value

tt gval which increases by steps

tt gstep with the size of the ball.

*image	Pointer to the 3D binary image (btd-format)	
*distance	Must be a copy of	
	tt image in ddd-format and contains the resulting distance map	
	after execution	
*opened	Must be a copy of	
	tt image in ddd-format and contains the resulting distance map	
	after execution	
gval	Grey level for the smallest size class	
gstep	Grey level step between subsequent size classes	
step	increment for structuring element (typically $0.5$ )	
return value:	Number of detected size classes	

#### void SetBtdShell(image\_cc \*im, int dx, int dy, int dz, int mode)

Writes the shell of a 3D image with the thickness of dx, dy, dz [voxels] to the value mode.

im	Pointer to the 3D image
dx, dy, dz	thickness of the shell in different dimensions [voxels]
mode	Value to be written to the shell $[0,1]$

#### double BtdEuler(image\_cc \*im);

Claculates the volumetric 3D Euler number. Note that the resolutions im->ncol, im->nrow and im->nbits must be set to a meaningful value. The result is given in the corresponding unit  $[1/L^3]$ .

*im	Pointer to the 3D binary image.
return value:	Volumetric Euler number $L^{-3}$ )

#### double BtdVolSurf(image\_cc \*im, double \*vv, double \*sv);

Claculates the volume density (vv) and surface density (sv).

*im	Pointer to the 3D binary image.
*vv, *sv	Addresses where the results are written to
return value:	Volume of the sample in units of im-¿rcol

#### long int \*BtdQuant(image\_cc \*image);

Calculates the frequency distribution of 255 different voxel configurations in a 2x2x2 cube. The returned pointer is input for the routines to calculate volume density, surface density, mean curvature and Euler number.

\*im Pointer to the binary 3D-image.

return value: Pointer to the 255-element array containing frequencies of voxel configurations

### long int \*BtdQuantMask(image\_cc \*image, int xm, int ym, int zm, char \*mask);

Calculates the frequency distribution of the 255 different voxel configurations within a 2x2x2 cube for a region identified by mask. The format of mask corresponds to that returned by GetSphereElement. The returned pointer is input for the routines to calculate volume density, surface density, mean curvature and Euler number.

*im	Pointer to the binary 3D-image.
int xm, ym, zm	Coordinates of the center of the region described by mask.
*mask	description of the region to be analyzed.
return value:	Pointer to the 255-element array containing frequencies of voxel
configurations	

#### double BtdVoldens(long int \*h);

Returns the volume density of the phase coded by [1]

\*hPointer to the array of voxel configurations obtained by BtdQuant()return value:volume density [-]

#### double BtdSurfdens(image\_cc \*image, long int \*h);

Returns the surface density of a binary structure

*h	Pointer to the array of voxel configurations obtained by BtdQuant()
return value:	surface density $[L^2/L^3]$ in units of image-¿rcol

#### double BtdMeancurv(image\_cc \*image, long int \*h);

Returns the mean curvature of a binary structure

*h	Pointer to the array of voxel configurations obtained by BtdQuant()
return value:	mean curvature in units of image-¿rcol

#### double BtdEuler6(image\_cc \*image, long int \*h);

Returns the volumetric Euler number of a 3D binary structure considering 6-connectivity of phase [1]

\*hPointer to the array of voxel configurations obtained by BtdQuant()return value:Euler number [1/L<sup>3</sup>] in units of image-¿rcol

## double BtdEuler26(image\_cc \*image, long int \*h);

Returns the volumetric Euler number of a 3D binary structure considering 26-connectivity of phase [1]

*h	Pointer to the array of voxel configurations obtained by BtdQuant()
return value:	Euler number $[1/L^3]$ in units of image- $i$ rcol

#### RGB stuff **RGB images**

## image\_cc \*ChangeResolutionRGB(image\_cc \*image, int newx, int newy);

Returns the pointer to a rescaled RGB-image. The new dimensions are **newx** and **newy** in x and y direction respectively.

*image	Pointer to the original image
newx, newy	new dimensions in <b>x</b> and <b>y</b> direction
return value:	pointer to the rescaled image

## image\_cc \*TurnRGBImage(image\_cc \*im, double grad)

rotates a RGB image by the angle grad

*image	Pointer to the original image
grad	angle to be turned (degree)
return value:	pointer to the rescaled image

### image\_cc \*FlipRGBImage(image\_cc \*im);

Flip the RGB-image in x direction.

*image	Pointer to the original image
return value:	pointer to the fliped image

# void WRGBPixel(image\_cc \*in, int x,int y,unsigned char rval,unsigned char gval,unsigned char bval);

Writes the RGB values at given coordinates.

*image		Pointer to the image
	х, у	coordinates
	rval, gval,	bvawritten rgb values
	return value:	no return